

普遍法则与架构

Universal laws and architectures:

Theory and lessons from
brains, hearts, cells, grids, nets, bugs,
fluids, bodies, planes, docs, fire, fashion,
earthquakes, music, buildings, cities, art, running,
cycling, throwing, **Synesthesia**, spacecraft, statistical mechanics

and zombies

John Doyle 道耀

Jean-Lou Chameau Professor
Control and Dynamical Systems, EE, & BioE

Ca#1tech

<https://www.cds.caltech.edu/~doyle>

普遍法则与架构

Universal laws
and architectures:
The videos

The following preview is
approved for all audiences.

~~and subtitles~~

<https://www.cds.caltech.edu/~doyle>

Thanks to

- **Yorie Nakahira**, Nikolai Matni, Yuh Shiang Wang, James Anderson, Yoke Peng Leong, Quanying Liu, ...
- **Terry Sejnowski, Marie Csete**, Simon Laughlin, Richard Murray
- ARO (MURI), NSF, AFOSR, DARPA
- Google, Cisco, Northrup-Grumman, Huawei

In attendance

Reading

Theoretical foundations for layered architectures and speed-accuracy tradeoffs in sensorimotor control

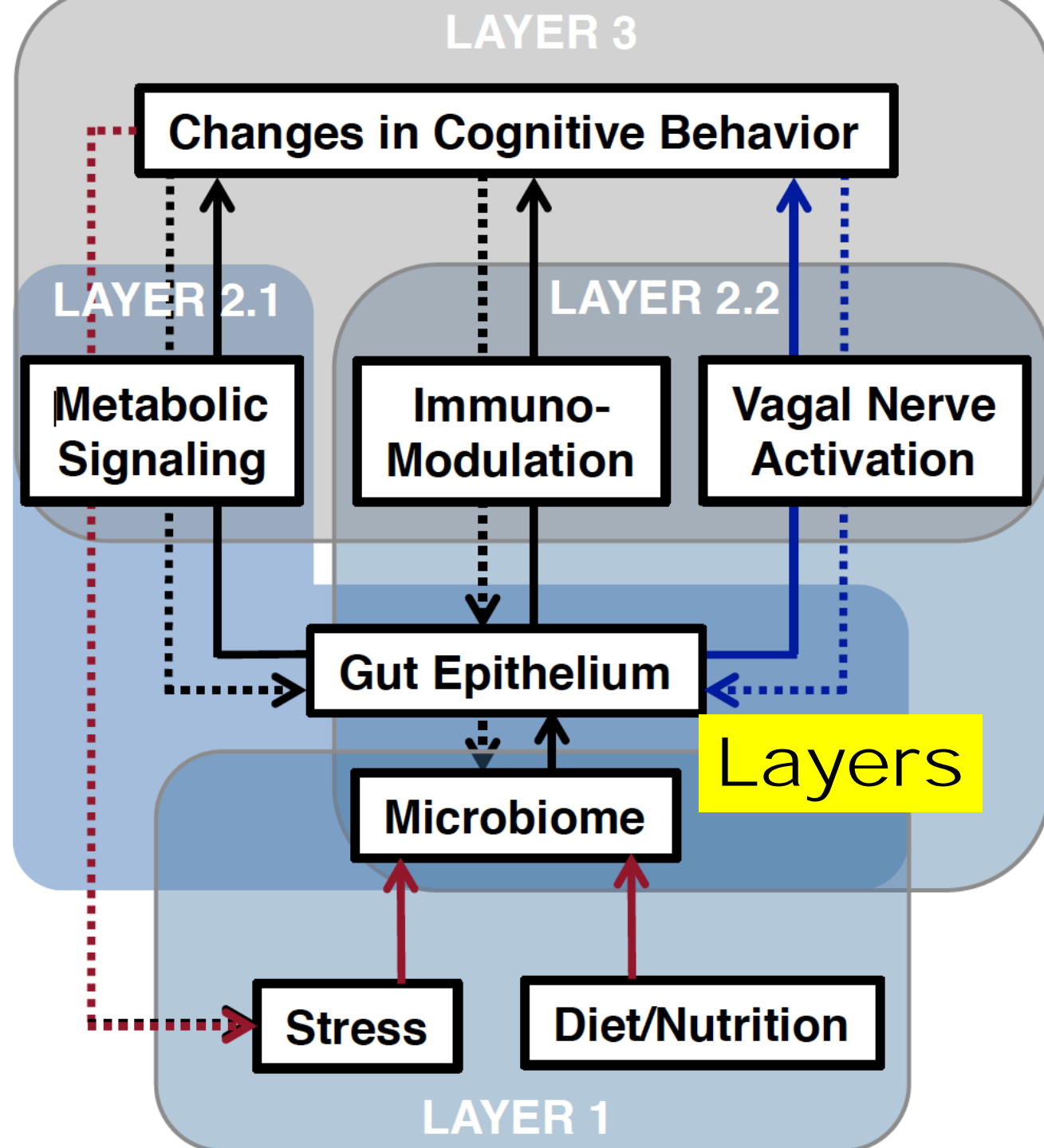
Yorie Nakahira¹, Quanying Liu¹, Natalie Bernat¹, Terry Sejnowski², John Doyle¹

Experimental and educational platforms for studying architecture and tradeoffs in human sensorimotor control

Quanying Liu¹, Yorie Nakahira¹, Ahkeel Mohideen¹, Adam Dai¹,
Sunghoon Choi¹, Angelina Pan¹, Dimitar M. Ho¹ and John C. Doyle¹

System Level Synthesis: A Tutorial

John C. Doyle, Nikolai Matni, Yuh-Shyang Wang, James Anderson, and Steven Low



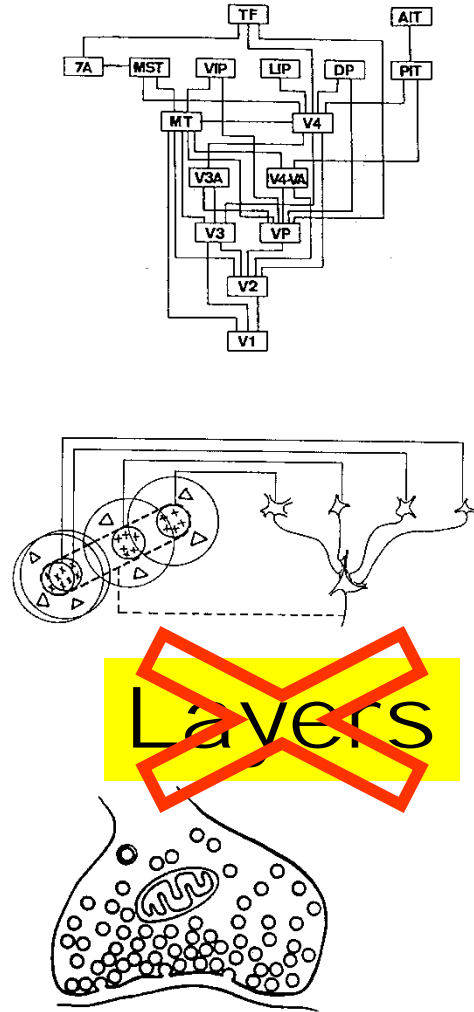
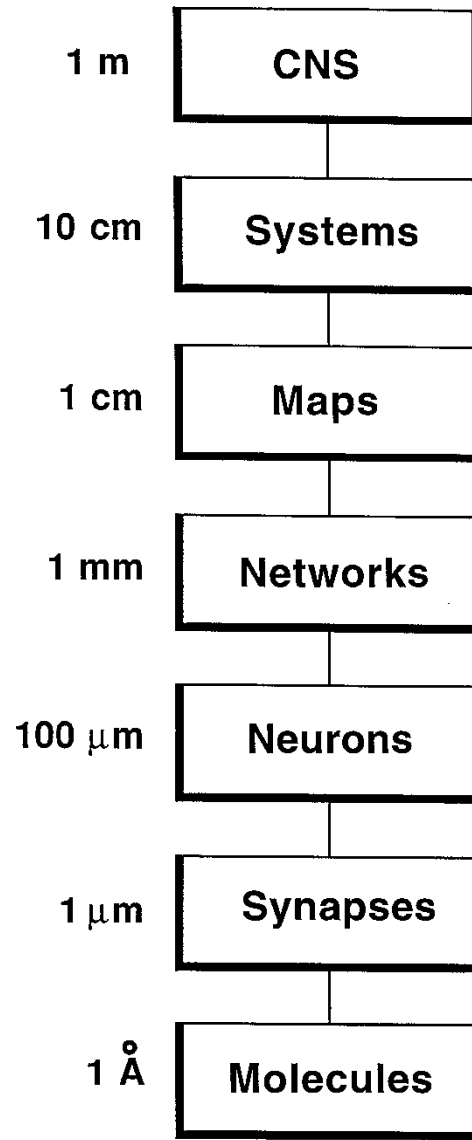
Extreme diversity

What is done?
Where?
How?
Why?
Necessary?

Elaine Hsiao, UCLA

Levels of Investigation

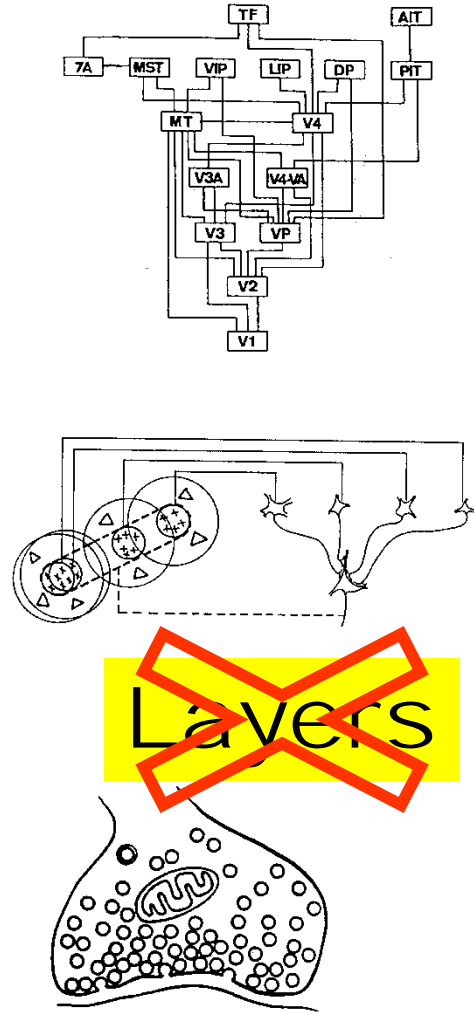
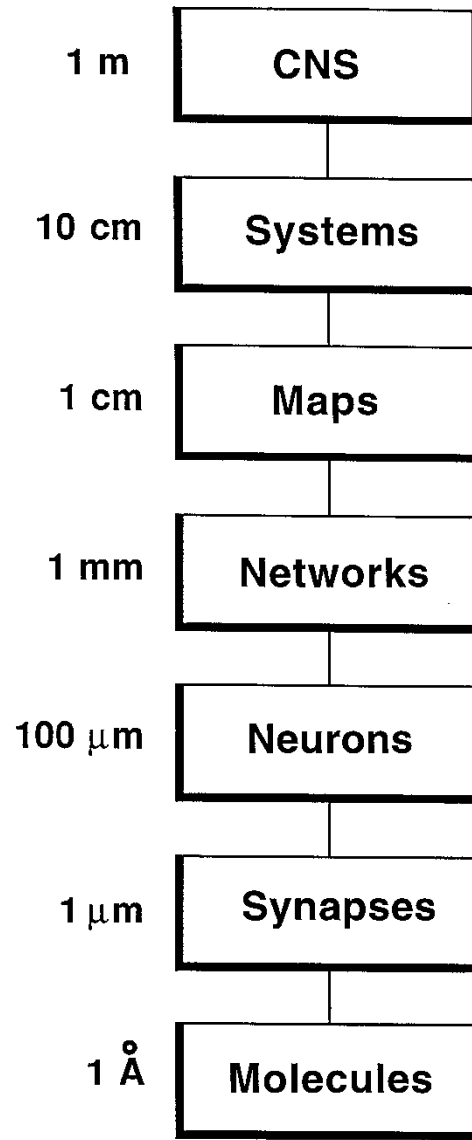
Extreme diversity



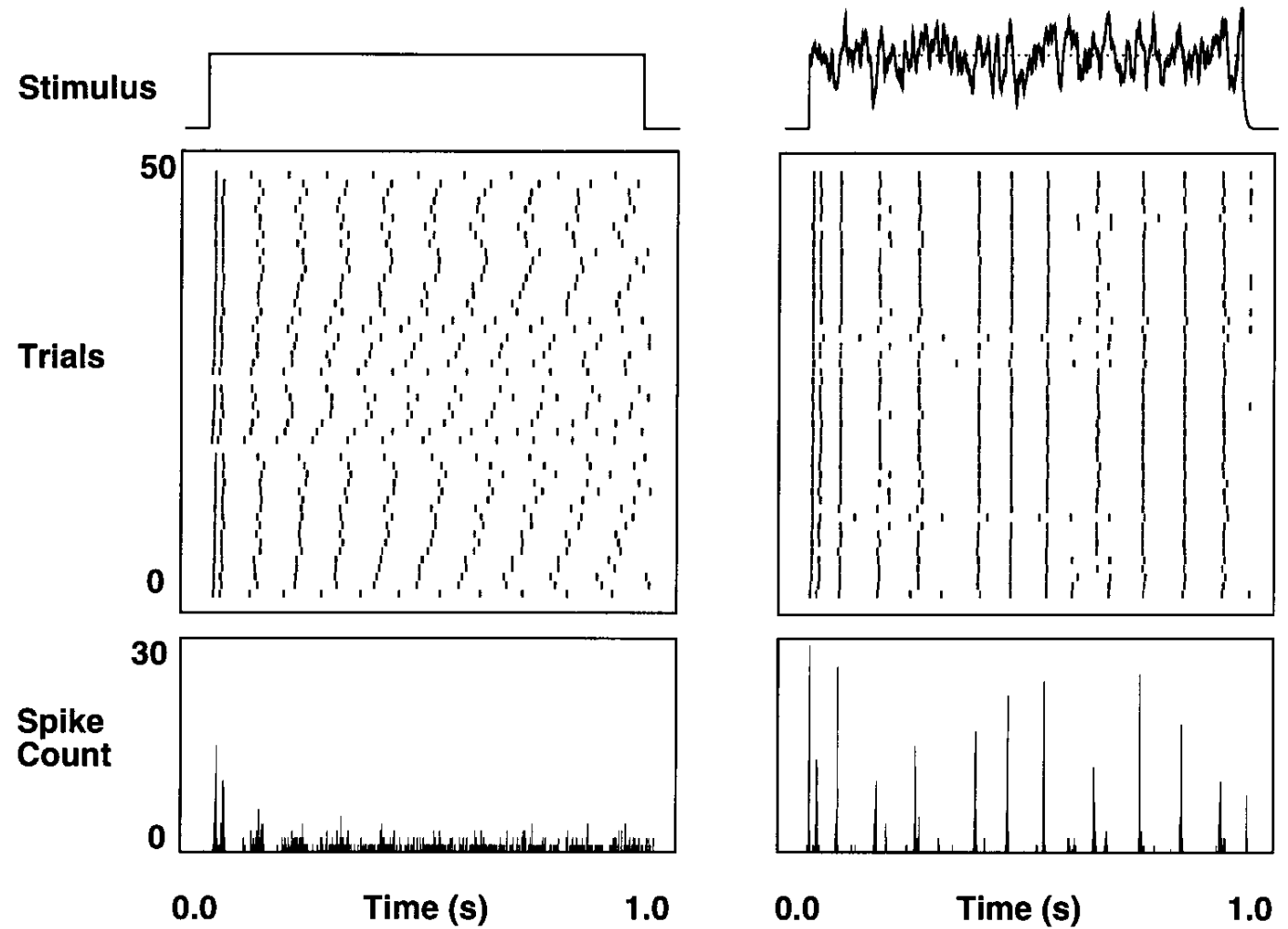
Levels
+
Layers

Sejnowski

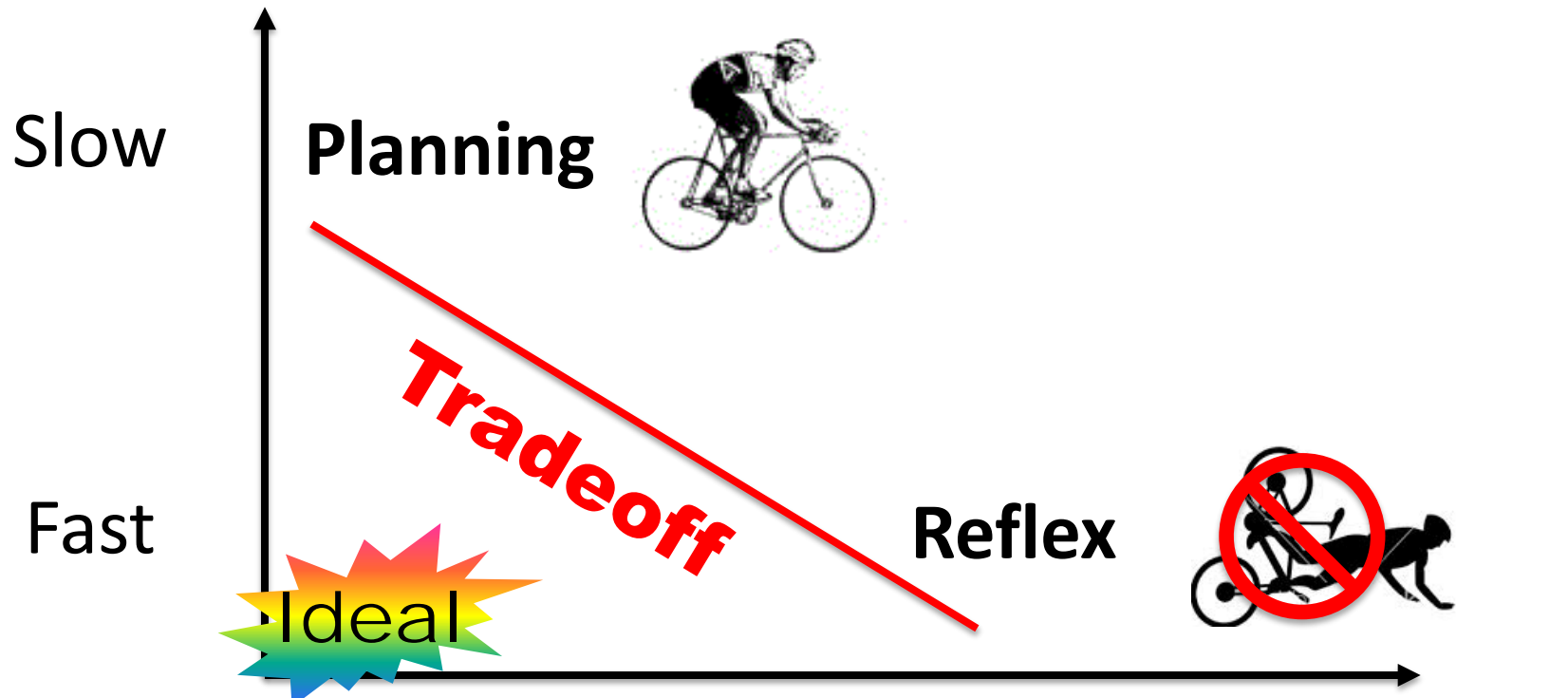
Levels of Investigation



Spike Timing Reliability



Mainen and Sejnowski, 1995

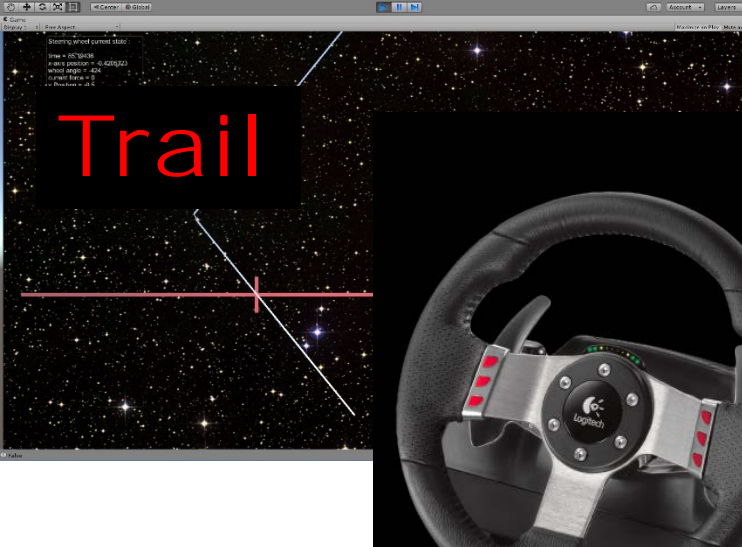


Accurate
 Flexible
 Centralized
 Conscious
 Deliberate
 Stable virtual

Inaccurate
 Rigid
 Localized, distributed
 Unconscious
 Automatic
 Unstable real dynamics

Layers





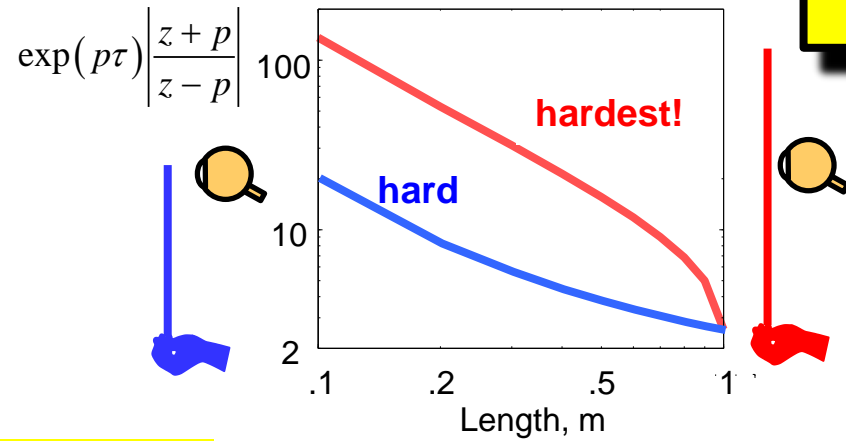
Bumps

Object motion

Slow

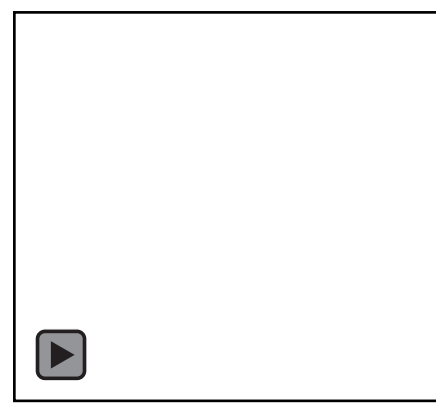


Experiments



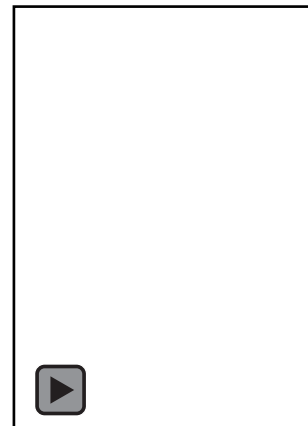
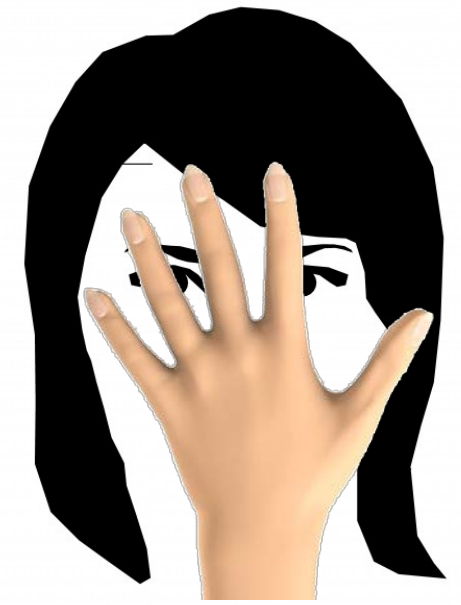
Waterbed

$$\left. \exp\left(\int \ln|T|\right) \right\|T\|_{\infty} \geq \exp(p\tau) \frac{z+p}{z-p}$$



Head motion

Fast



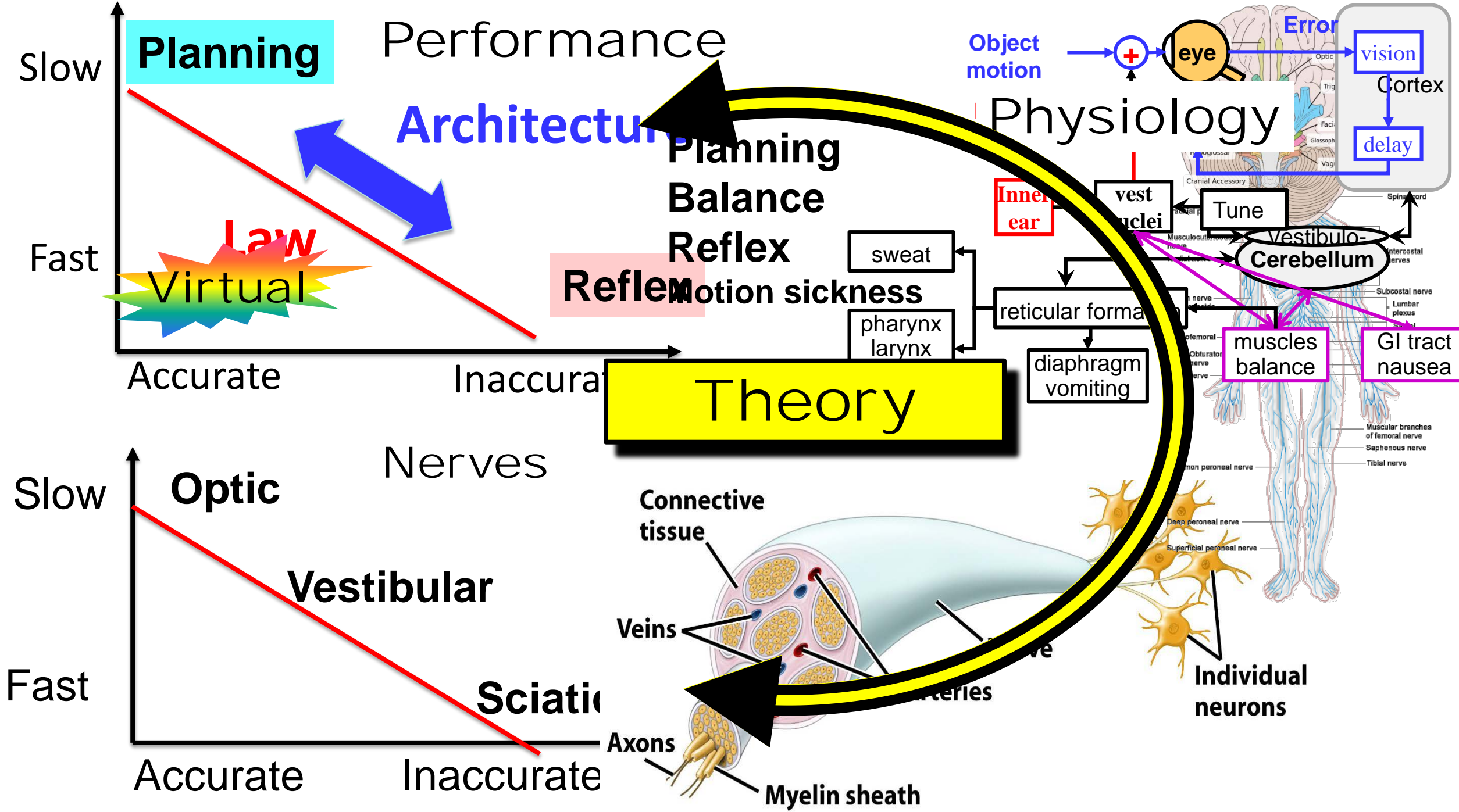


Figure 20.11. Diagram illustrating the relationship between performance, accuracy, speed, and theory in a biological context.

Slow

Planning



Fast

Ideal

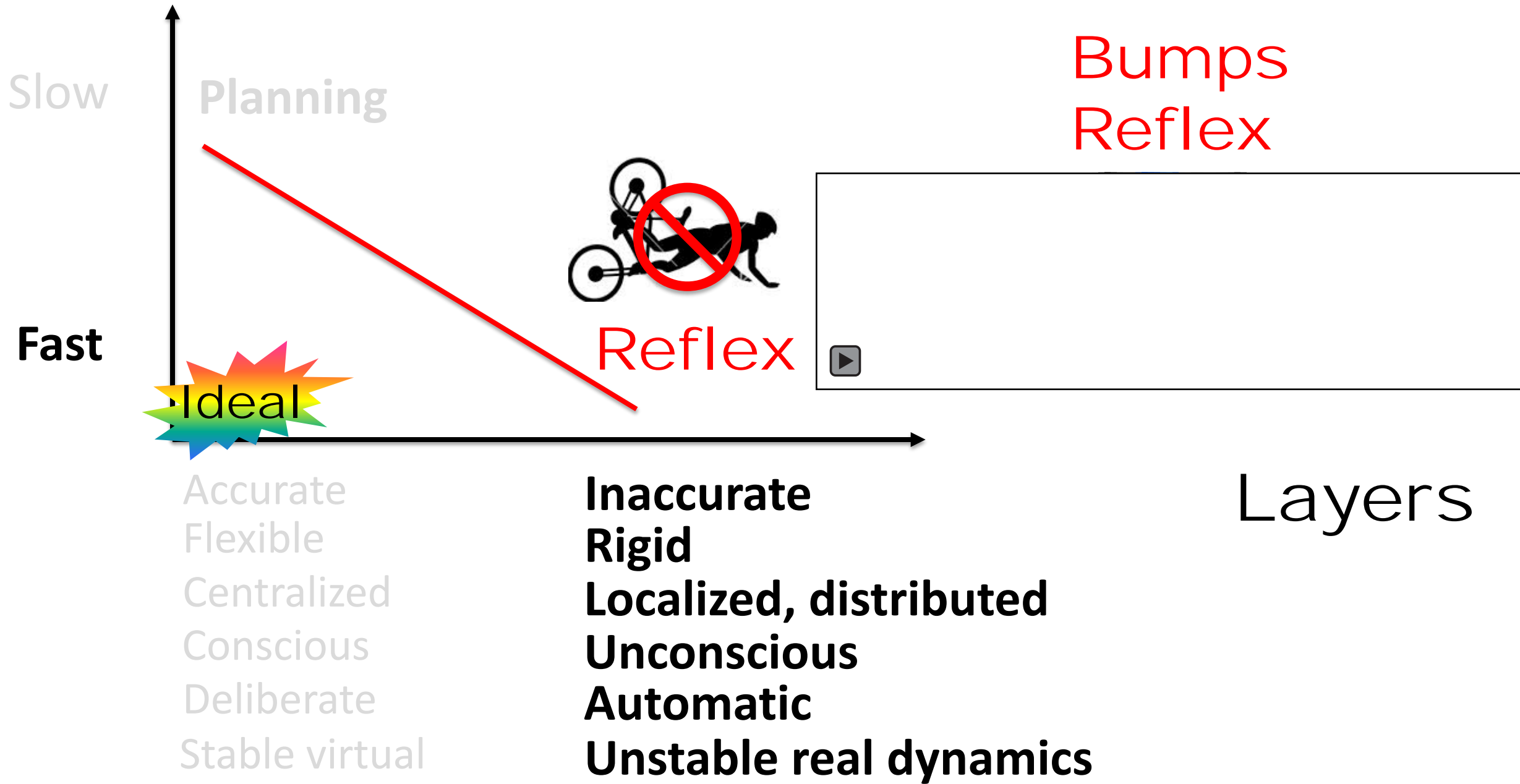
Reflex

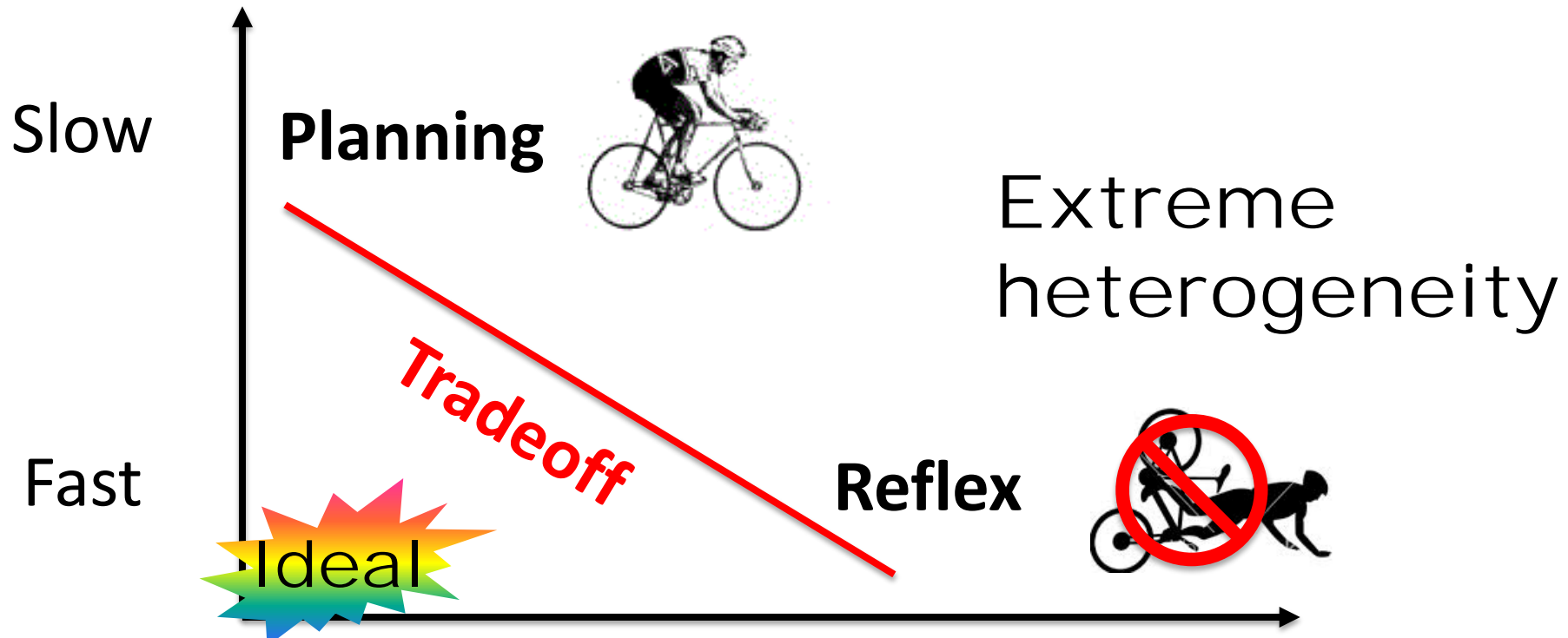
Trail
Vision

Accurate
Flexible
Centralized
Conscious
Deliberate
Stable virtual

Inaccurate
Rigid
Localized, distributed
Unconscious
Automatic
Unstable real dynamics

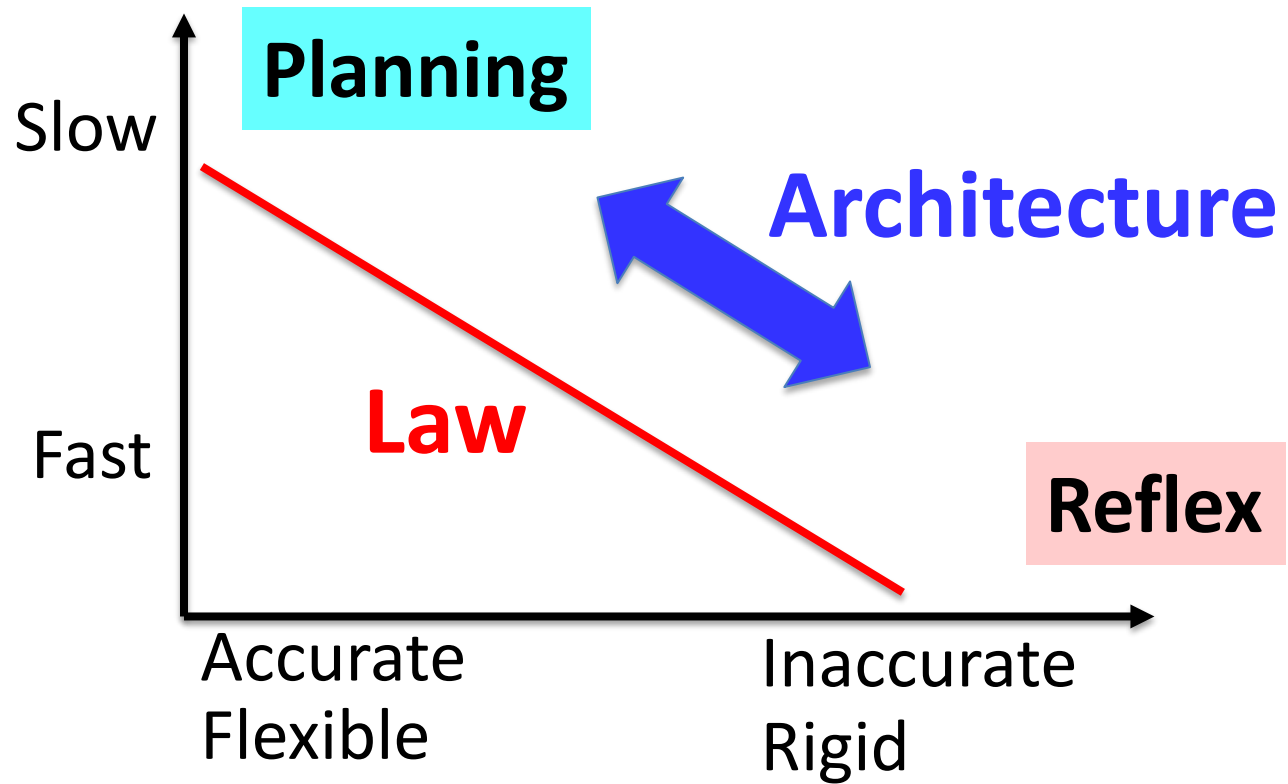
Layers





Accurate	Inaccurate
Flexible	Rigid
Centralized	Localized, distributed
Conscious	Unconscious
Deliberate	Automatic
Stable virtual	Unstable real dynamics

Layers



Universal laws
and
architectures

“constraints that
deconstrain”

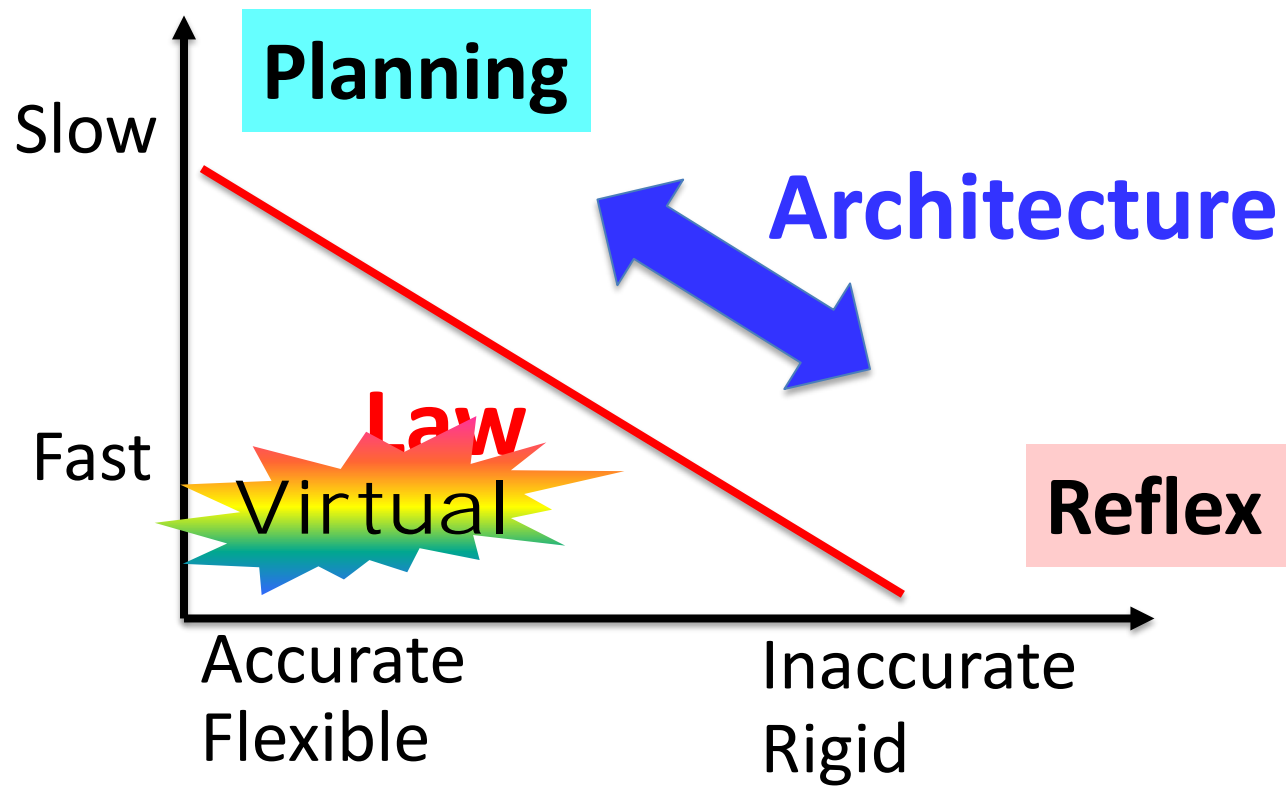
Gerhart &
Kirschner

Laws:

constrains the possible

Architectures:

deconstrains the lawful



Universal laws
and
virtual
architectures

Laws:

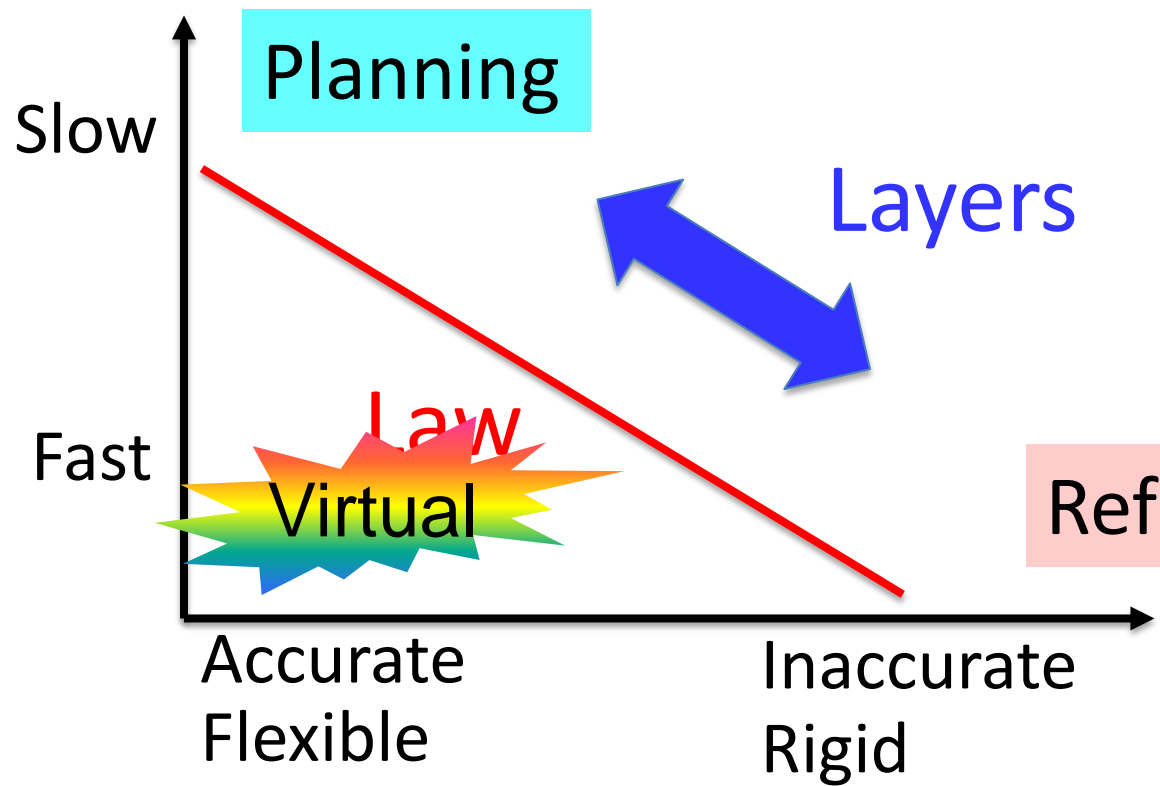
Architectures:

Virtualization:

constrains the possible

deconstrains the lawful

create sweet spot



Universal laws
and
virtual
architectures

Levels
+
Layers

Laws:	constrains the possible
Architectures:	deconstrains the lawful
Virtualization:	create sweet spot

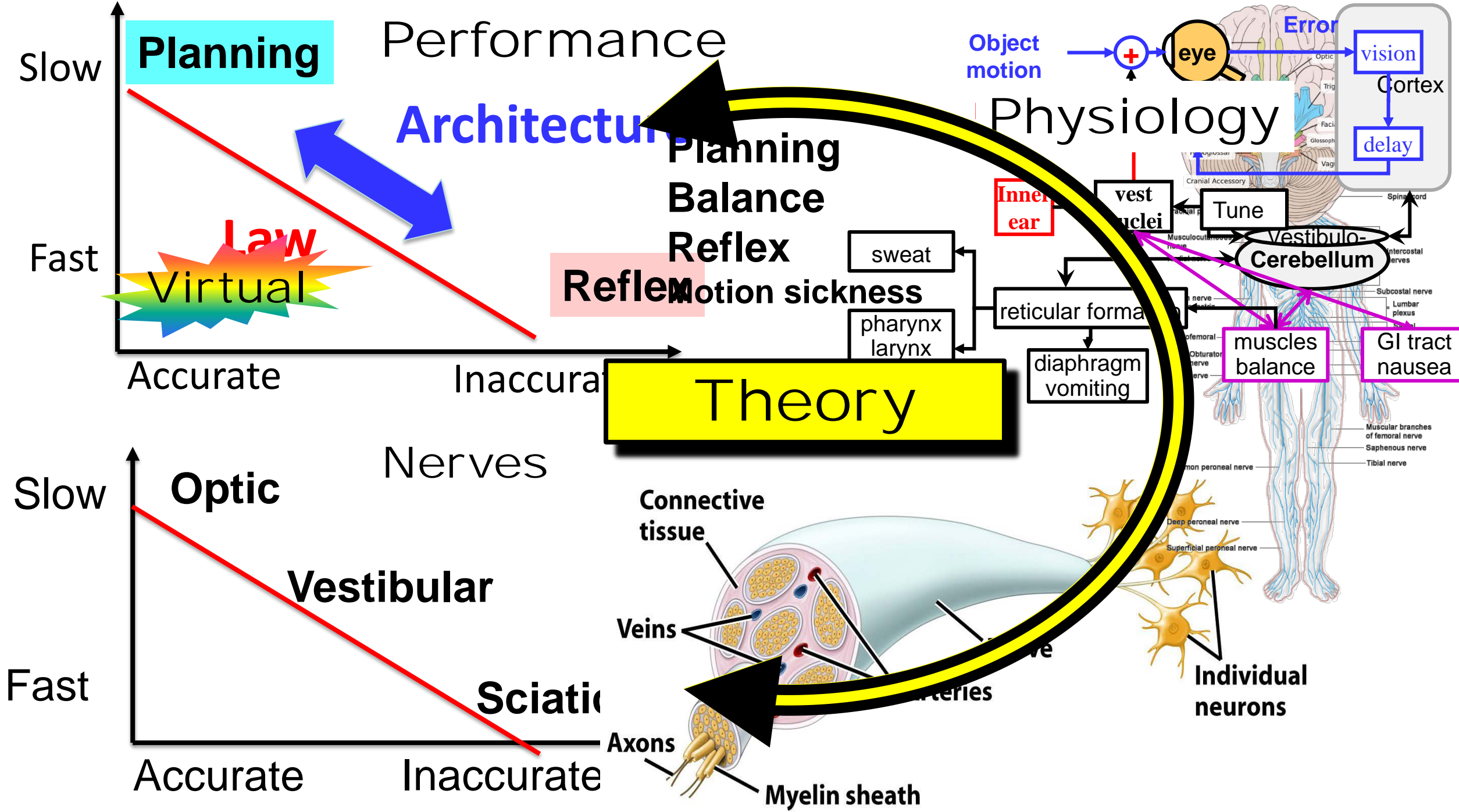
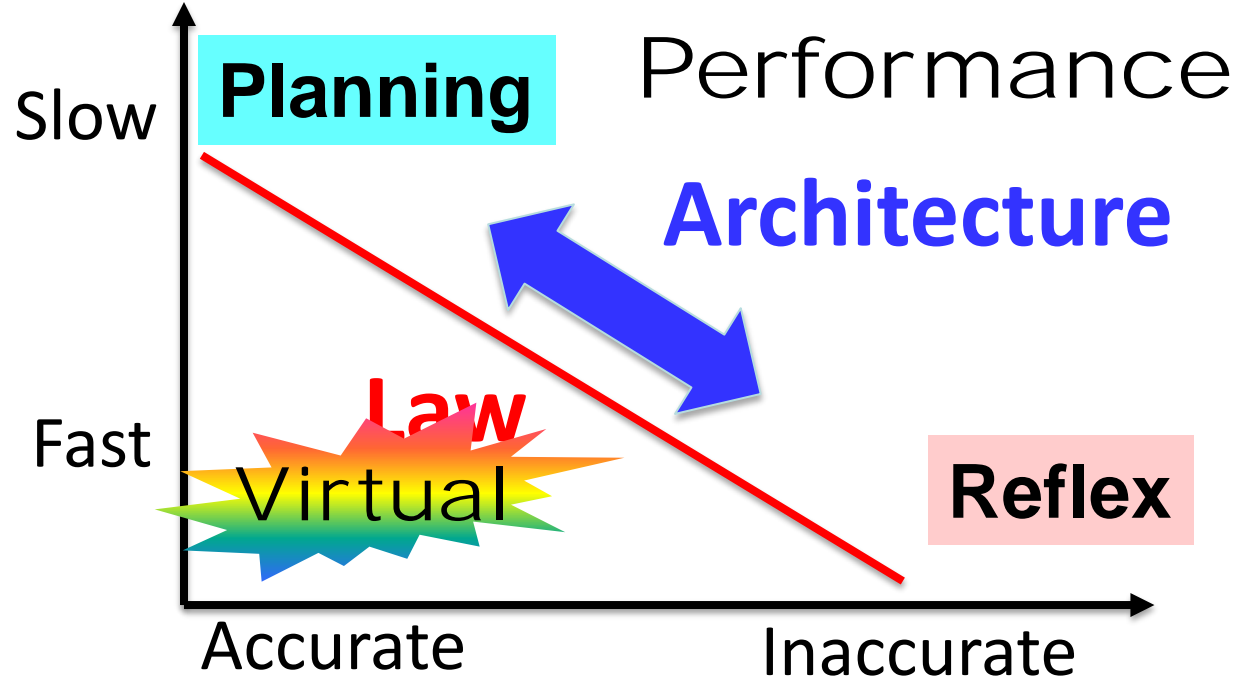
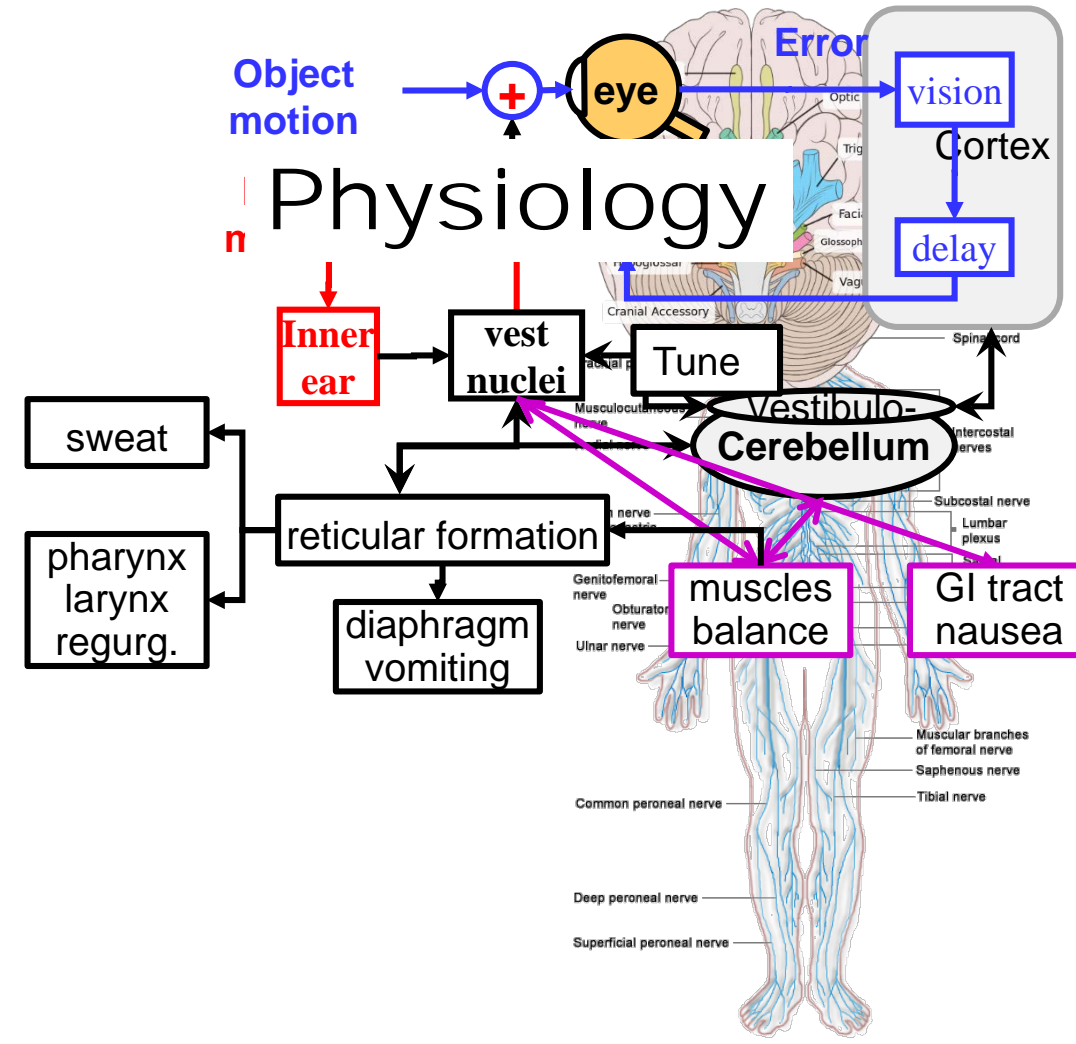
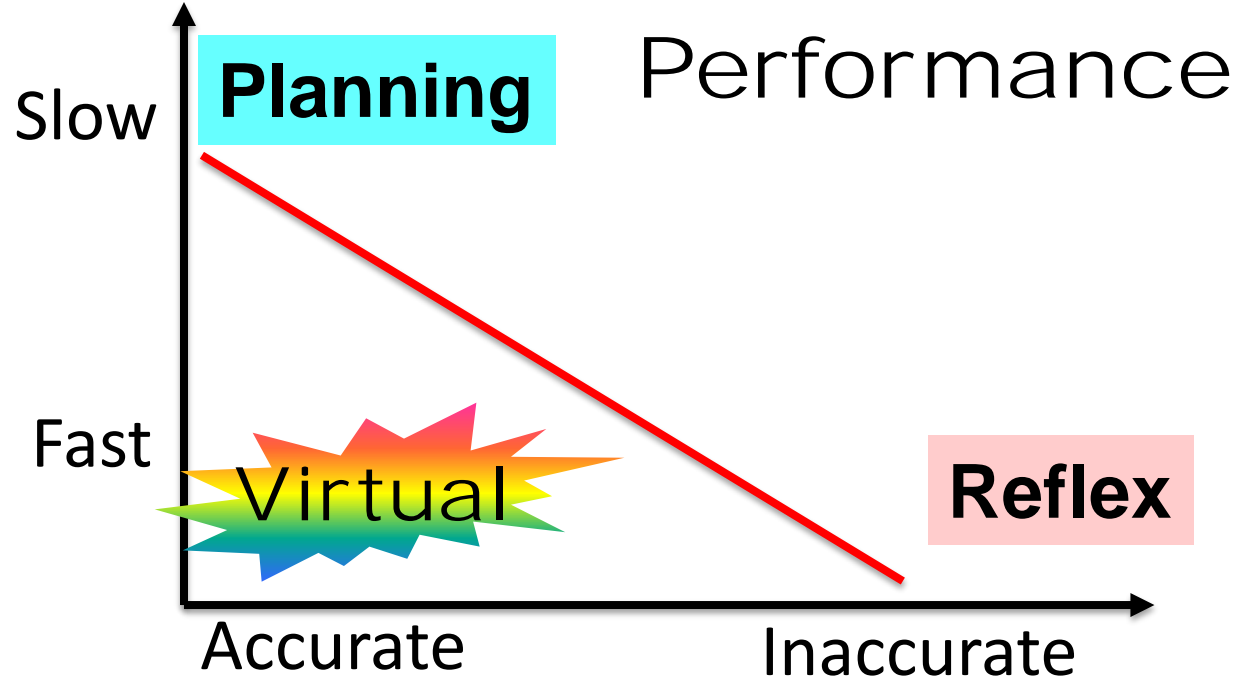


Figure 20-11. Diagram illustrating the relationship between performance, accuracy, speed, and theory in a biological context.

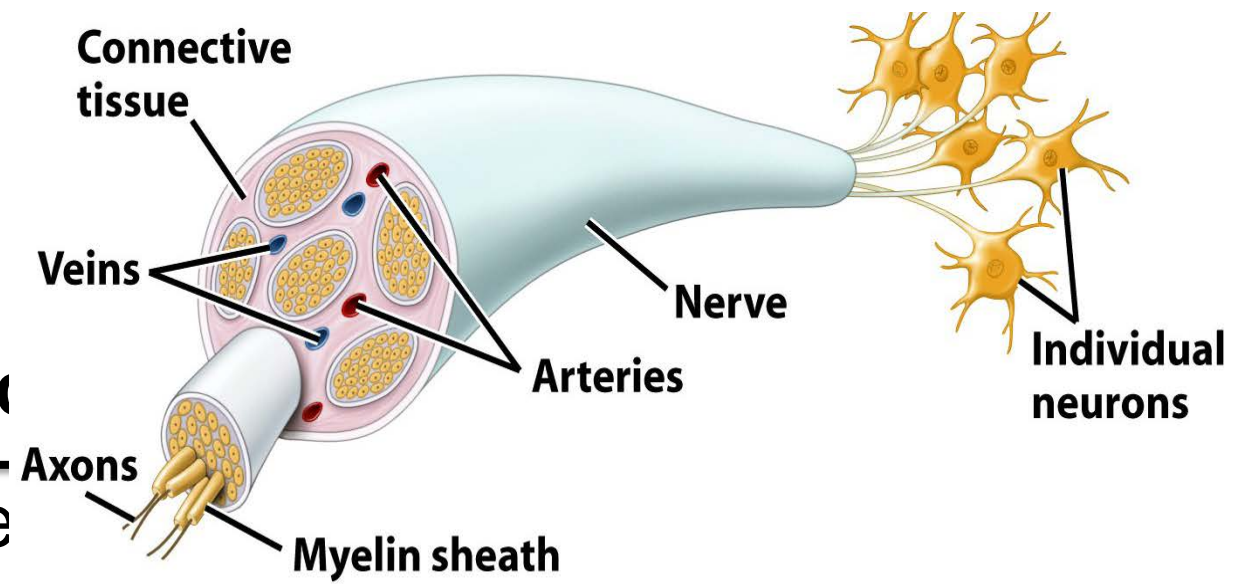
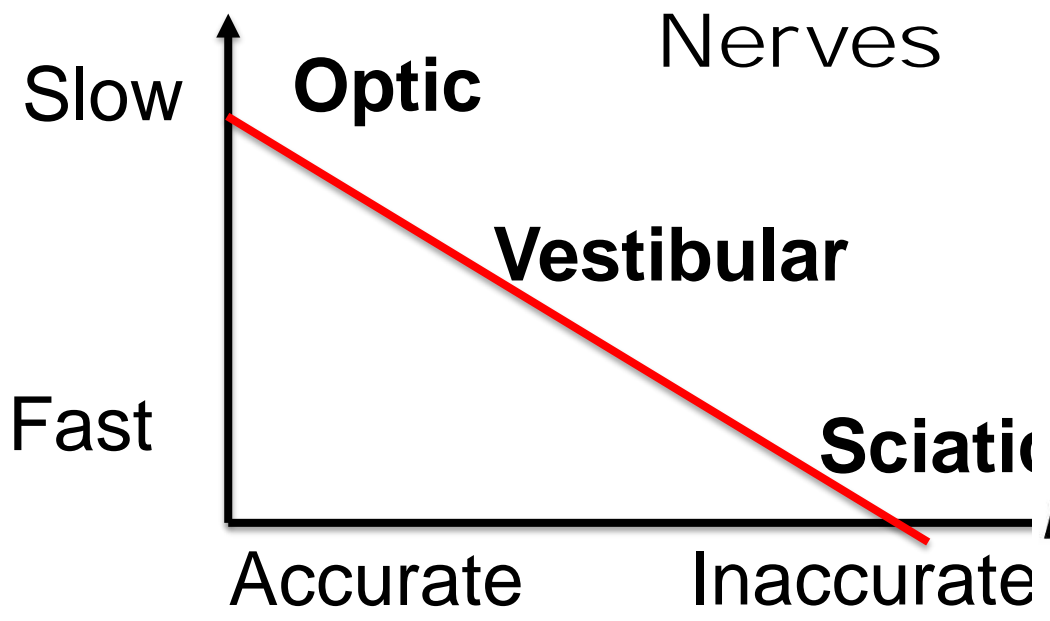


Layers





Levels



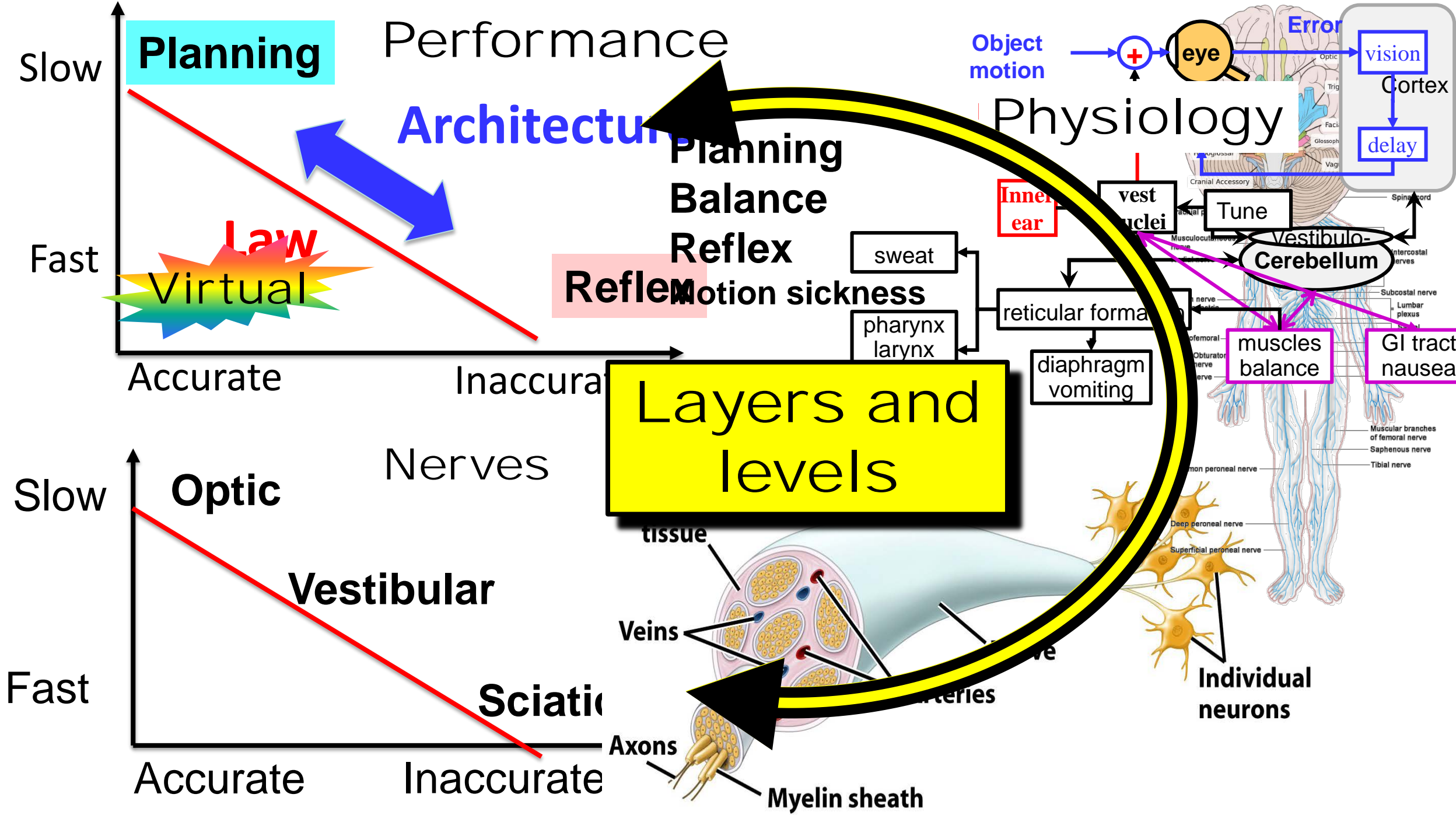
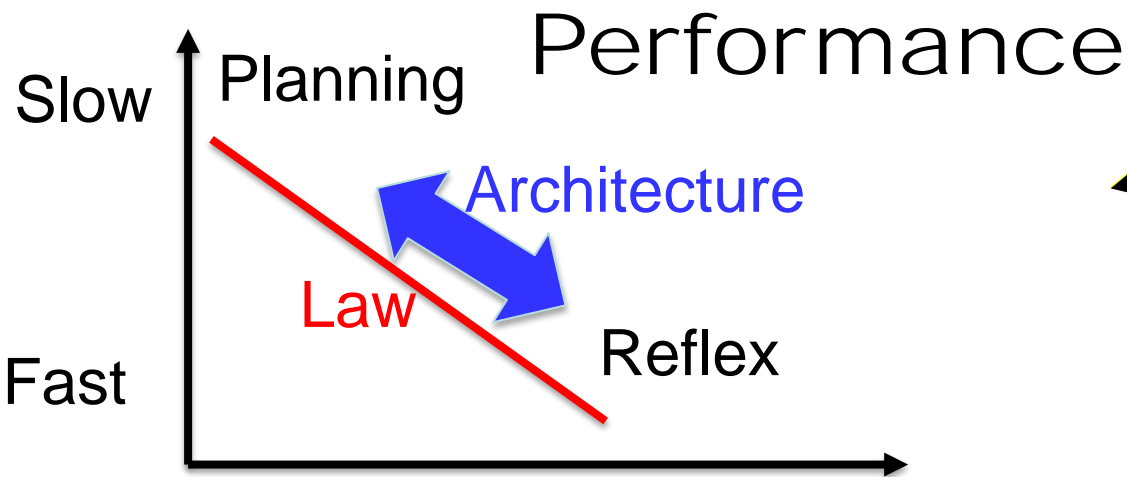
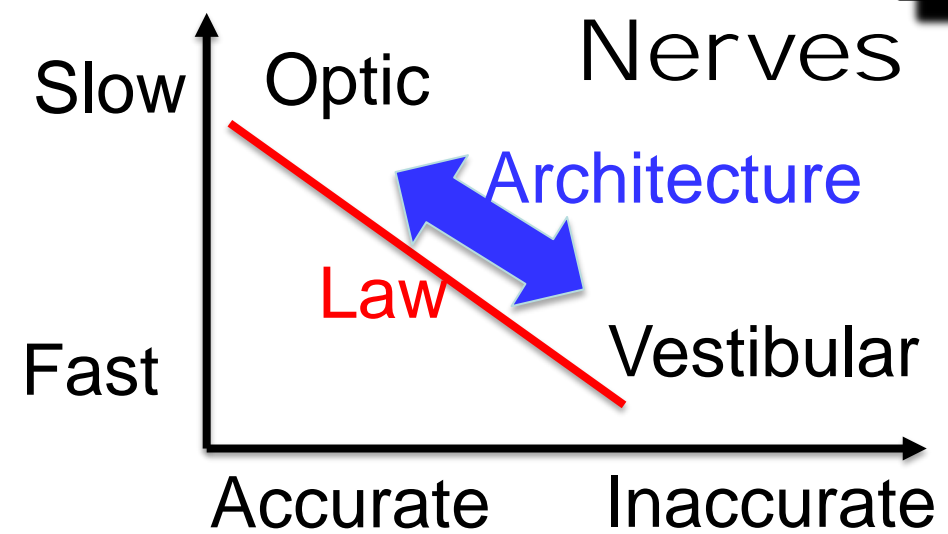


Figure 20.14: Diagram illustrating the relationship between performance, speed, accuracy, and biological layers.

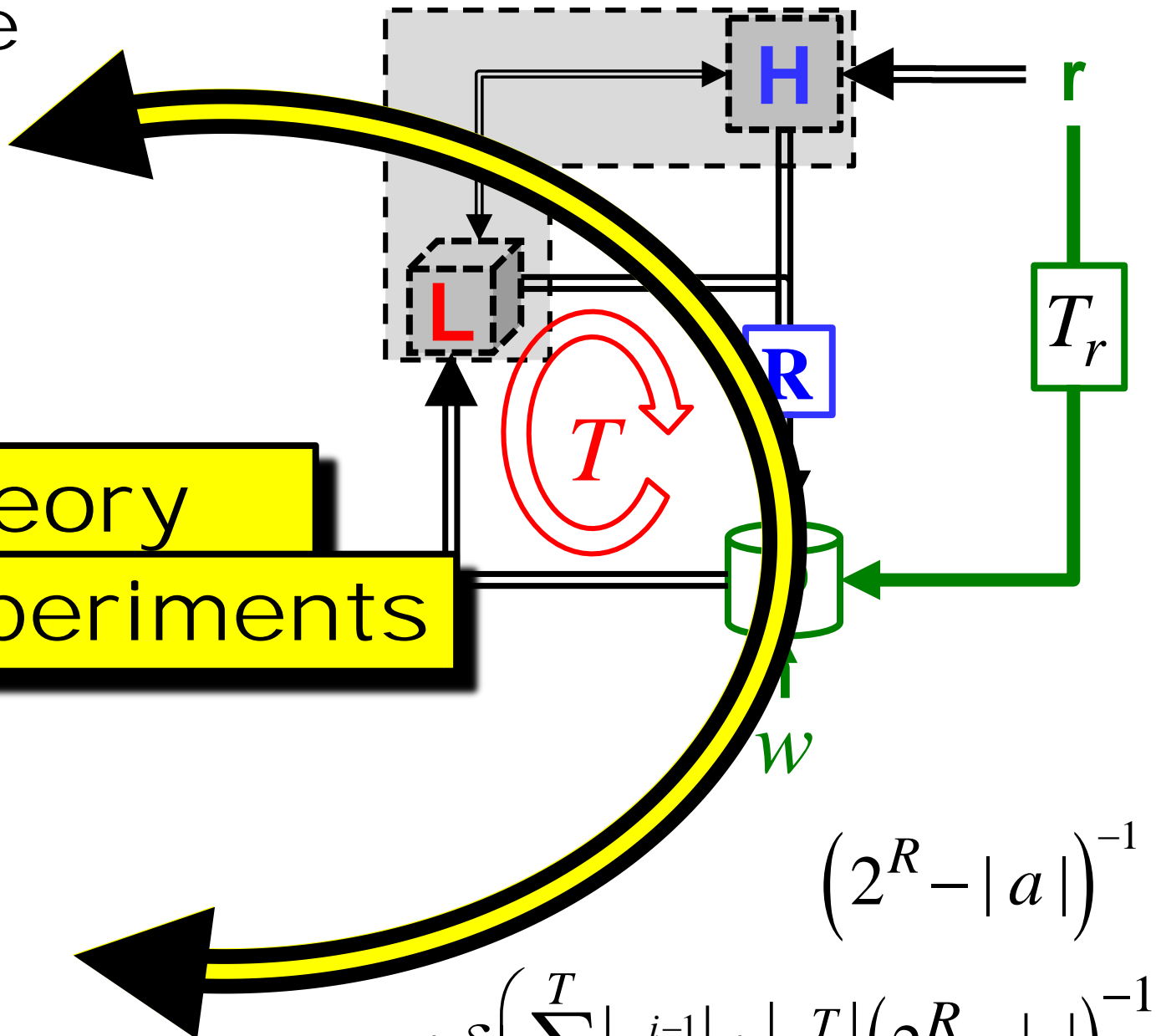


Accurate Flexible Inaccurate Rigid

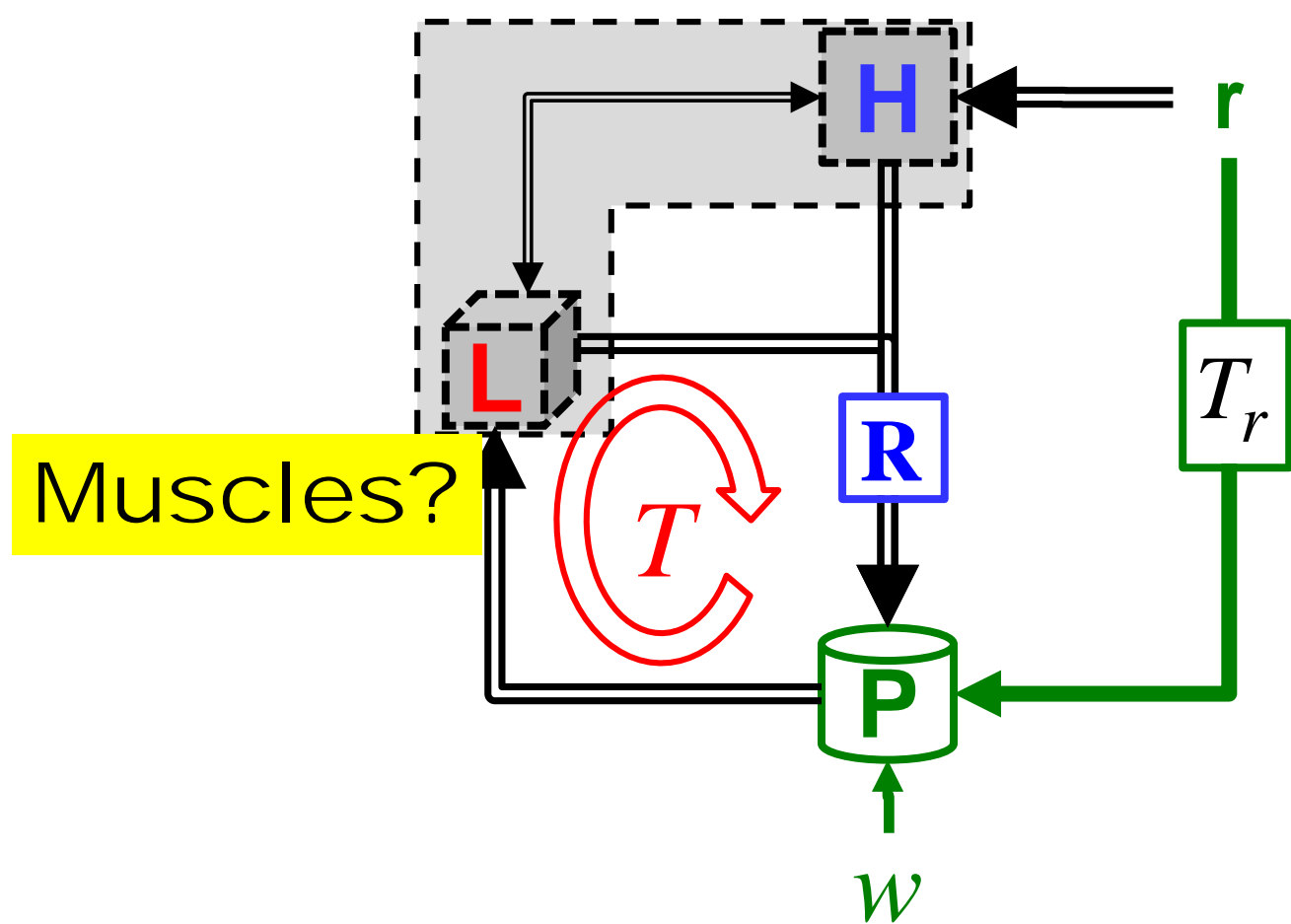
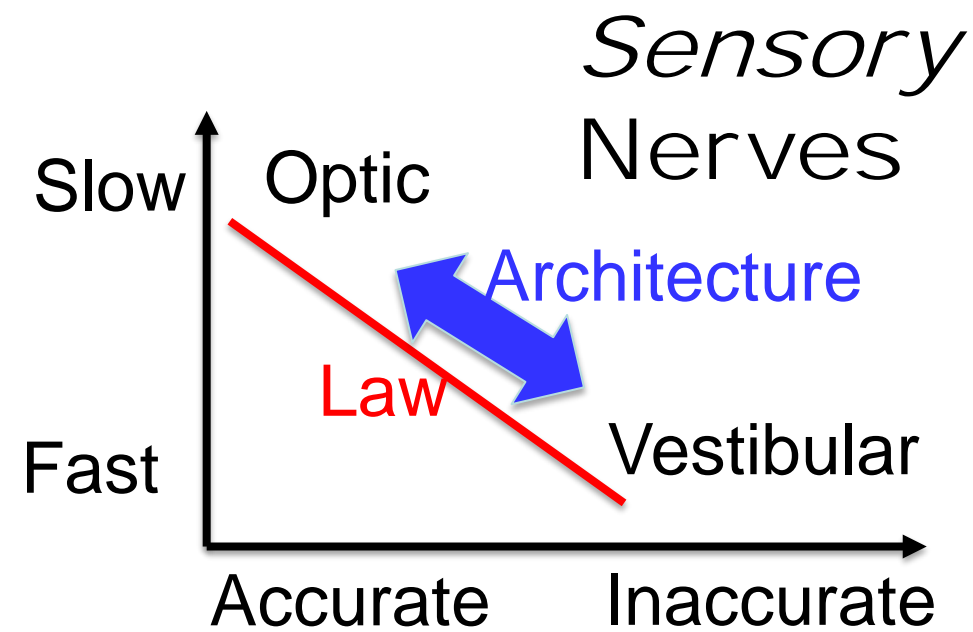
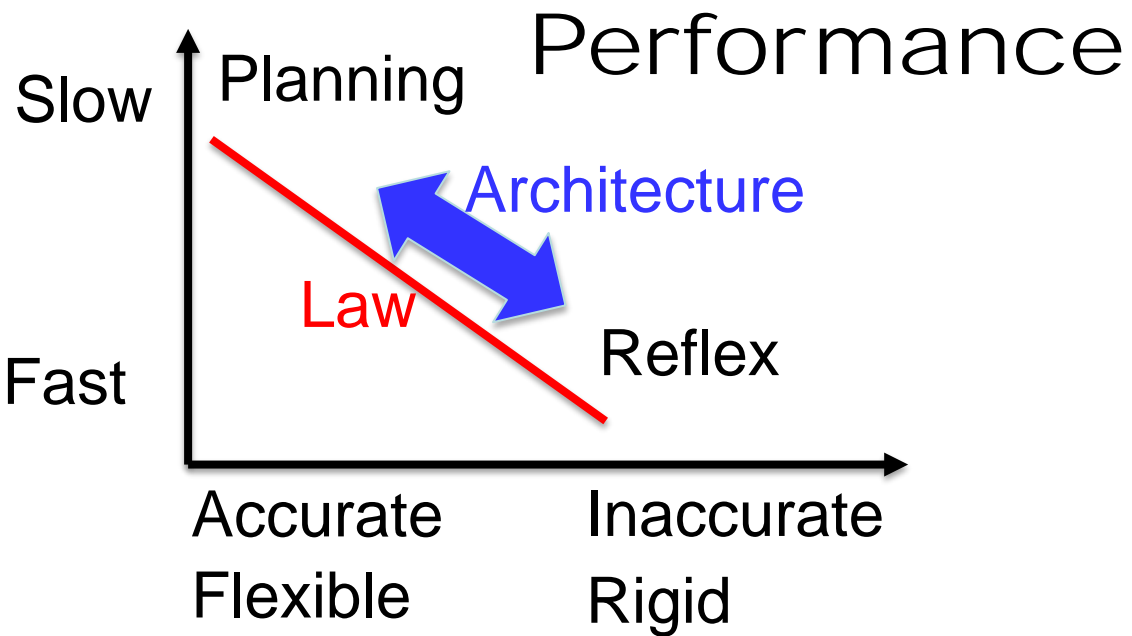


Accurate Inaccurate

Theory
Experiments

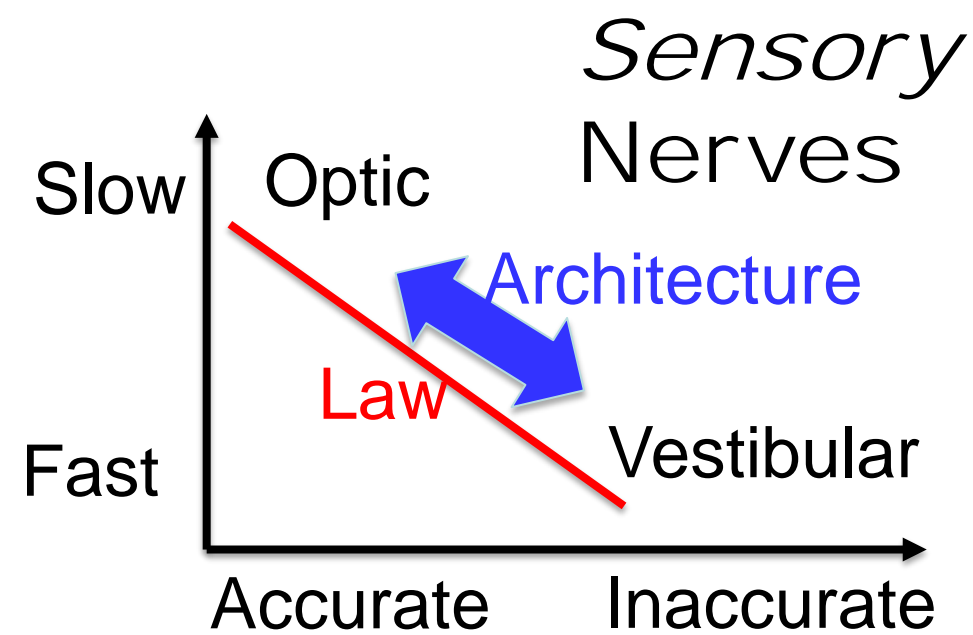
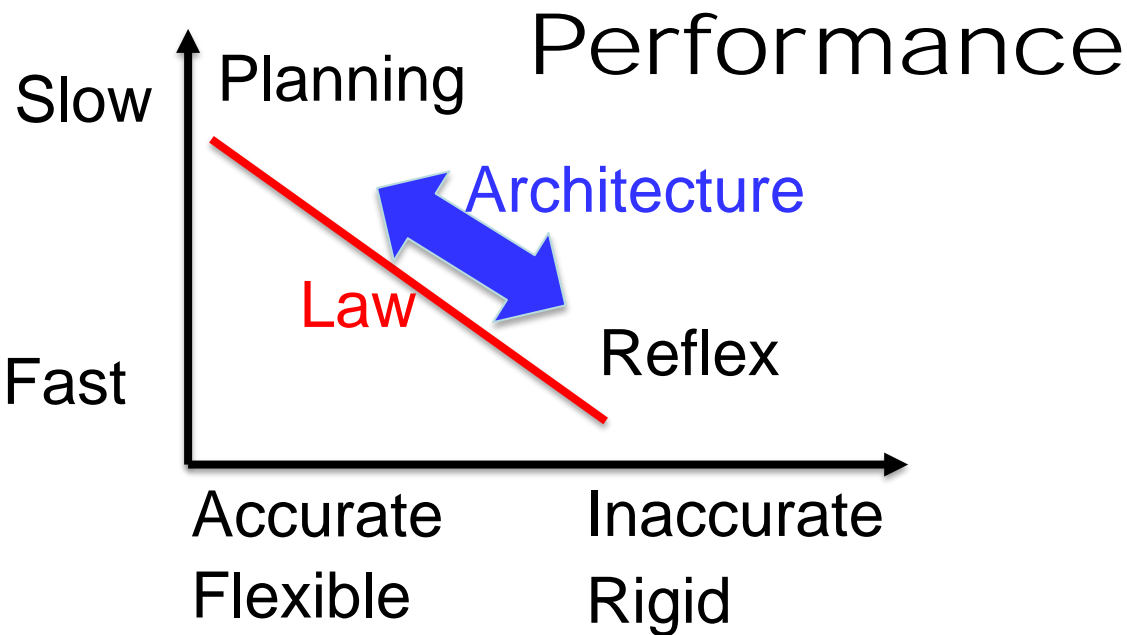


$$+ \delta \left(\sum_{i=1}^T |a^{i-1}| + |a^T| \left(2^R - |a| \right)^{-1} \right)$$

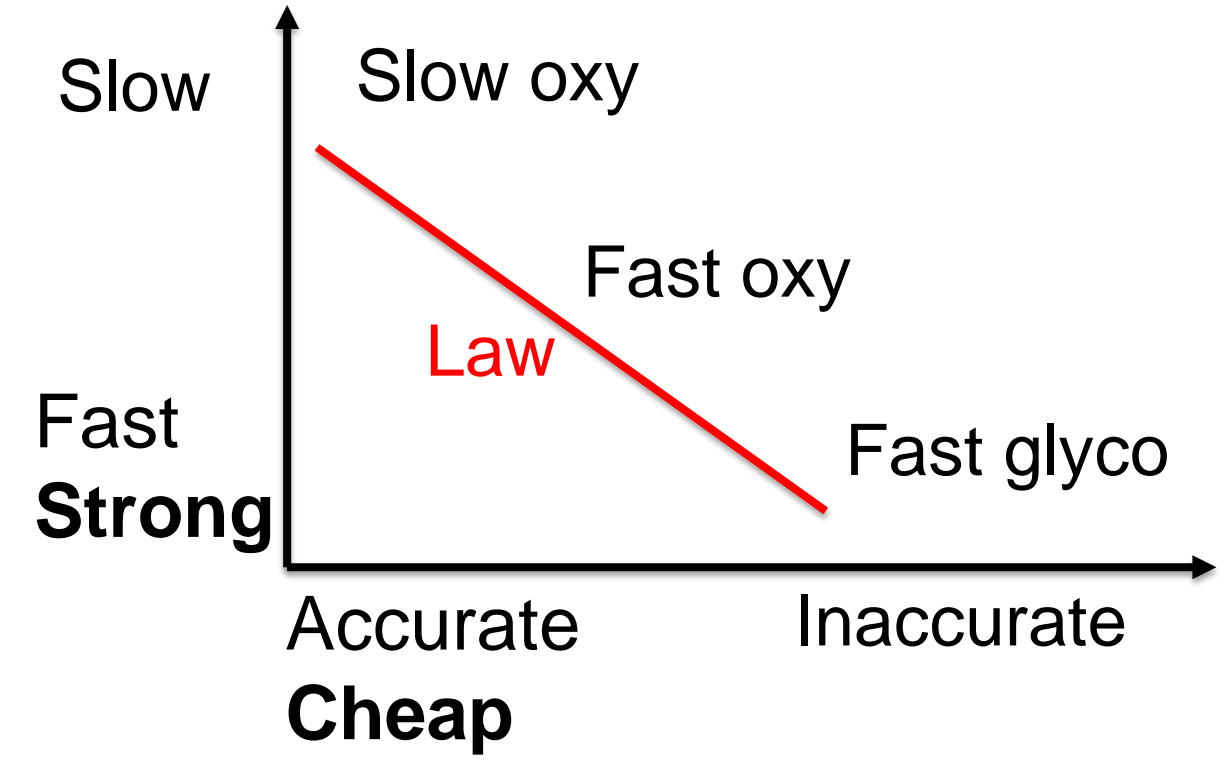


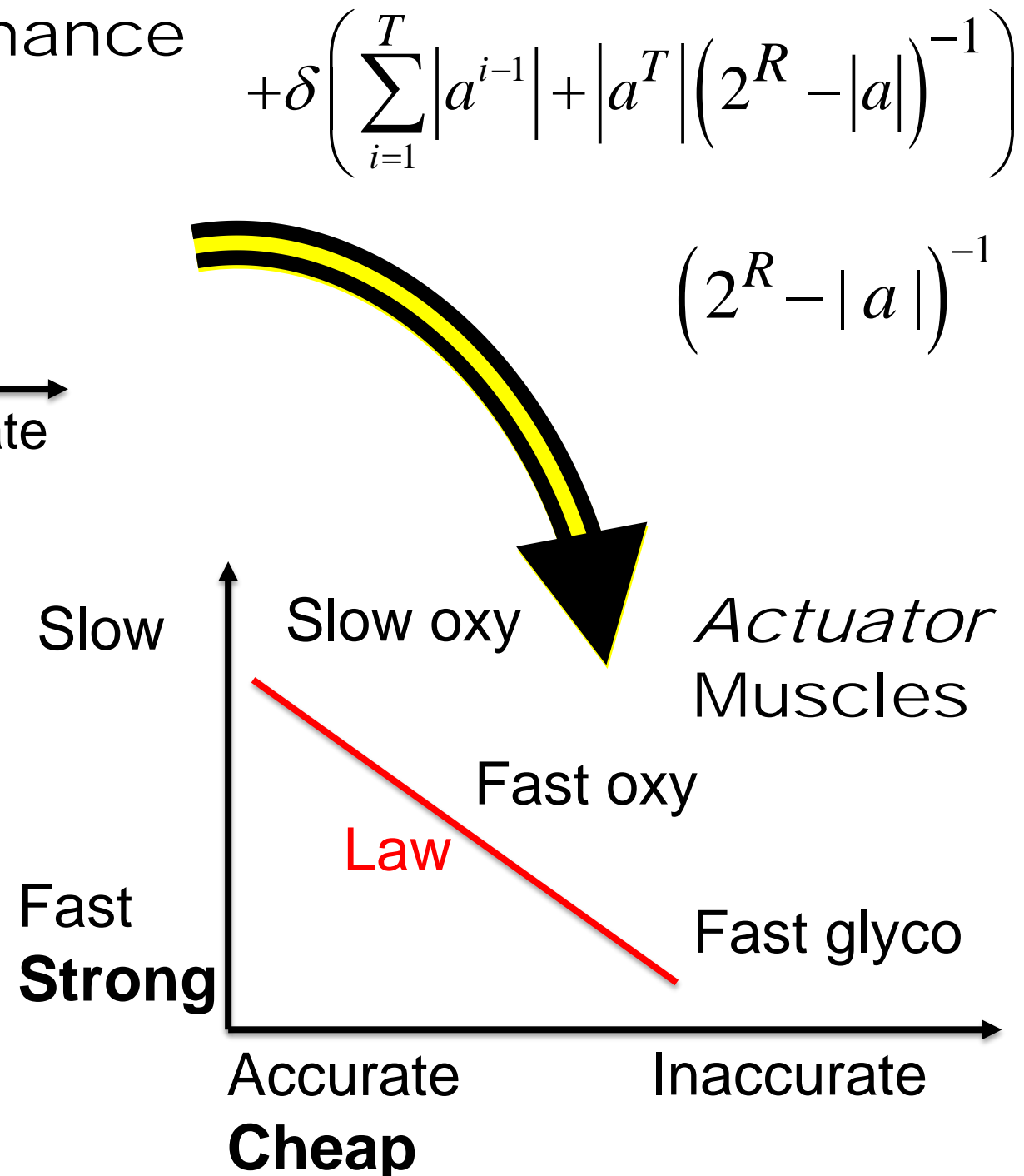
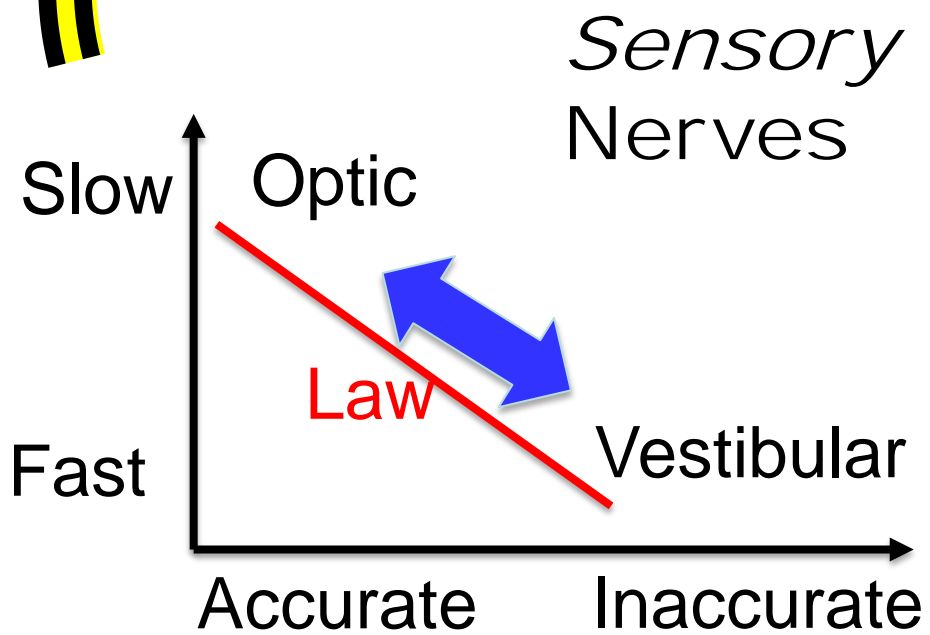
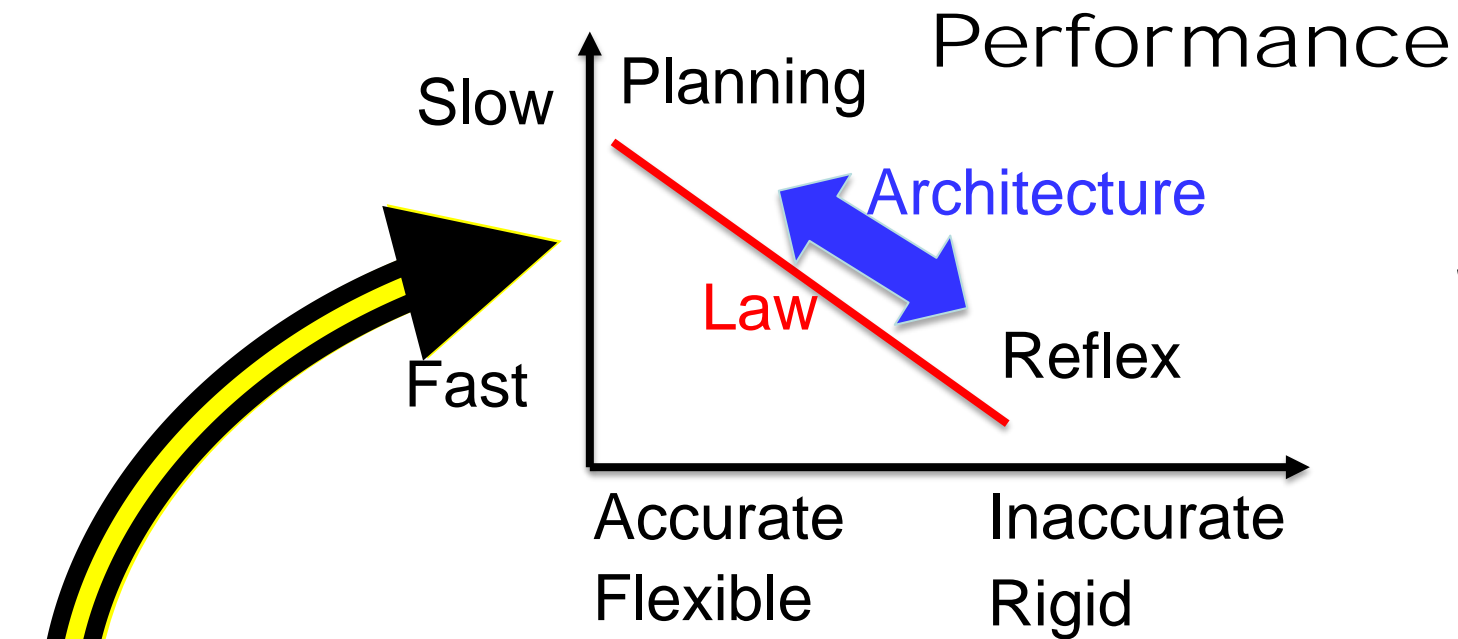
$$\left(2^R - |a|\right)^{-1}$$

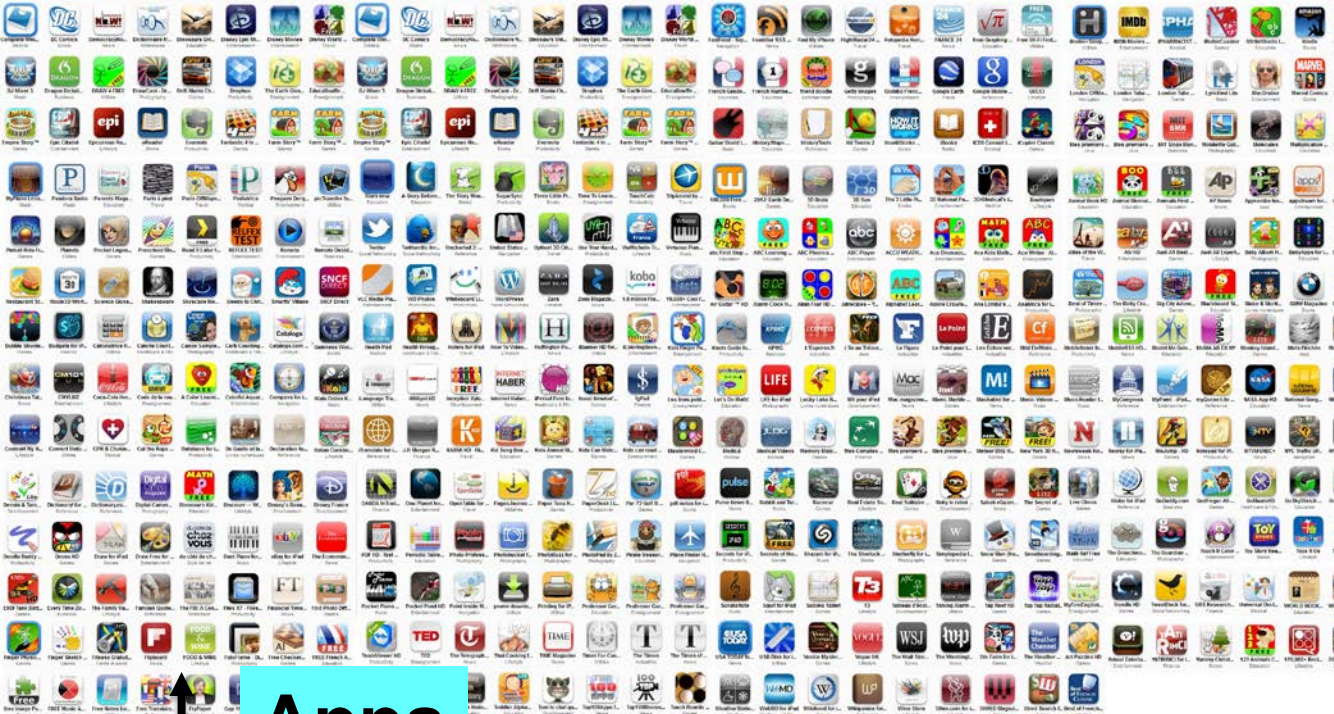
$$+ \delta \left(\sum_{i=1}^T |a^{i-1}| + |a^T| \left(2^R - |a|\right)^{-1} \right)$$



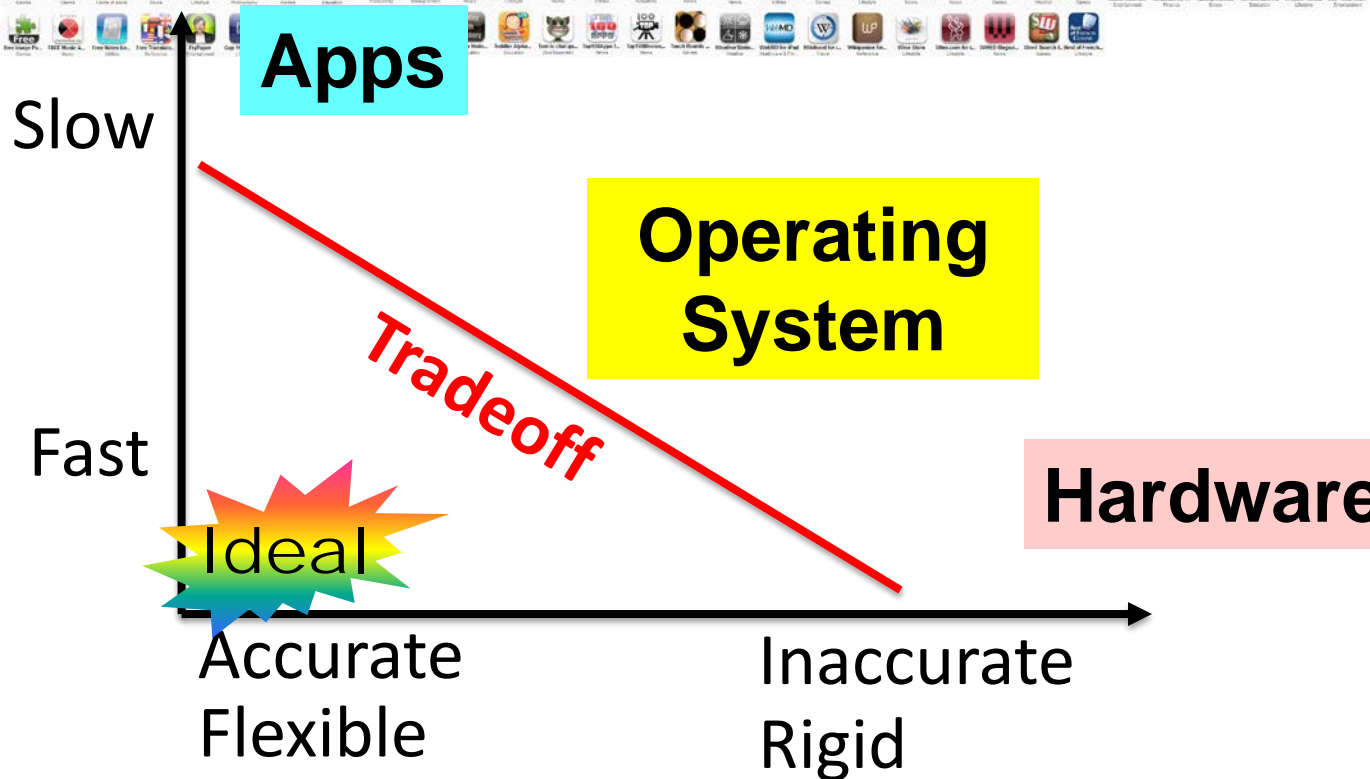
Muscles?



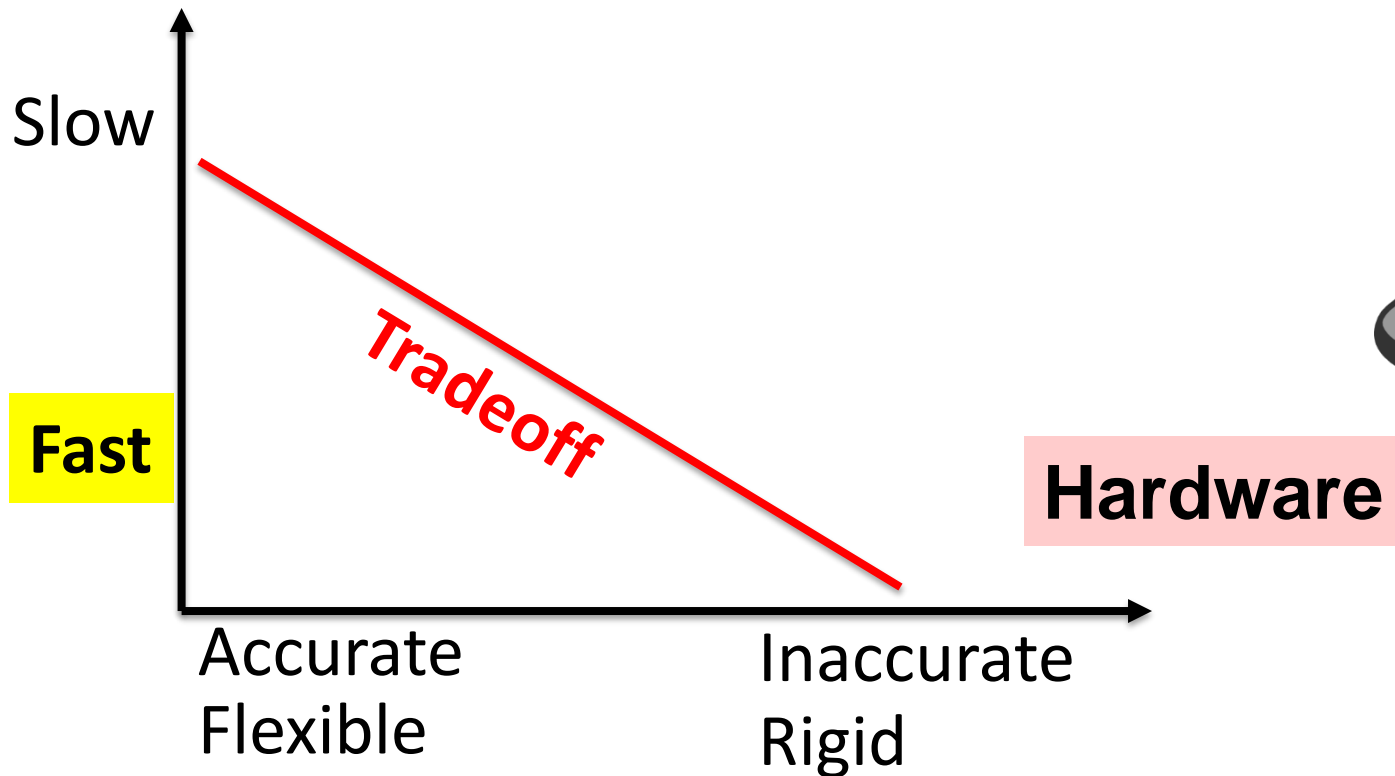


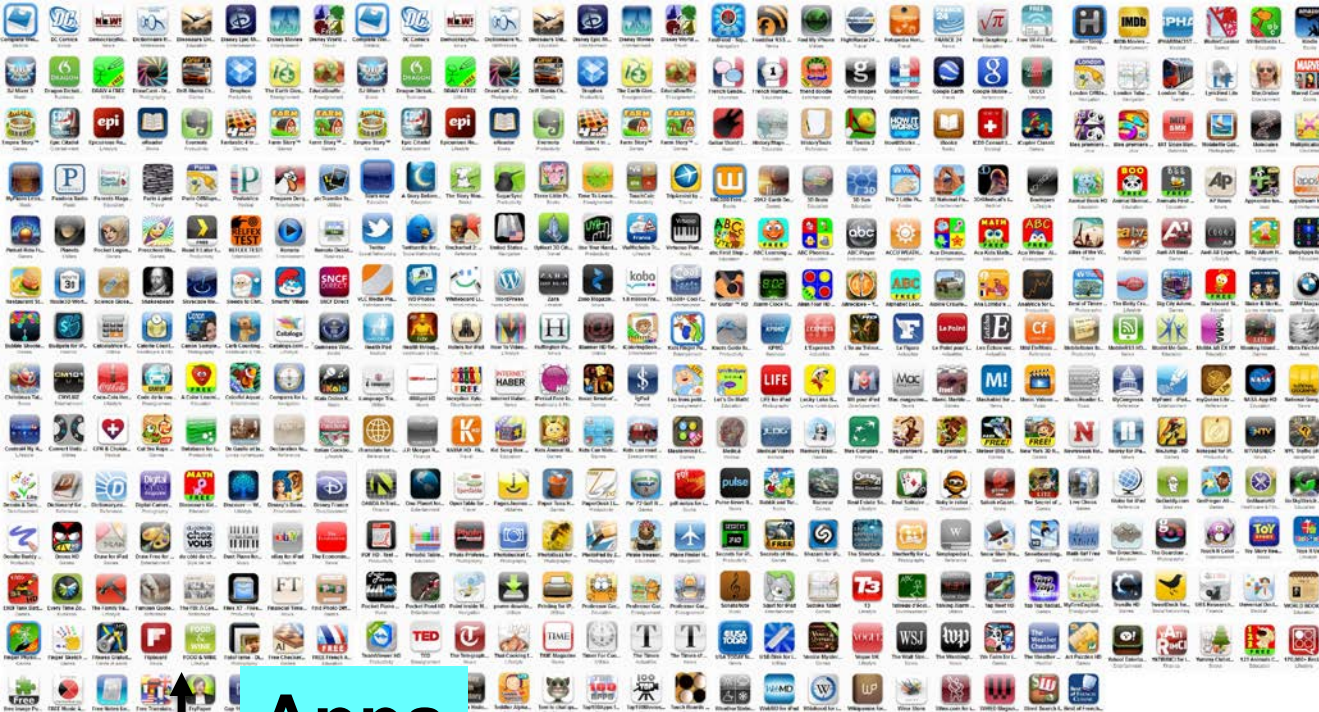


Layered architecture

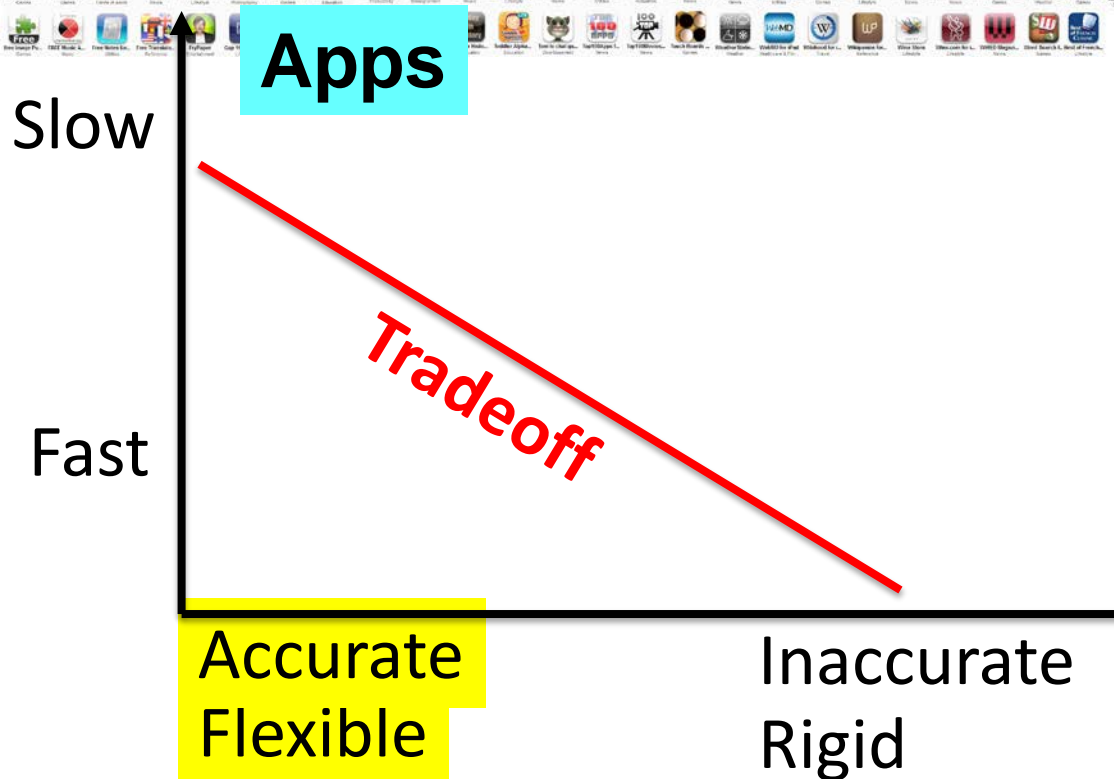


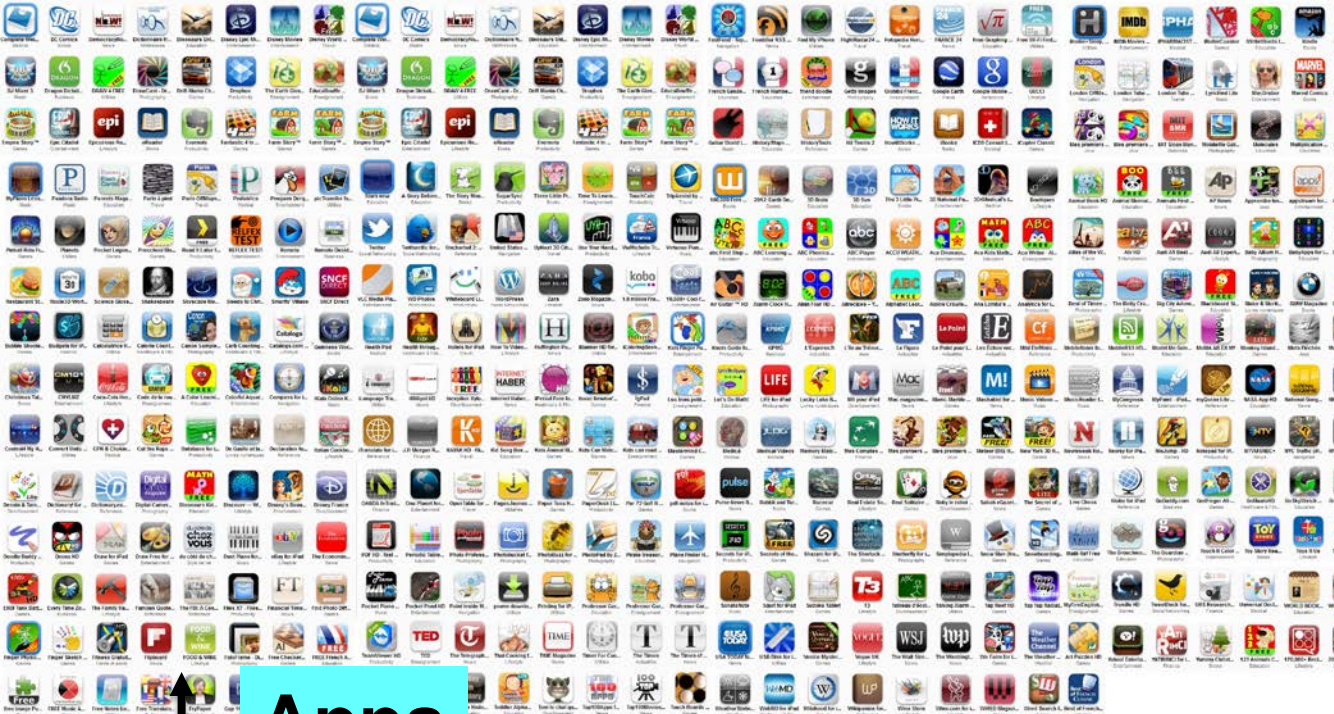
Layered architecture



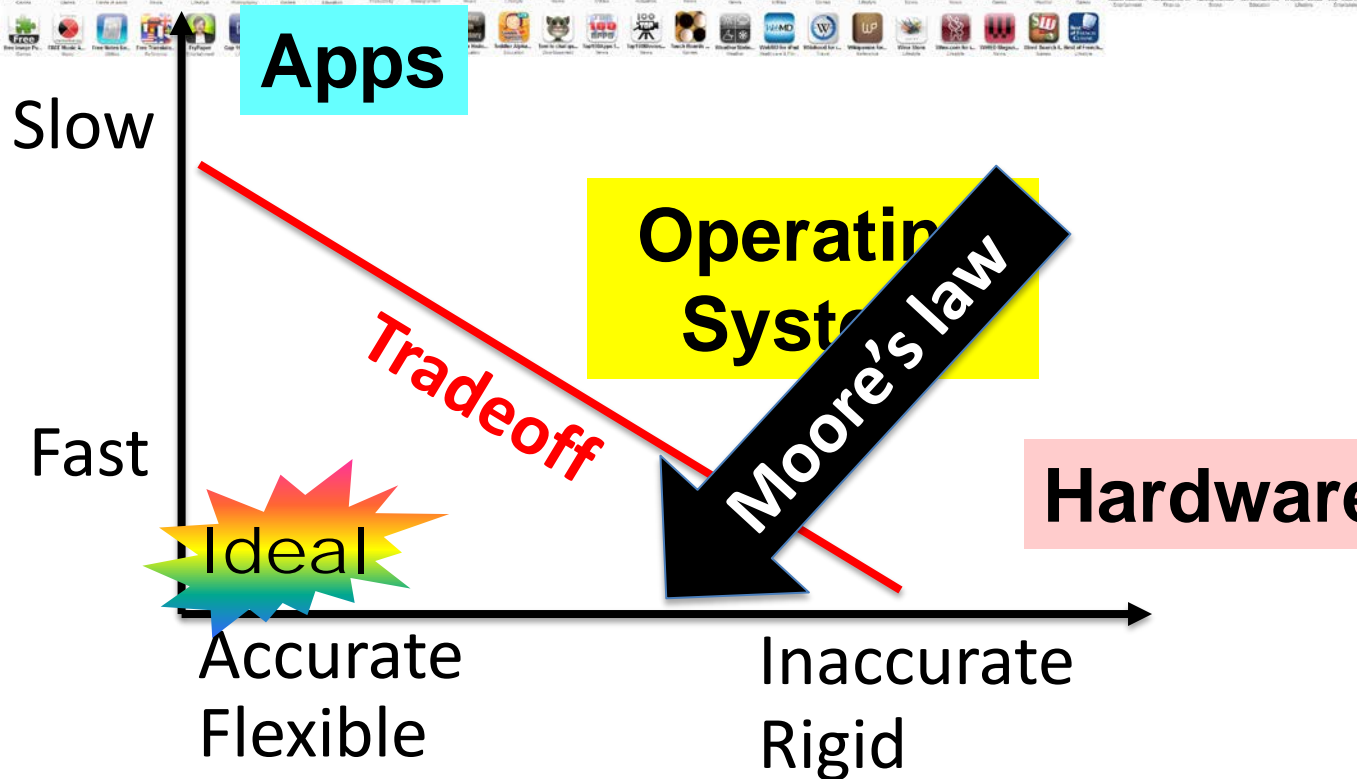


Layered architecture



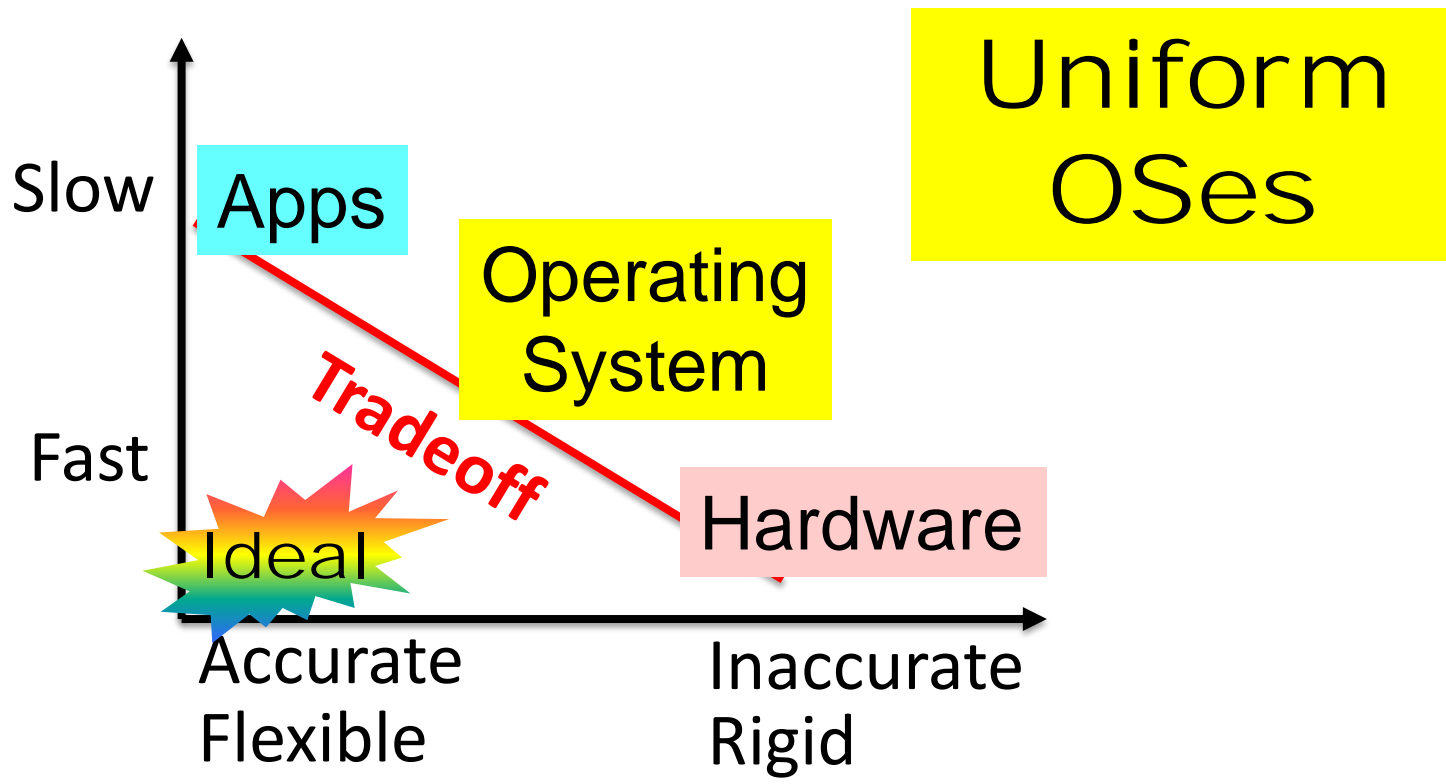


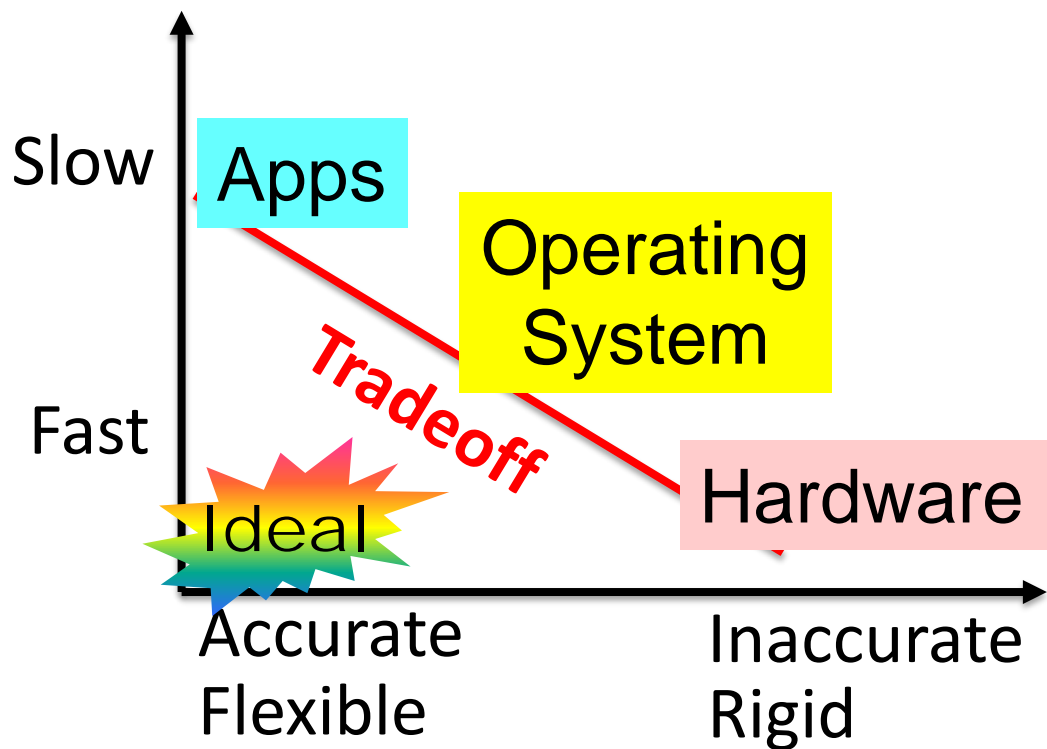
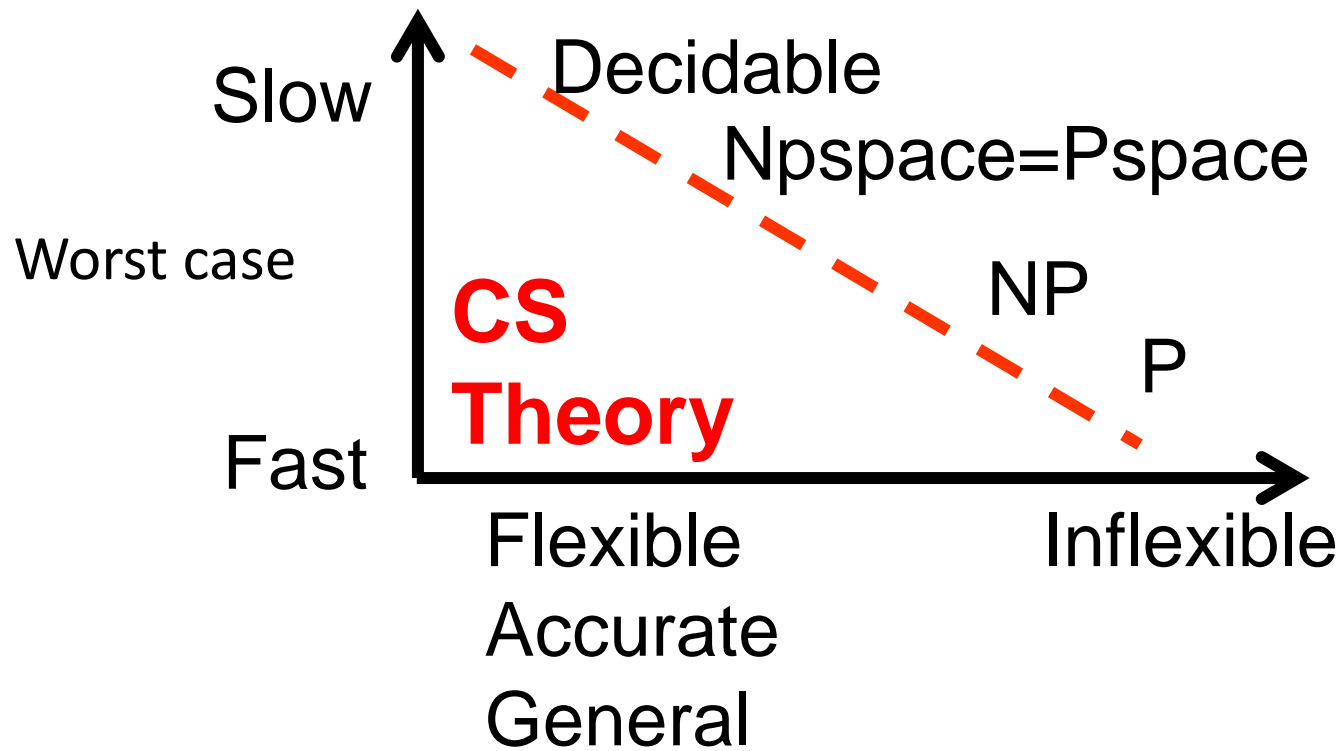
Layered architecture

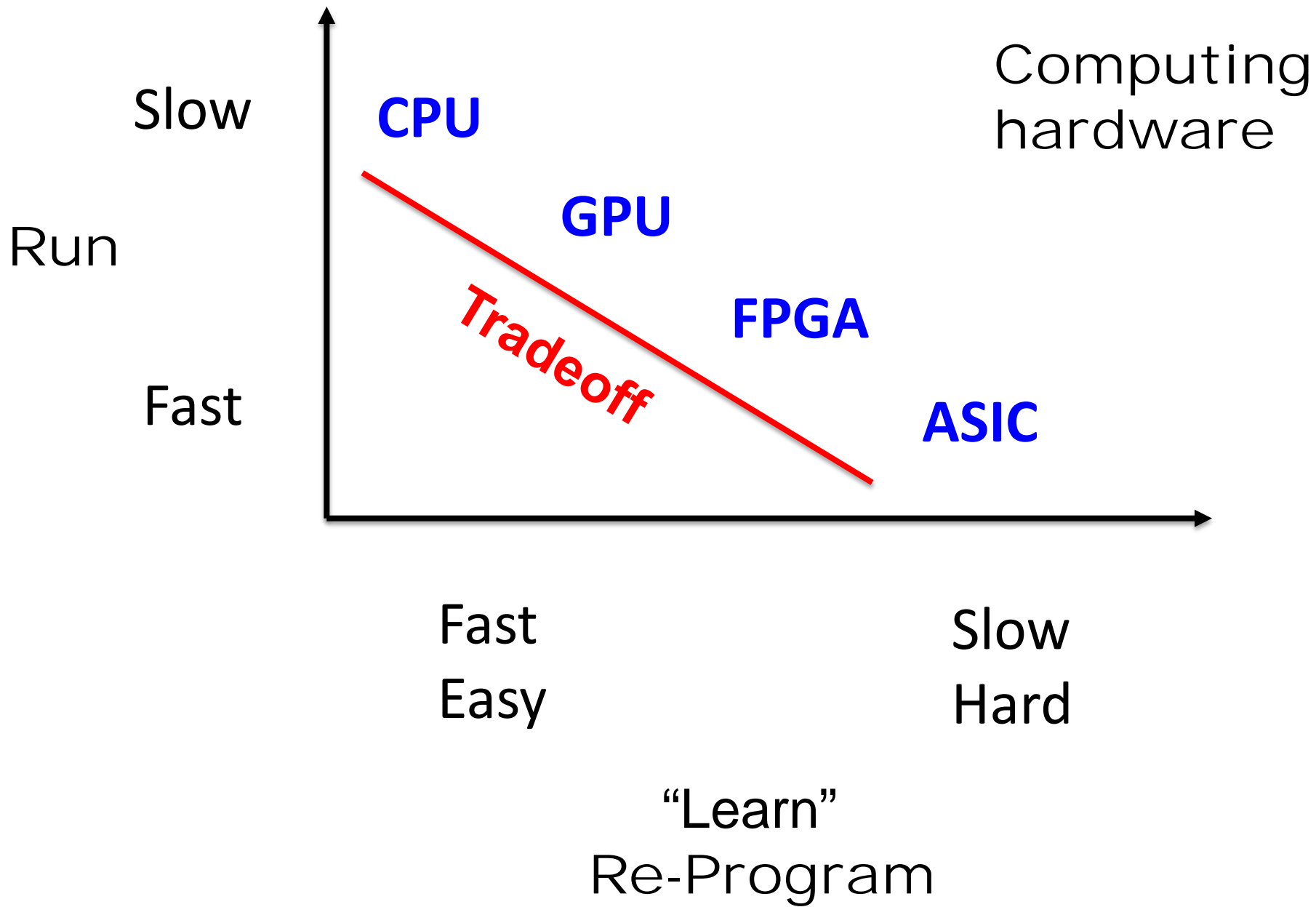


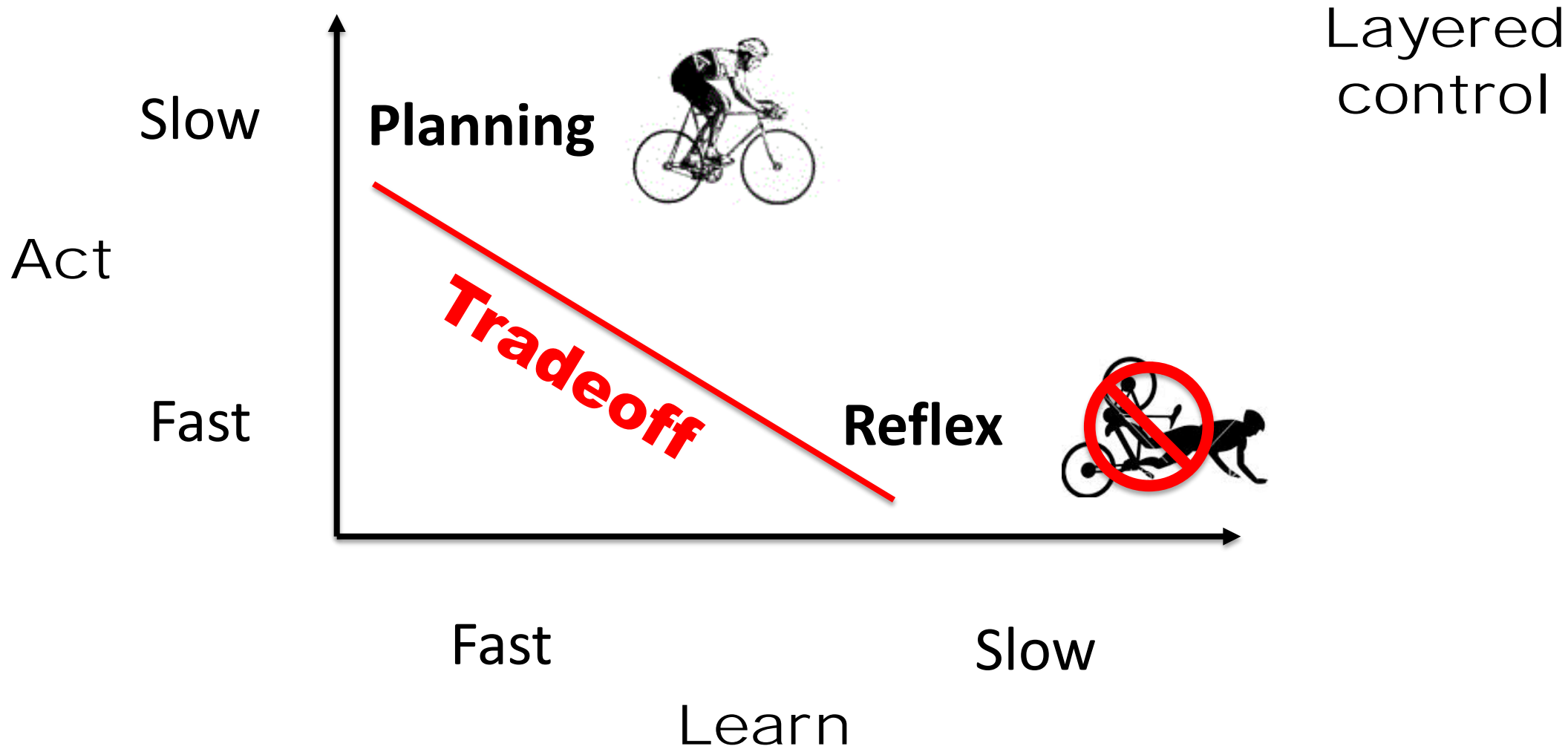


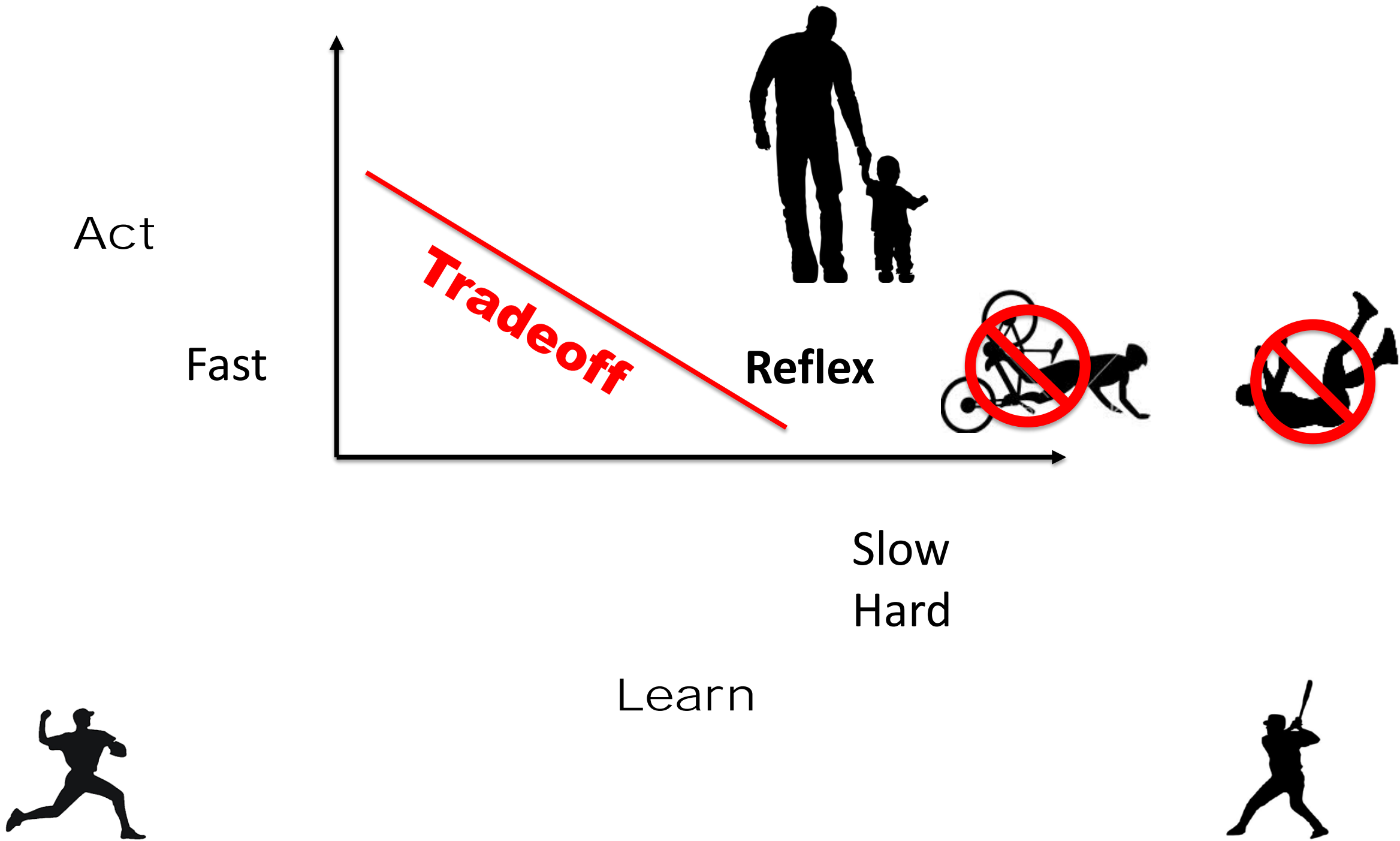
Constraints that deconstrain







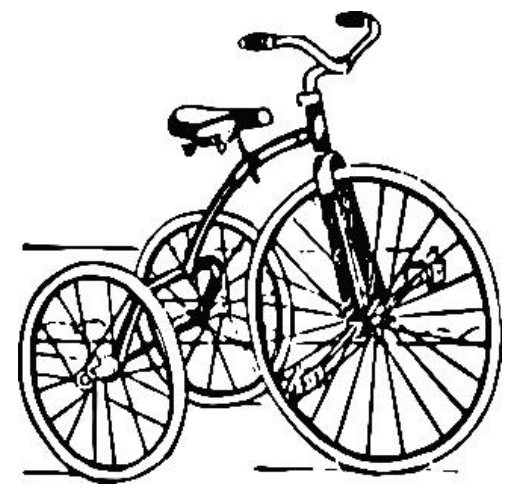




Slow
Act

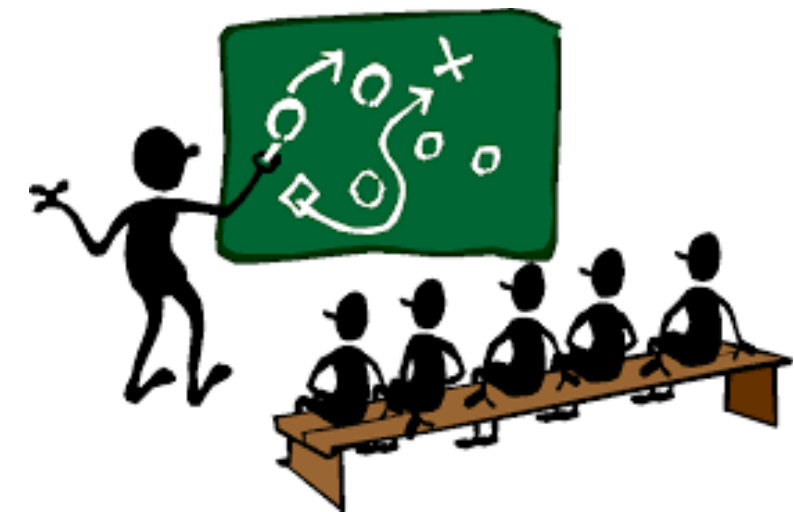
Planning

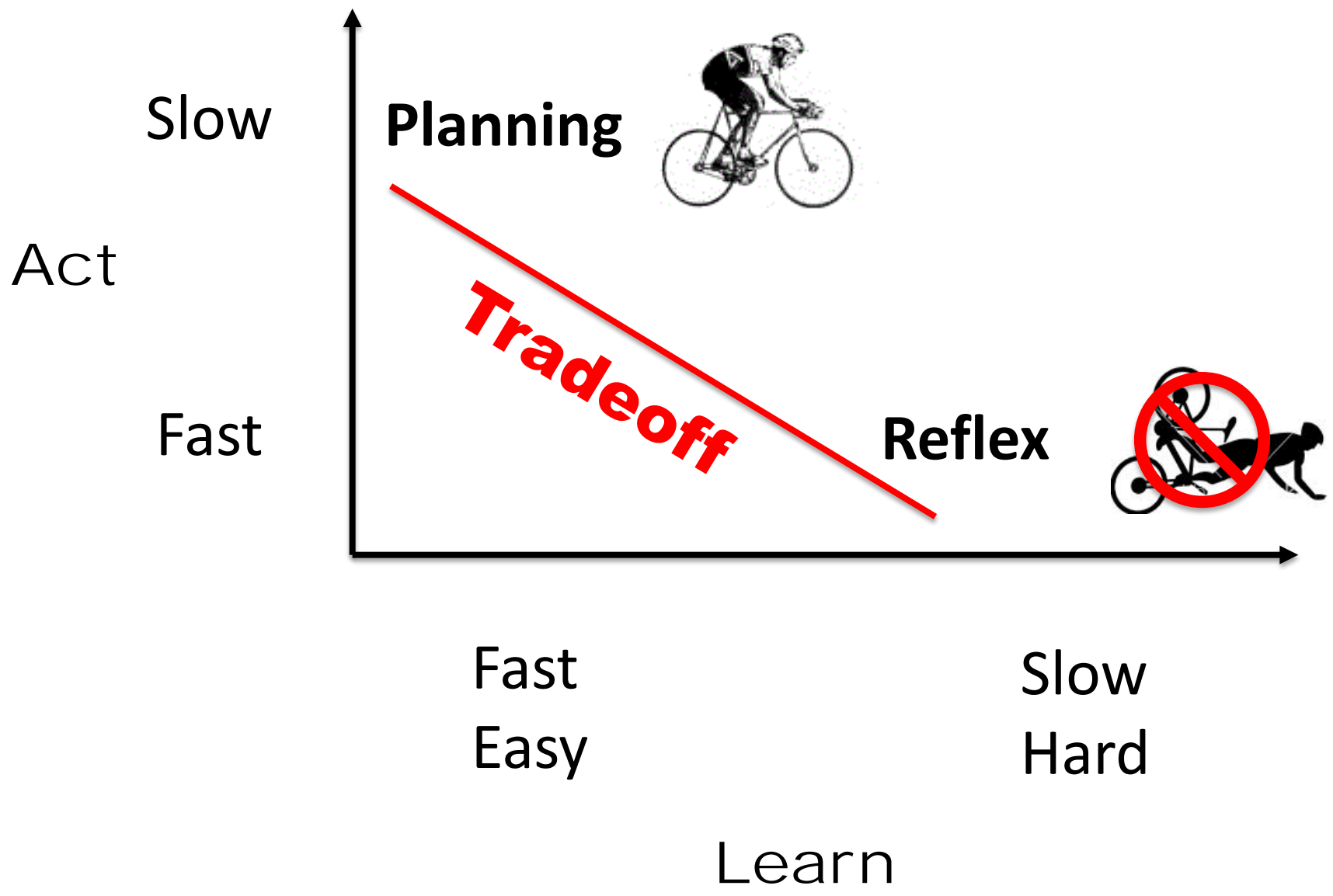
Tradeoff

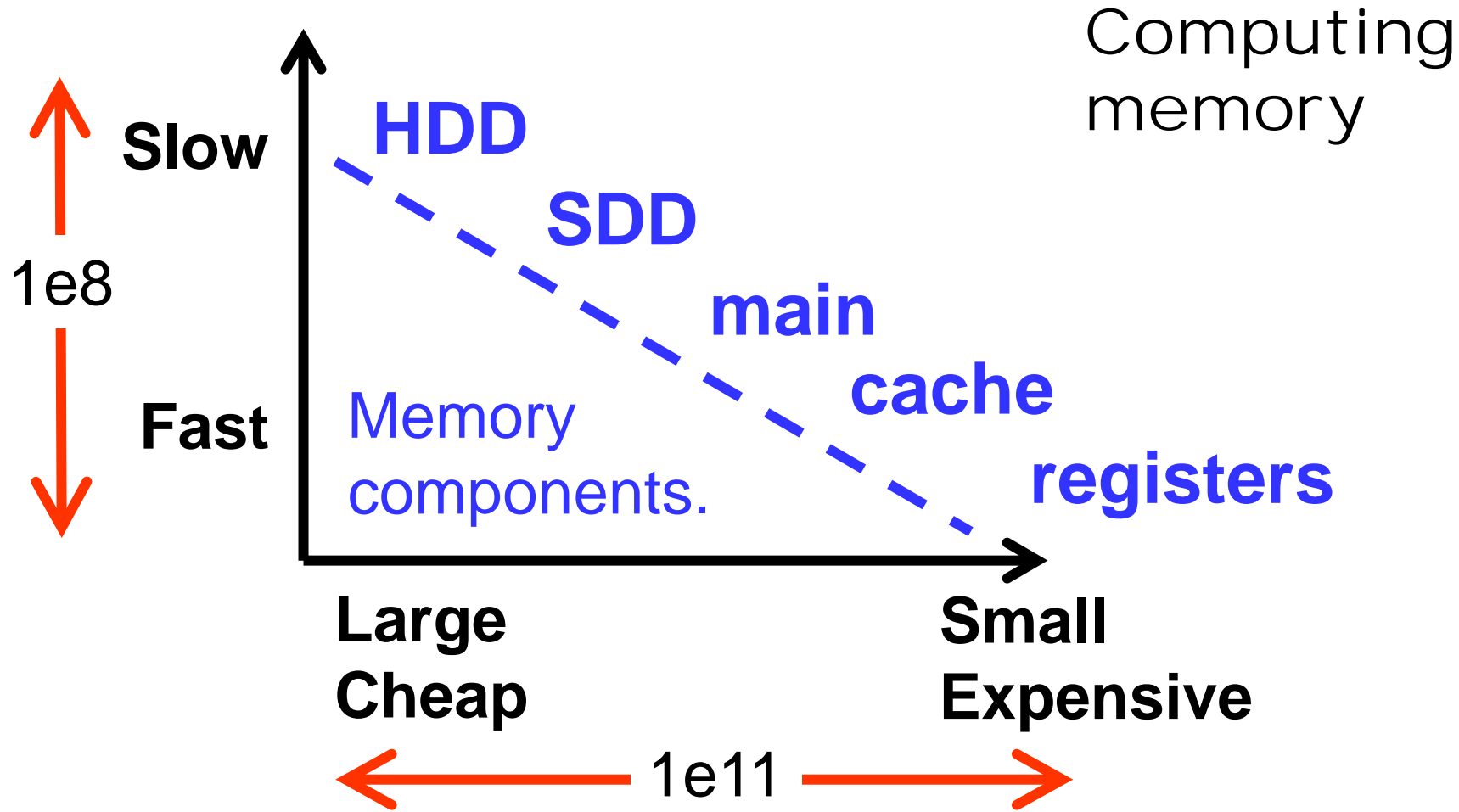


Fast
Easy

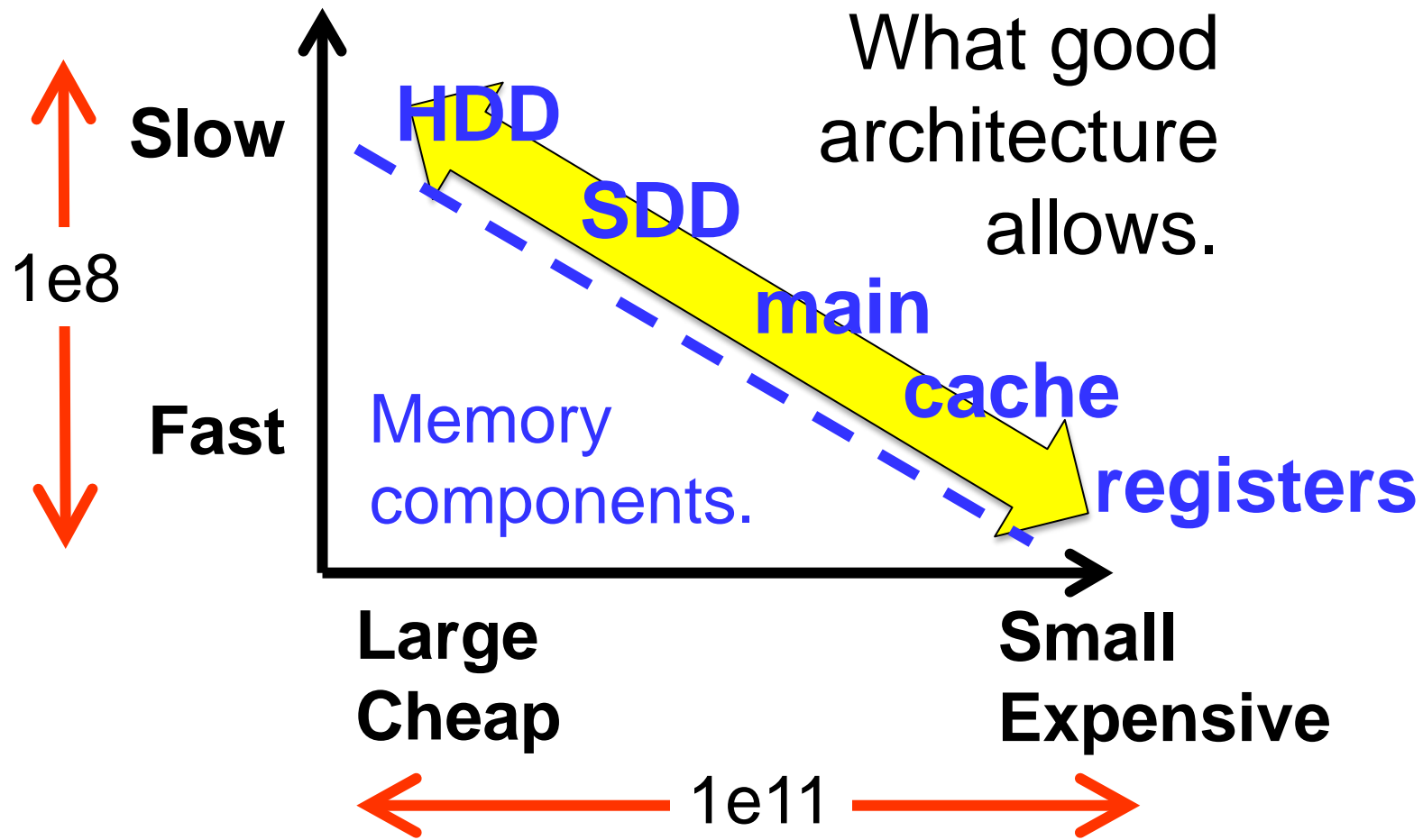
Learn



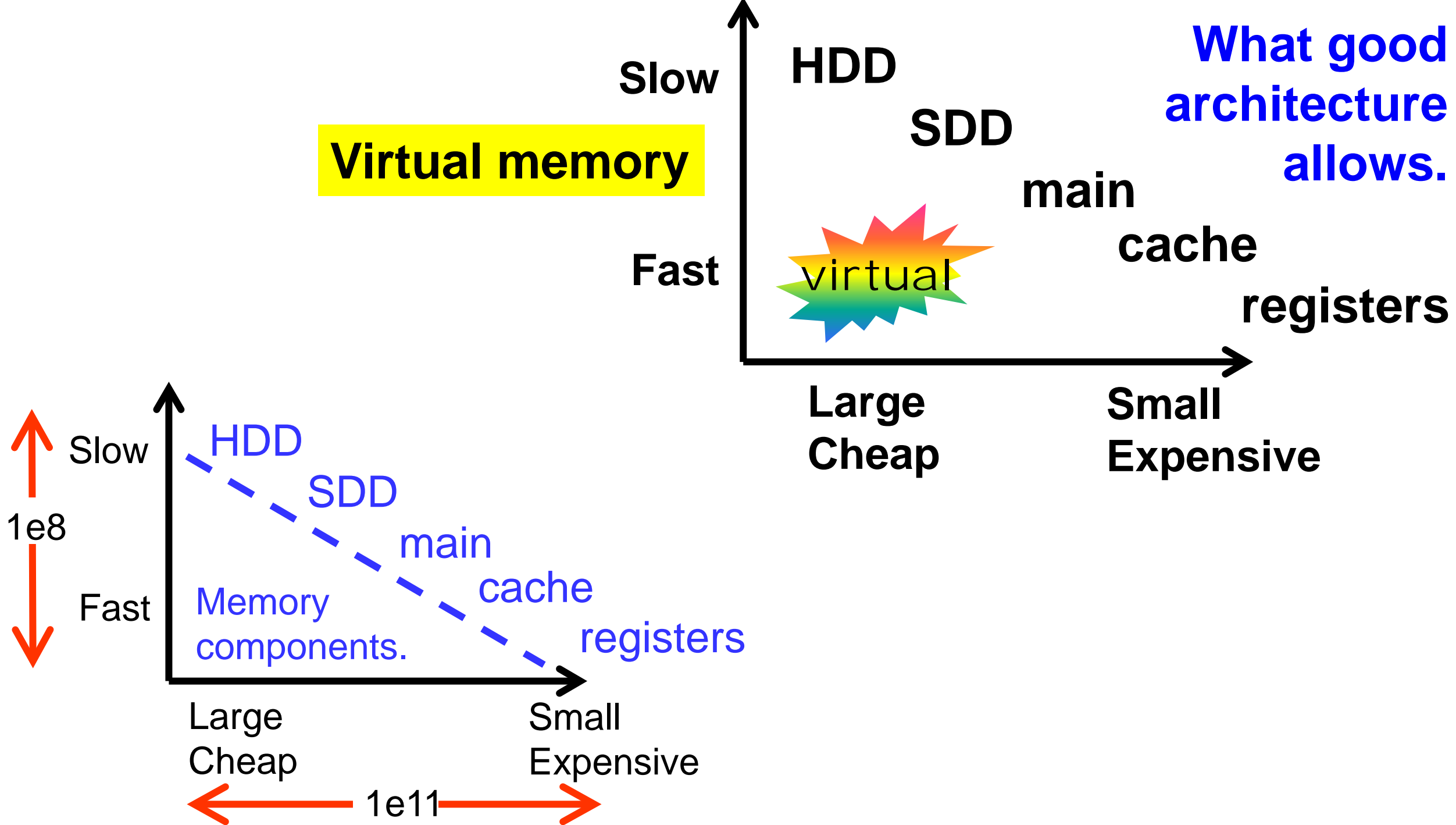




What good architecture allows.



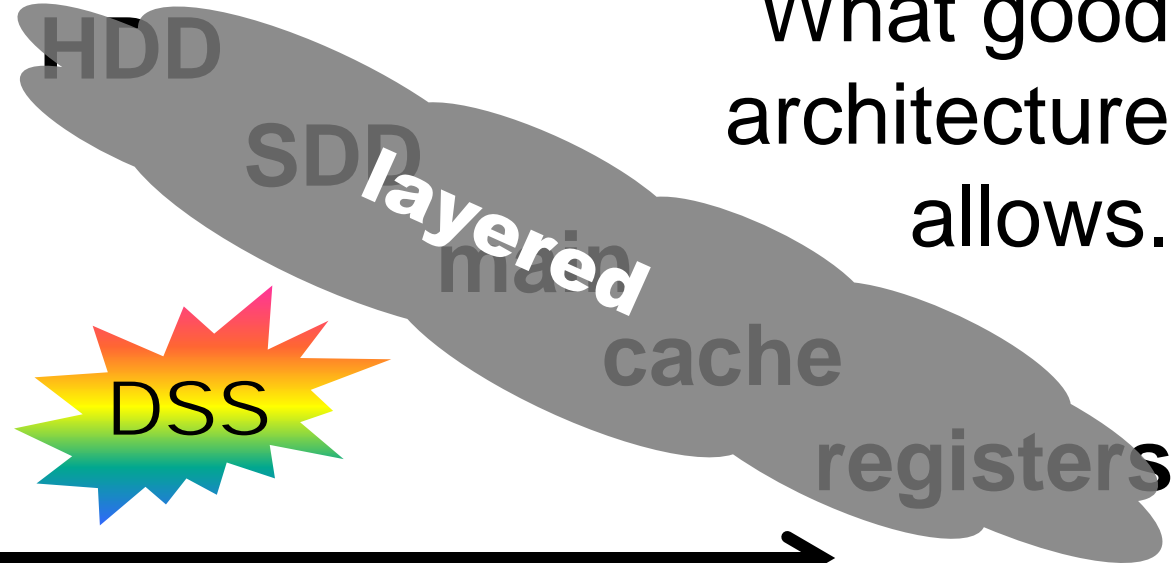
Flexibly
build what
is possible.



Virtual memory

Slow

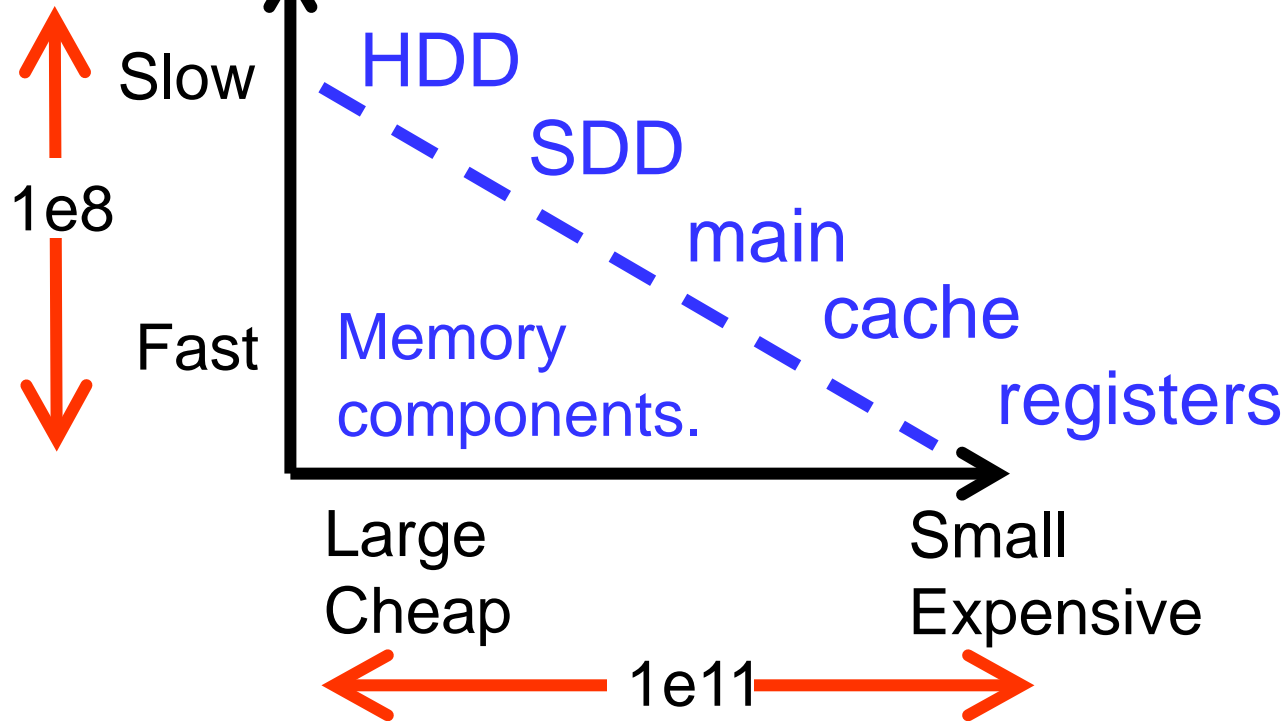
Fast



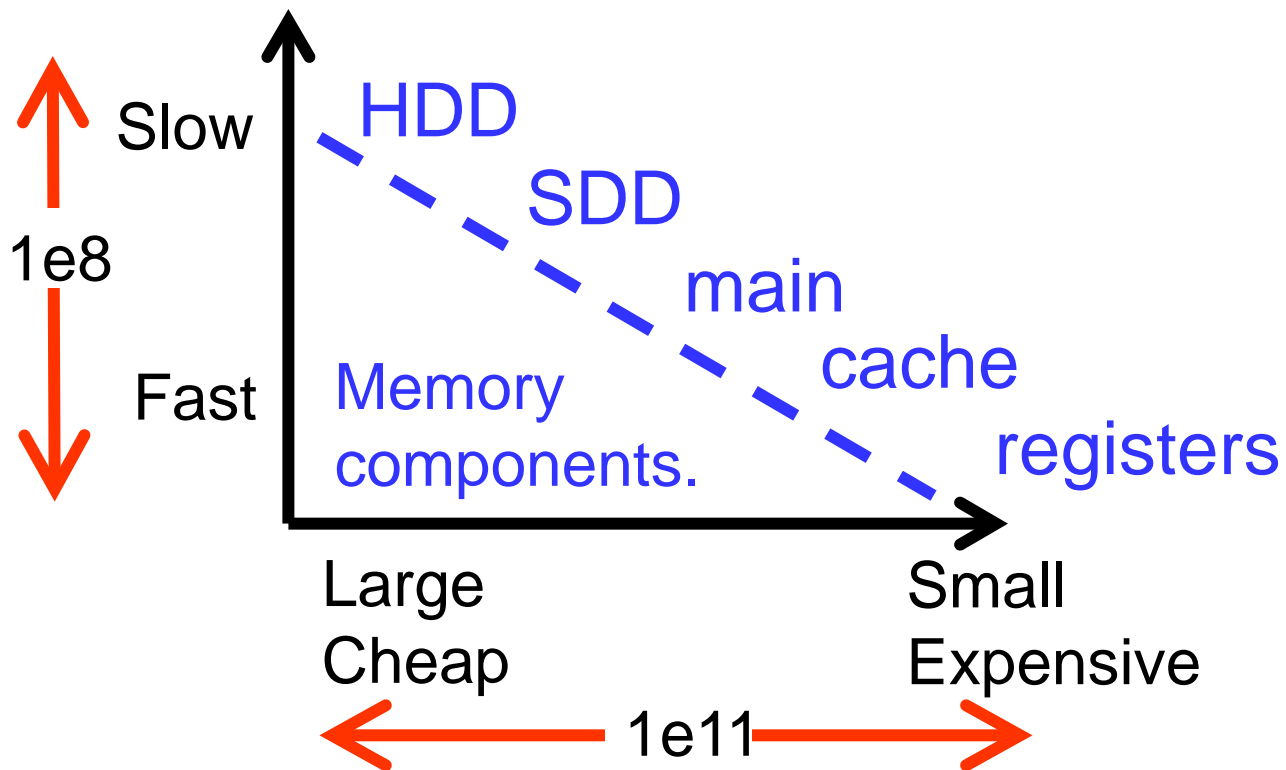
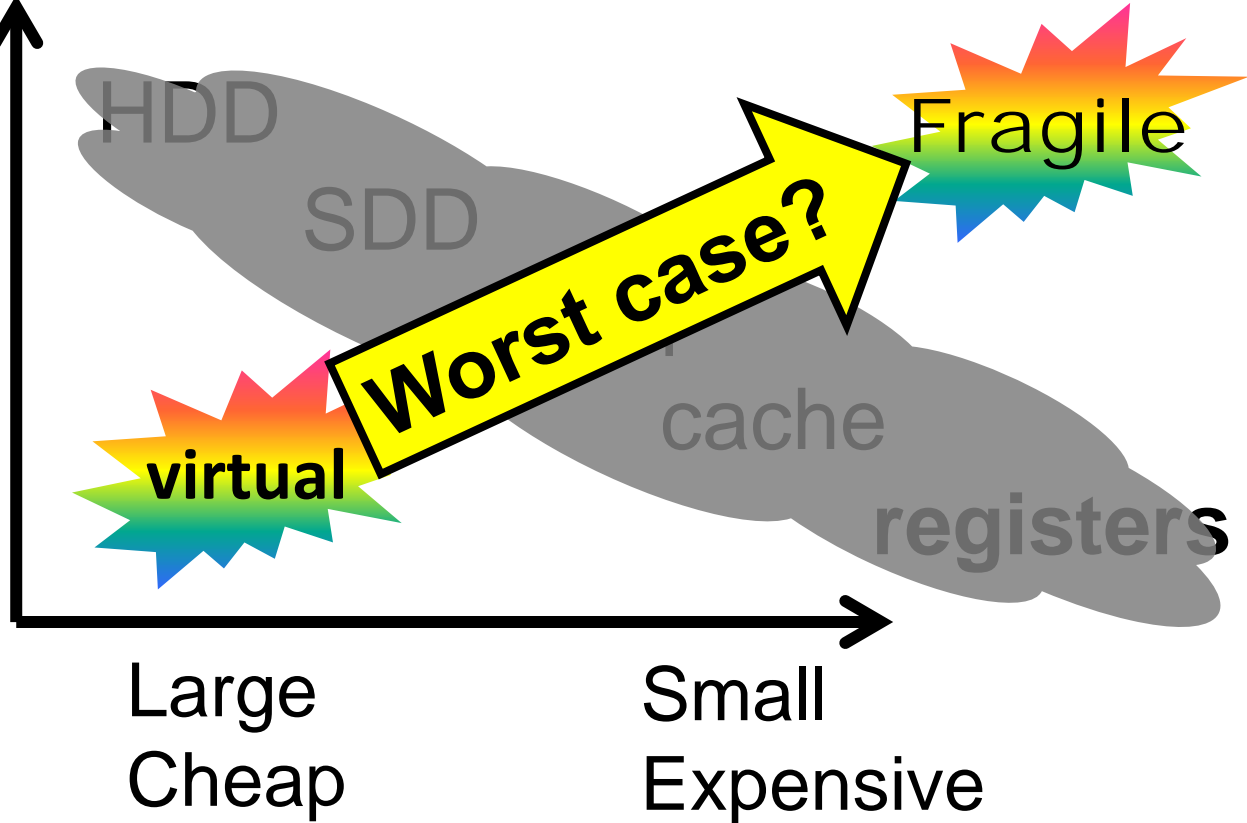
Large Cheap

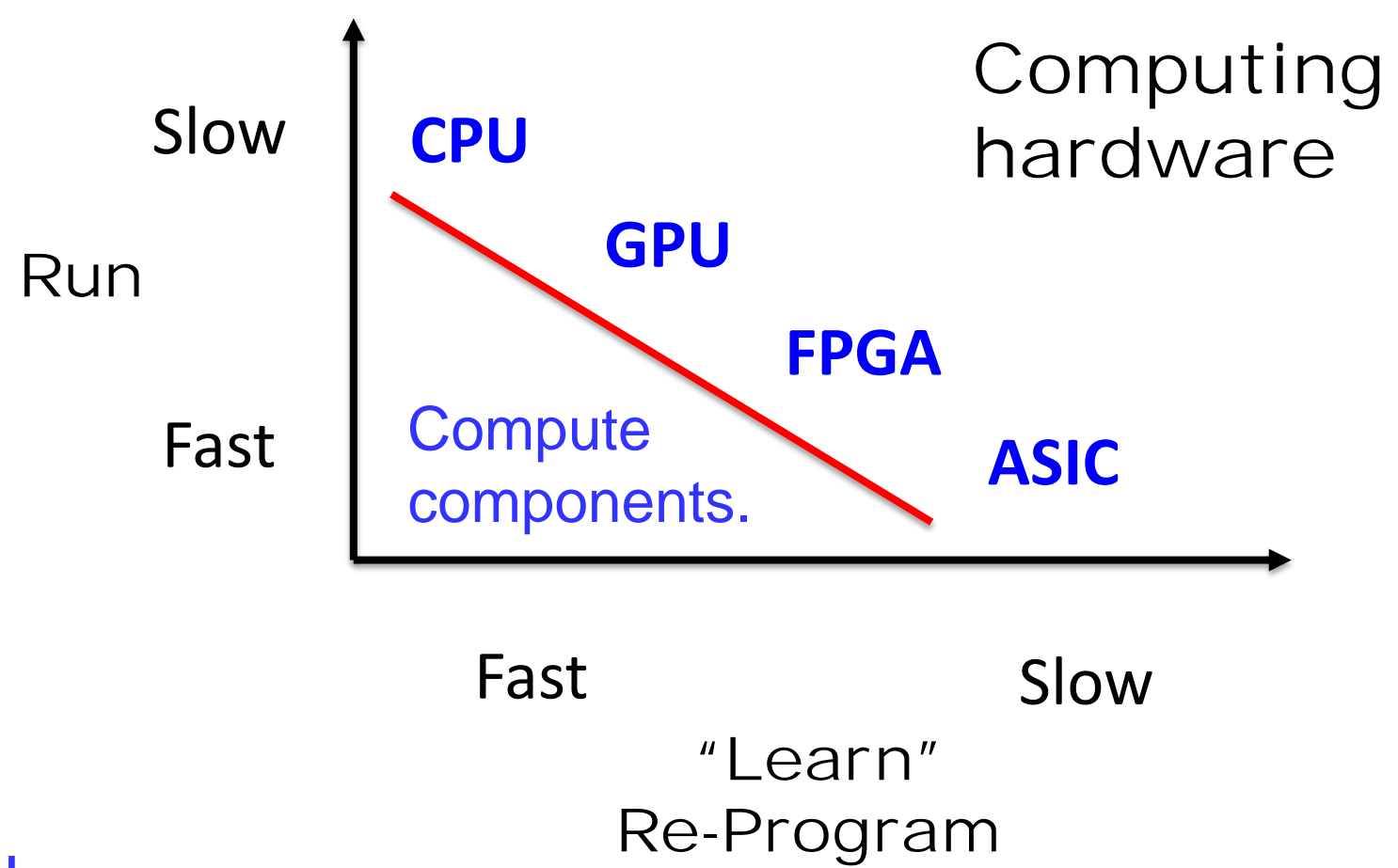
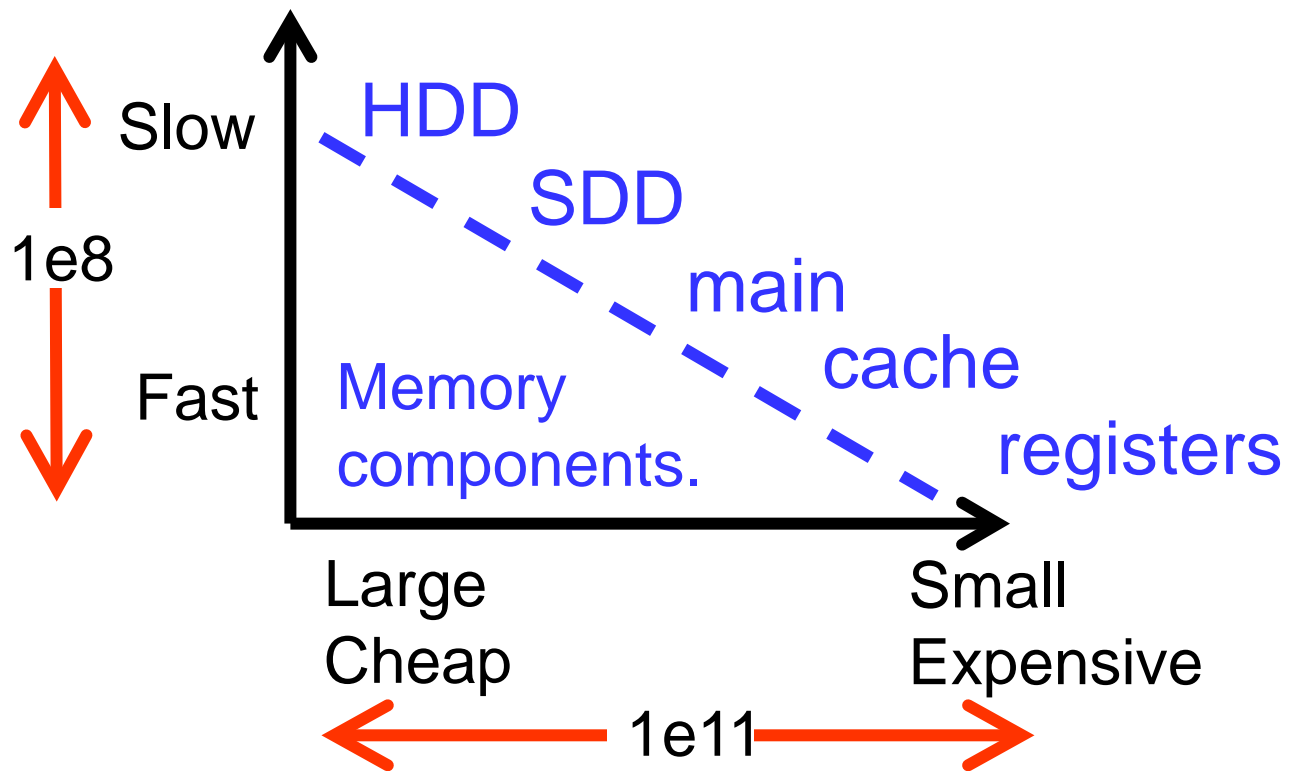
Small Expensive

Diversity Sweet Spot

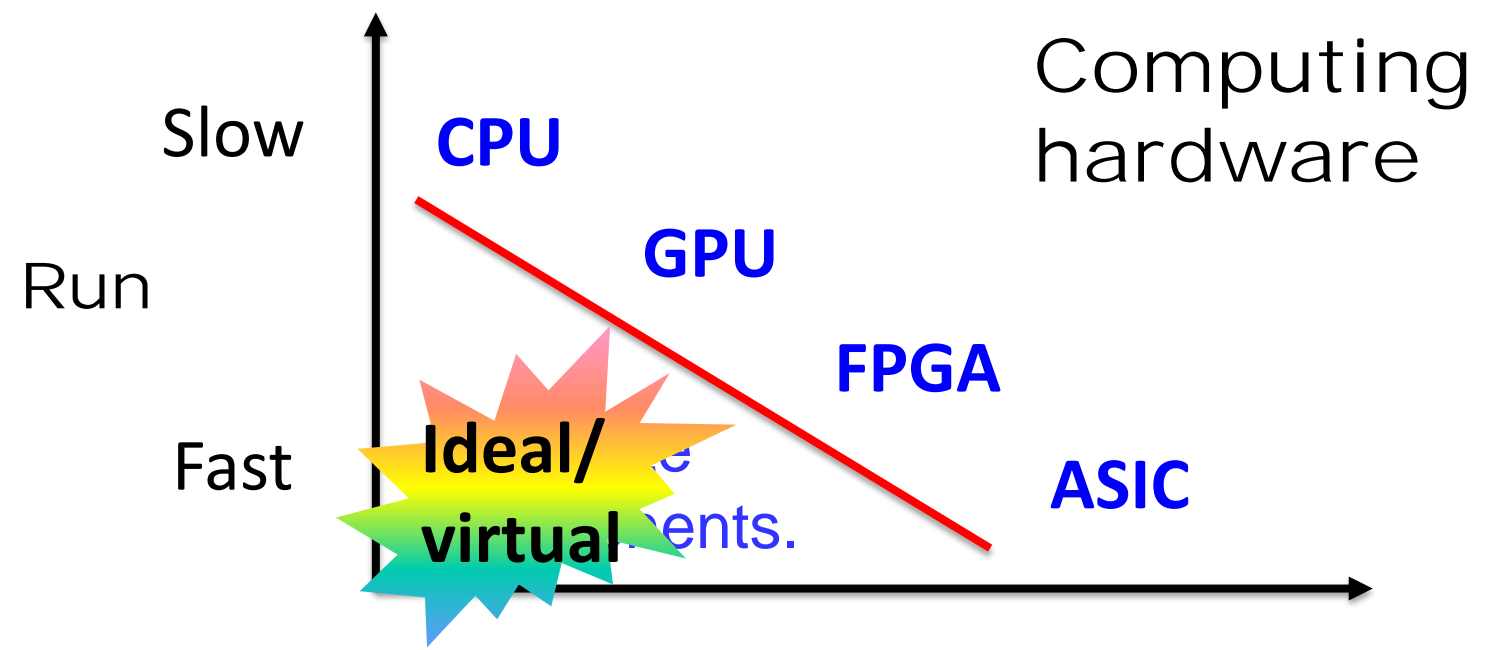
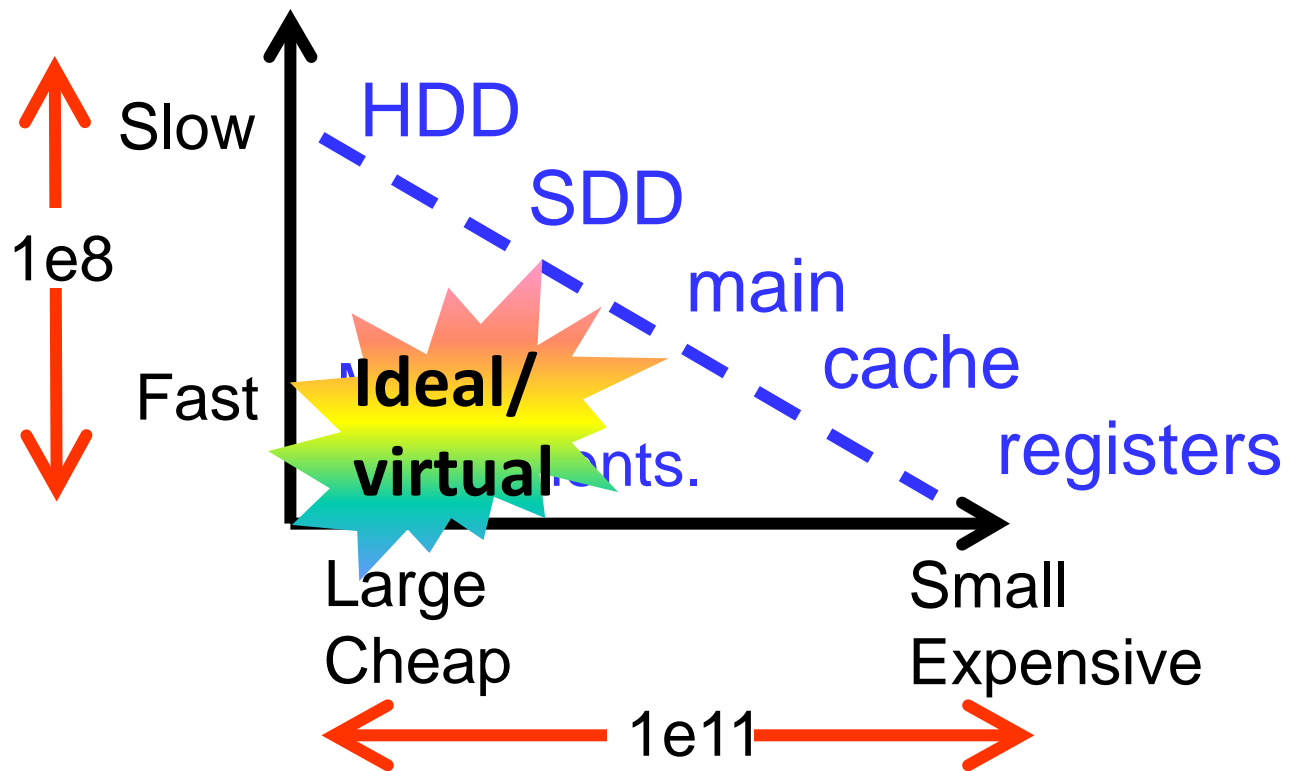


Virtual memory





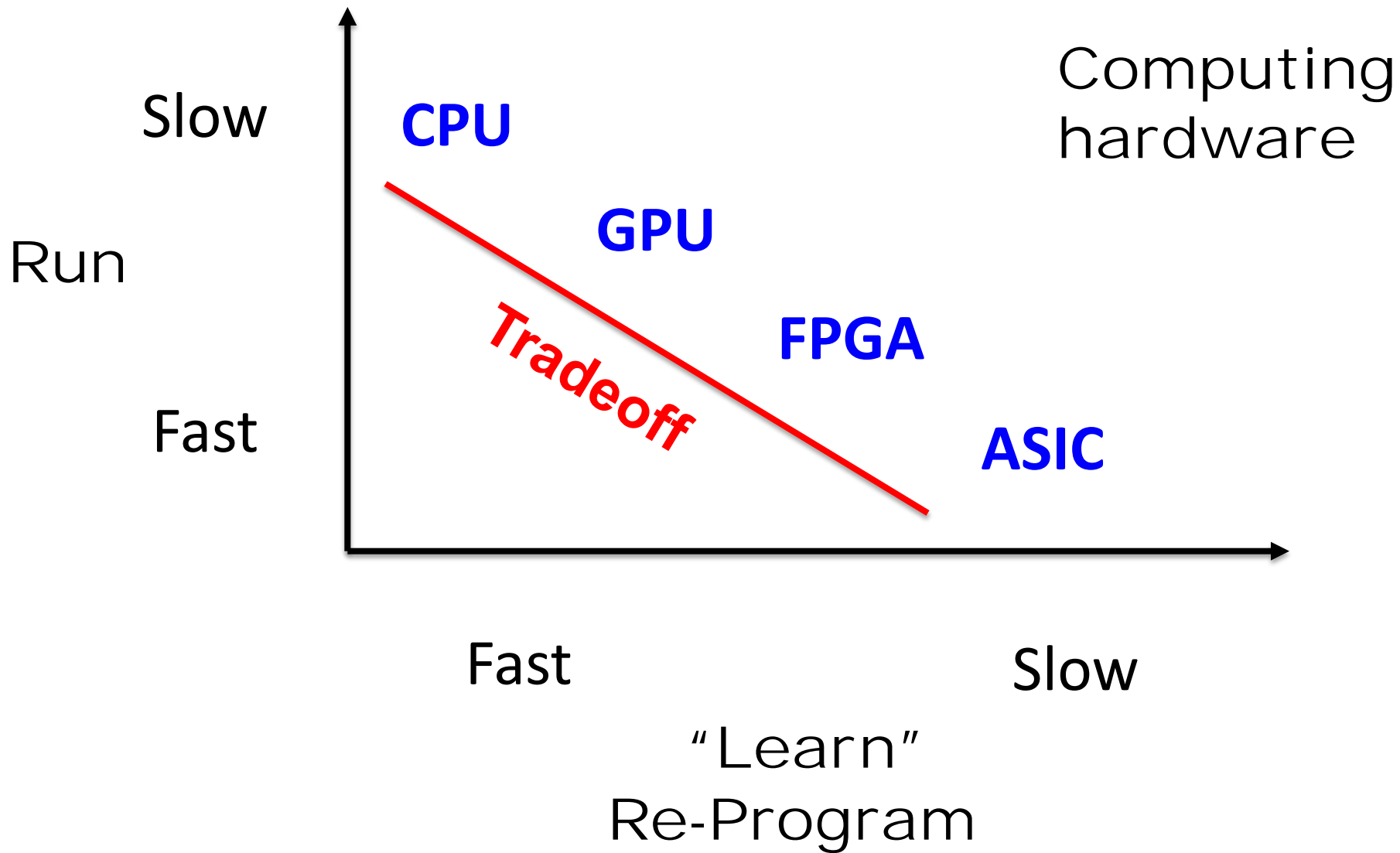
"Learn"
 Re-Program

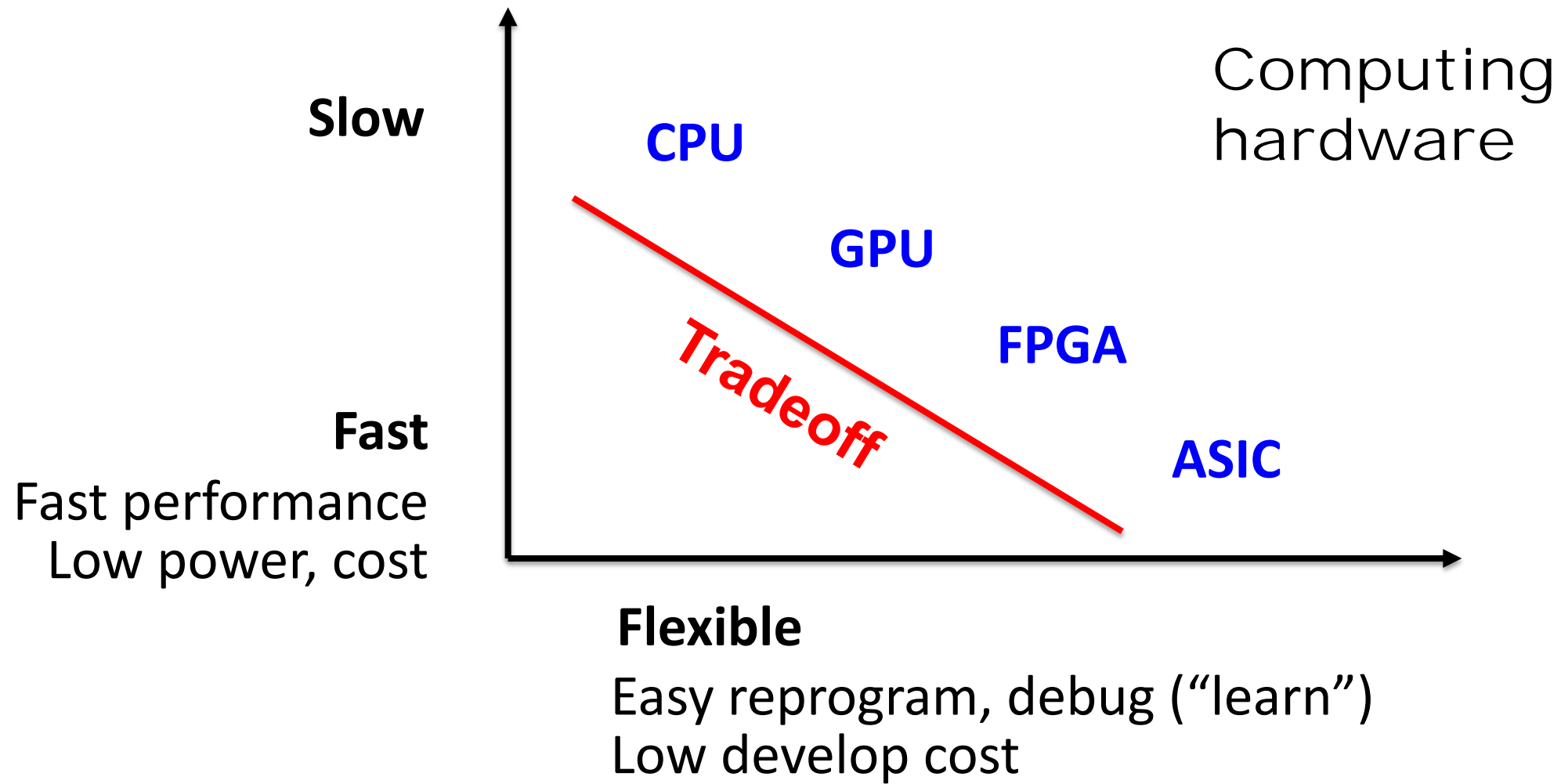


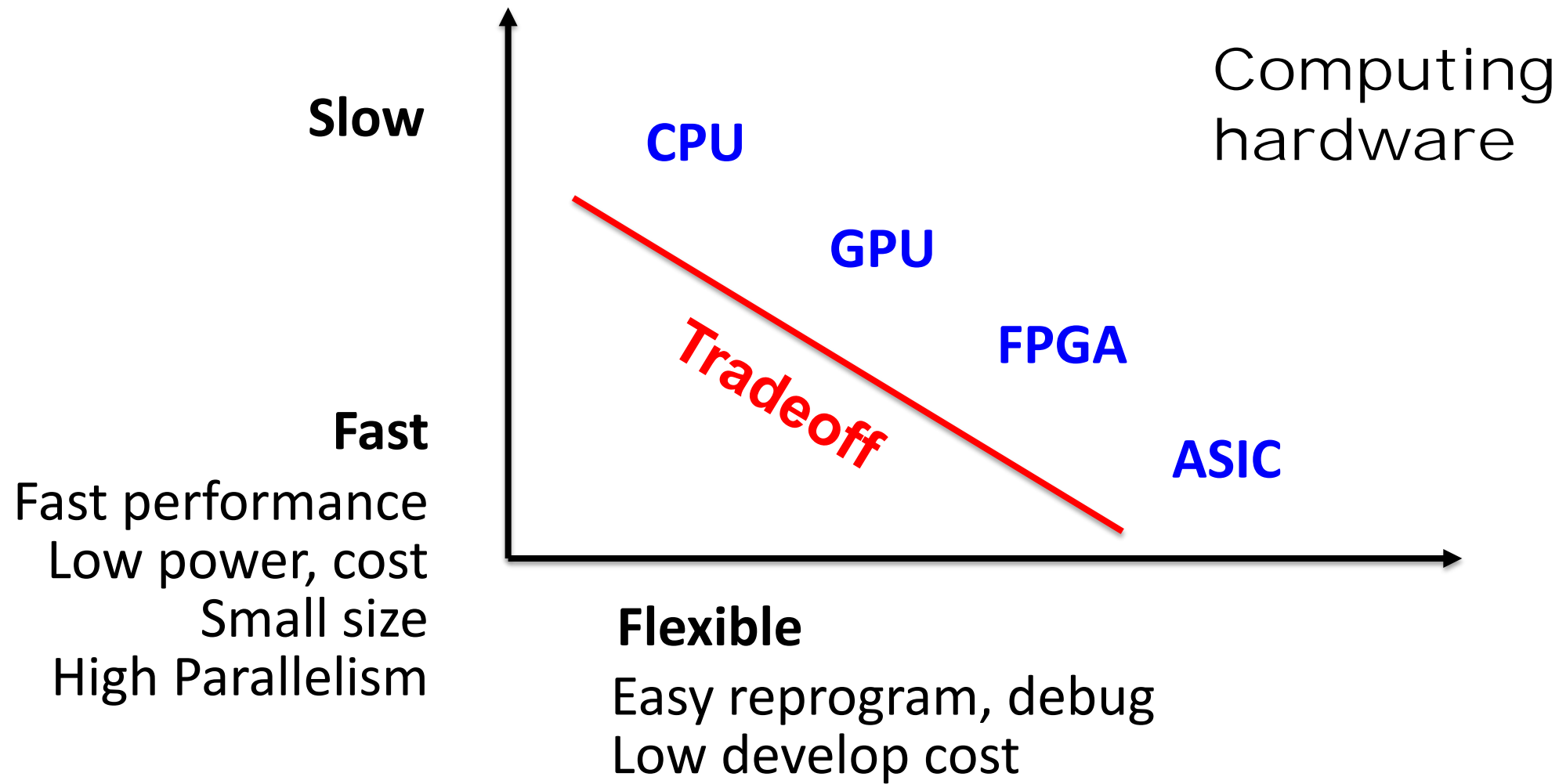
Computing hardware

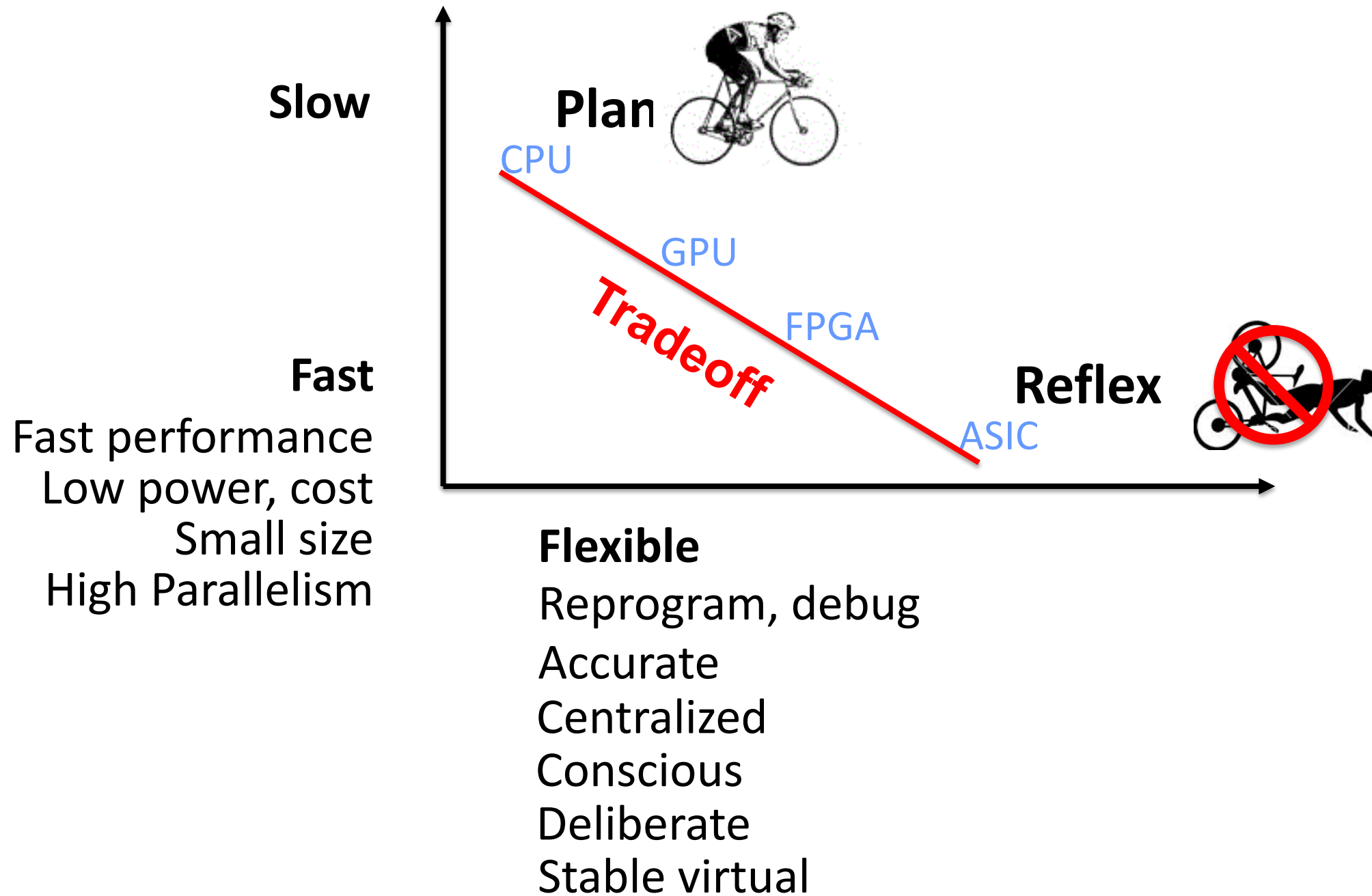
“Learn”
Re-Program

Diversity Sweet Spots









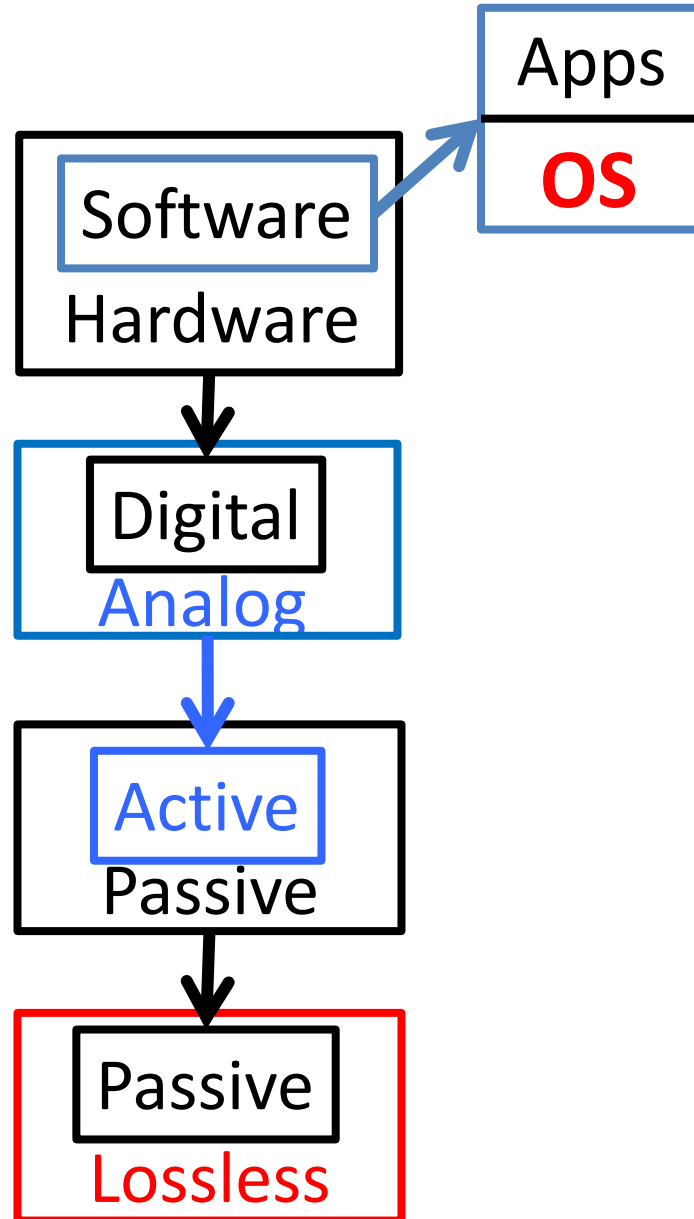
Virtualization

Mechanistic
Concrete

Networks

- Socio
- Techno
- Neuro
- Bio

- Physics



Math?
Abstract?

Claim: there are universal laws
and architectures that this
cartoon hints at

Question: What are the right
abstractions and mathematics?

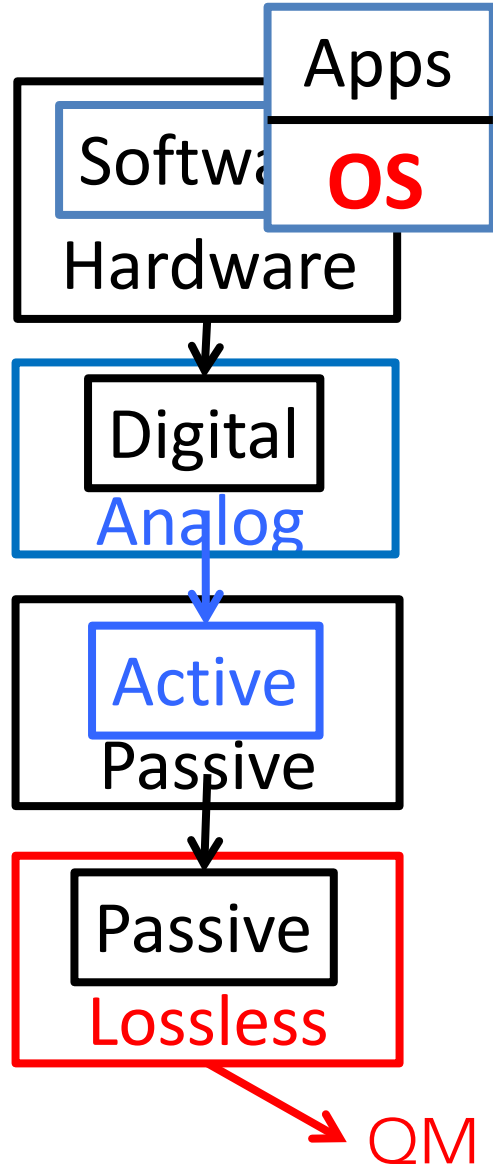
Virtualization

**Mechanistic
Concrete**

Networks

- Socio
- Techno
- Neuro
- Bio

- Physics



Turing

**Kalman
Bode**

**Shannon
Nyquist**

**Boltzmann
Carnot**

Newton

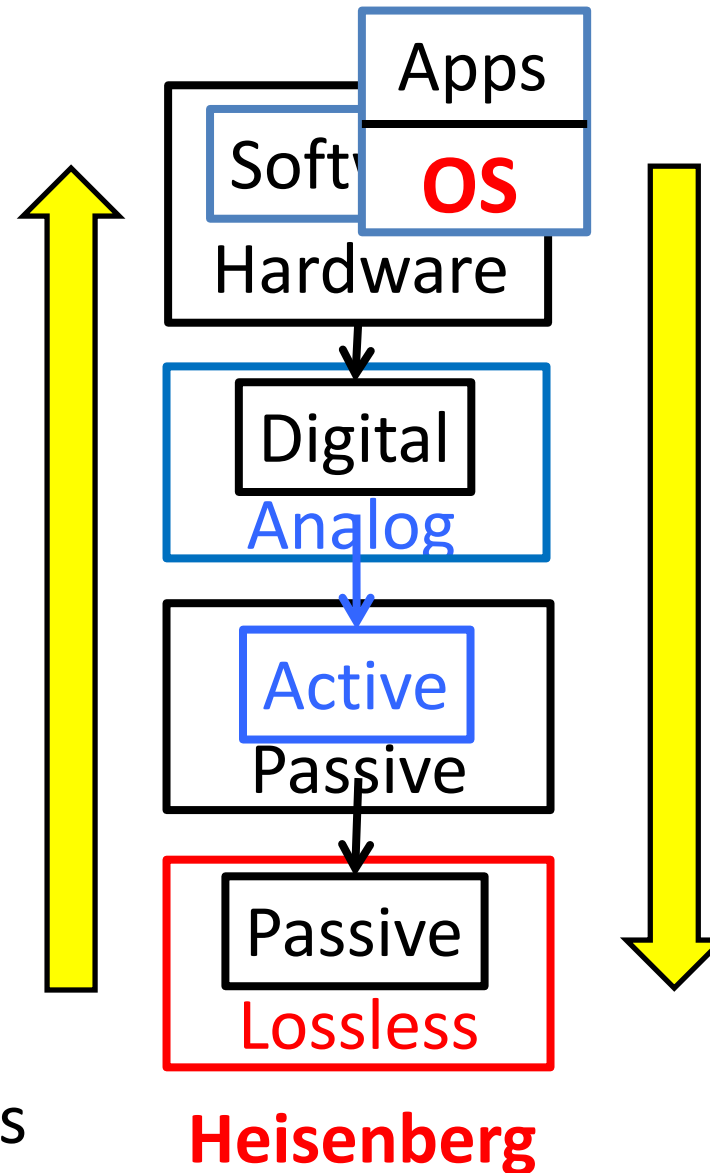
Heisenberg

**Math
Abstract**

- Incoherent, disconnected, models, abstractions, “laws”
- Historical artefacts
- No overall architecture

Virtualization

Turing



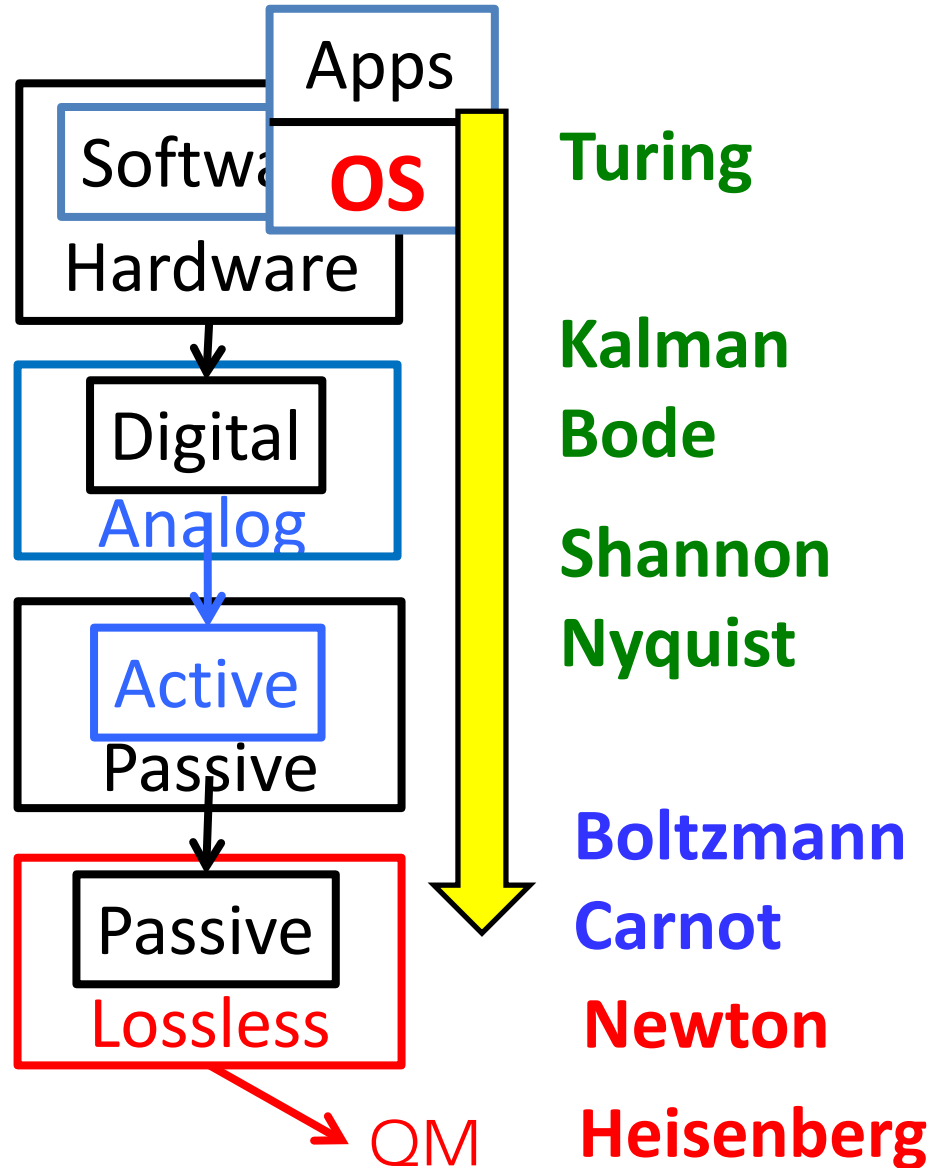
Physics

- “new sciences”
- No tradeoffs
- Minimally architectural
- Large, thick, convex
- Order for free
- Self-organization
- Emergence, edge of...
- Chaos, criticality, fractals

Engineering/math

- Tradeoffs everywhere
- Maximally architectural
- Large, thin, nonconvex

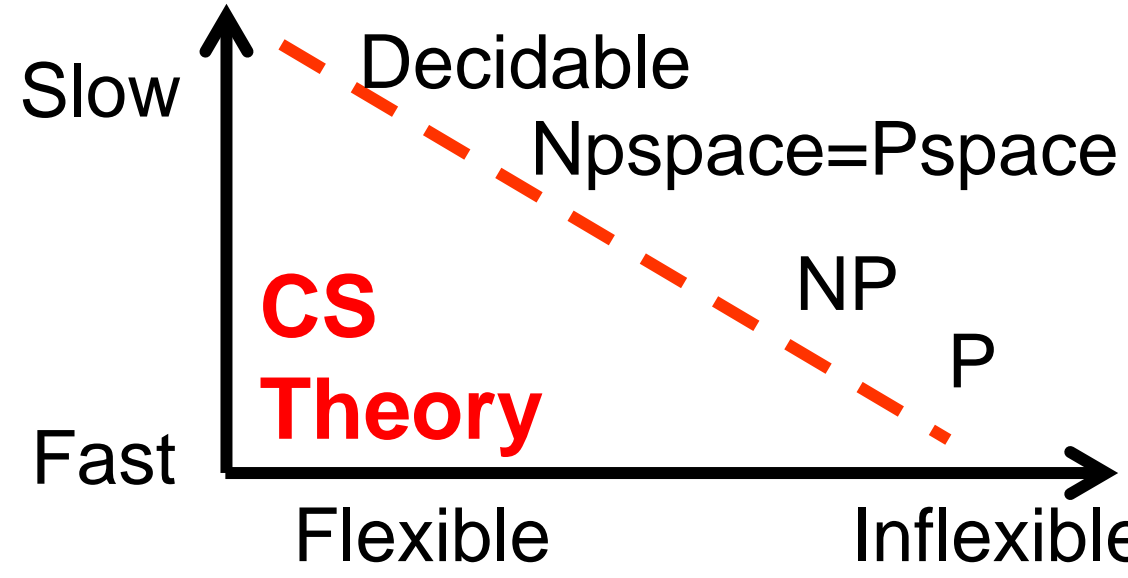
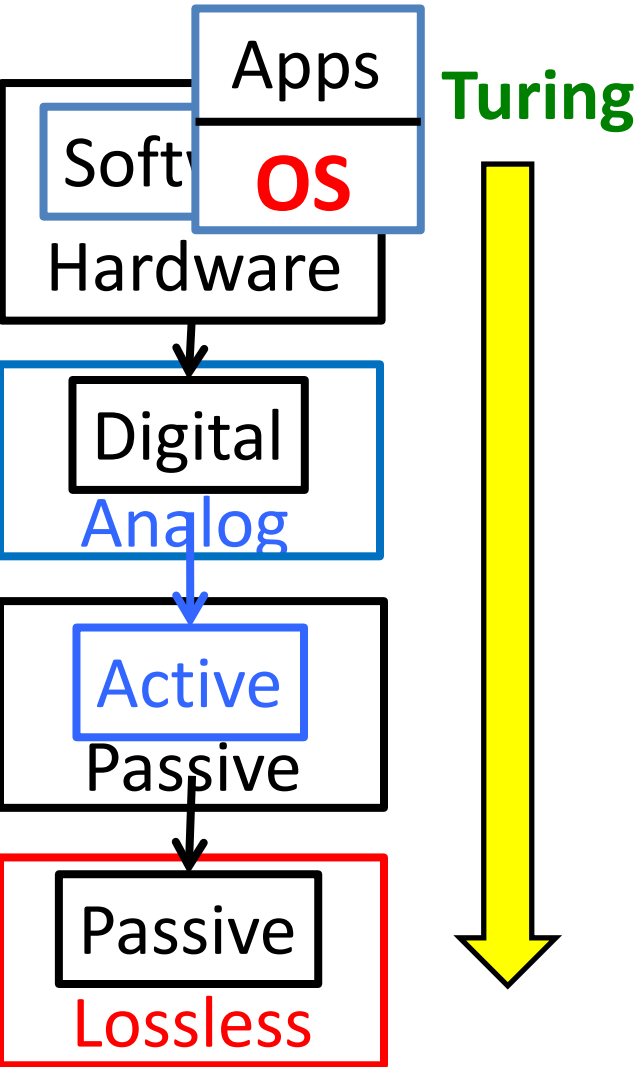
Virtualization reboot



Math Abstract

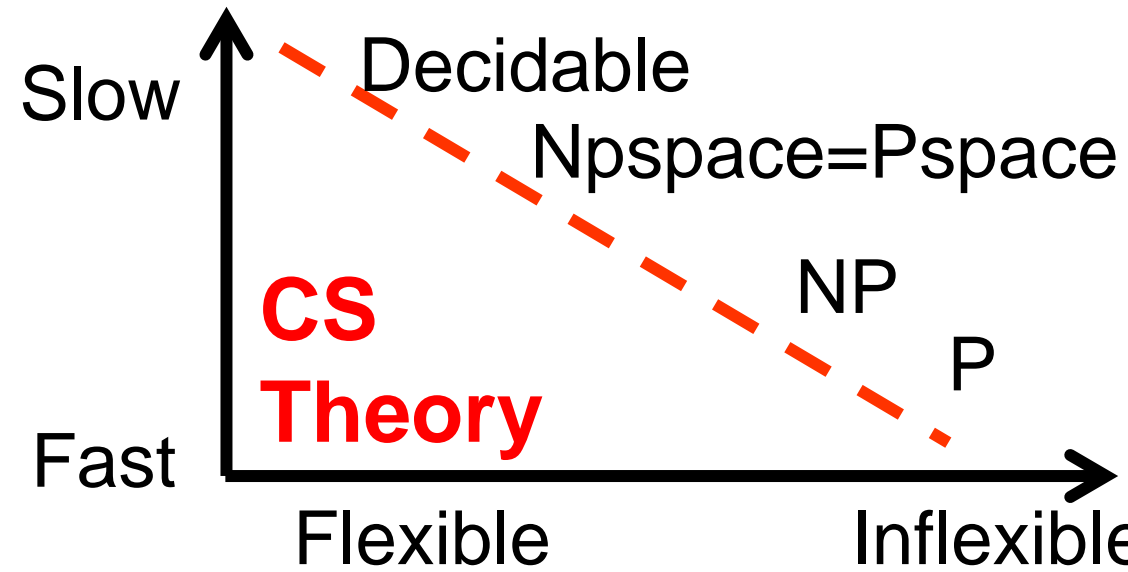
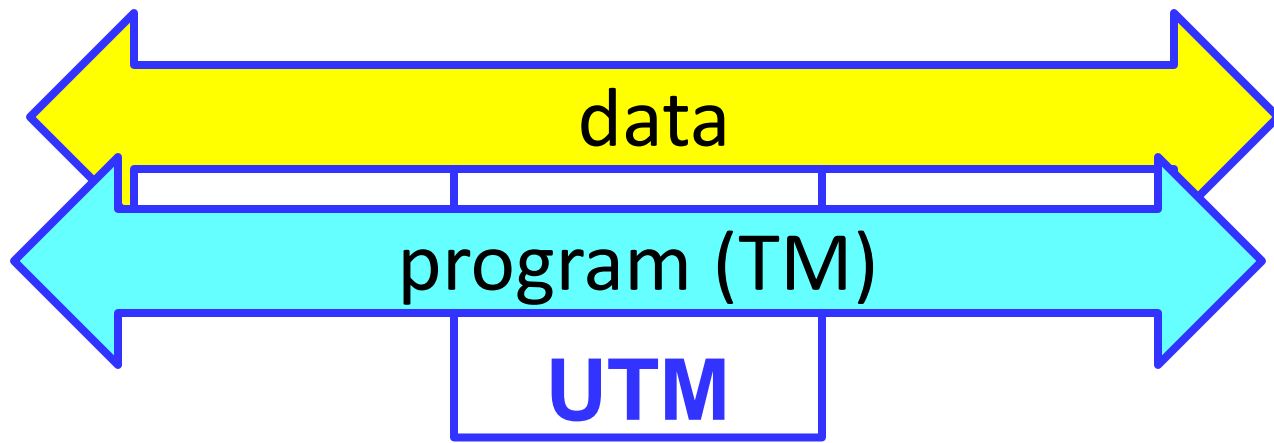
- Top down, start with Turing
- Redo “classical” laws (and architectures) but coherent and integrated
- And formulate new laws (and architectures) but...
- Motivated by “new” networks in tech and bio

Virtualization



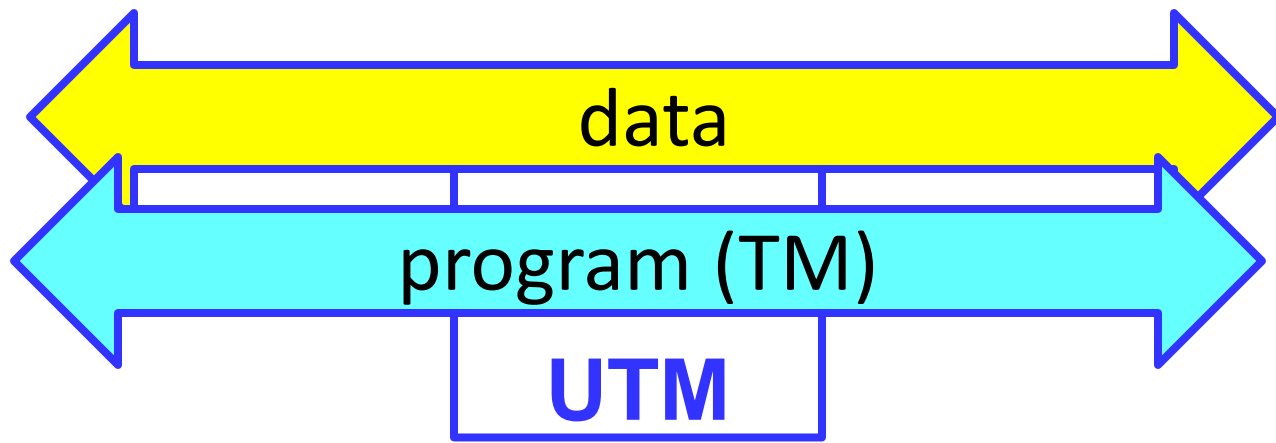
- Tradeoffs everywhere
- Maximally architectural
- Large, thin, nonconvex

Heisenberg



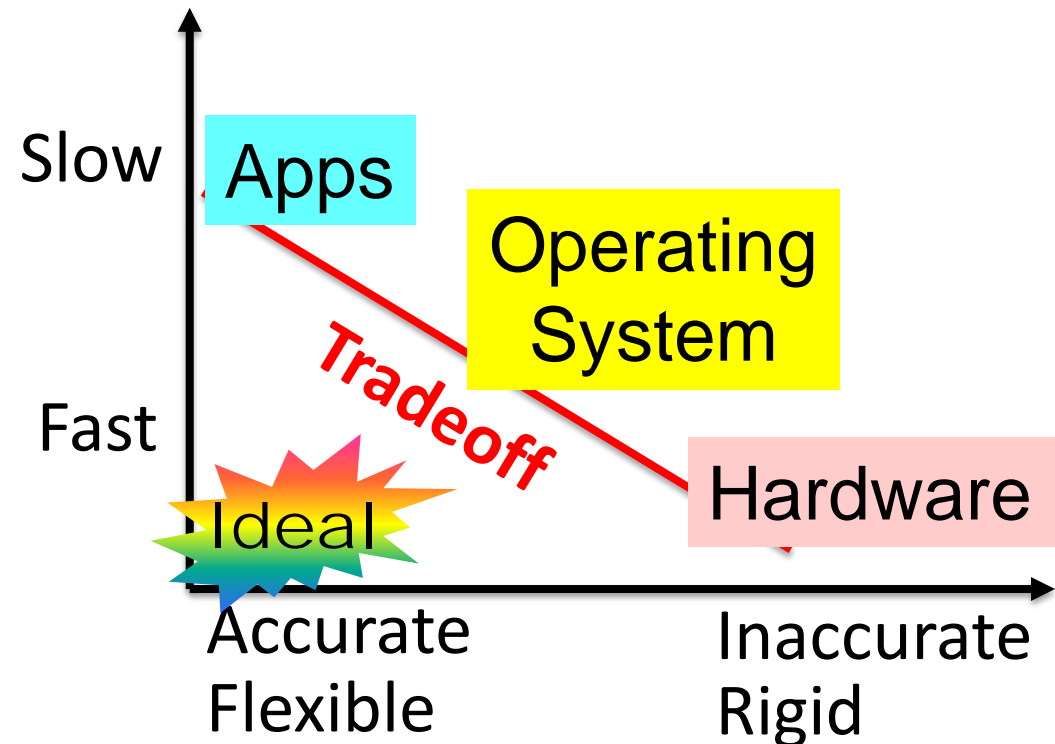
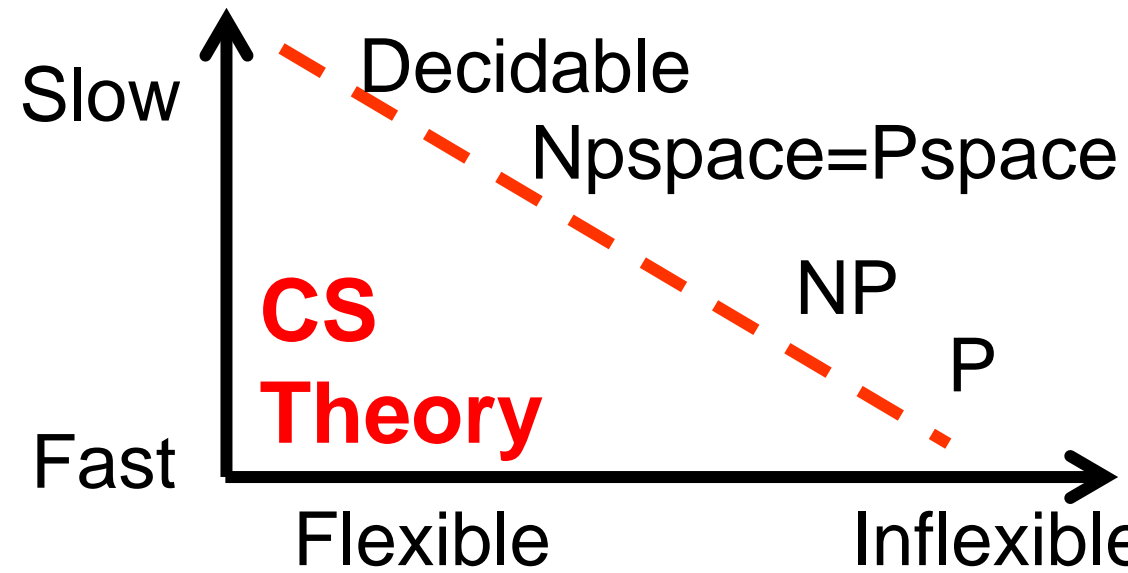
Turing's 3 step research:

0. Virtual (TM) machines
1. hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)**
3. Practical implementation in digital electronics (biology?)

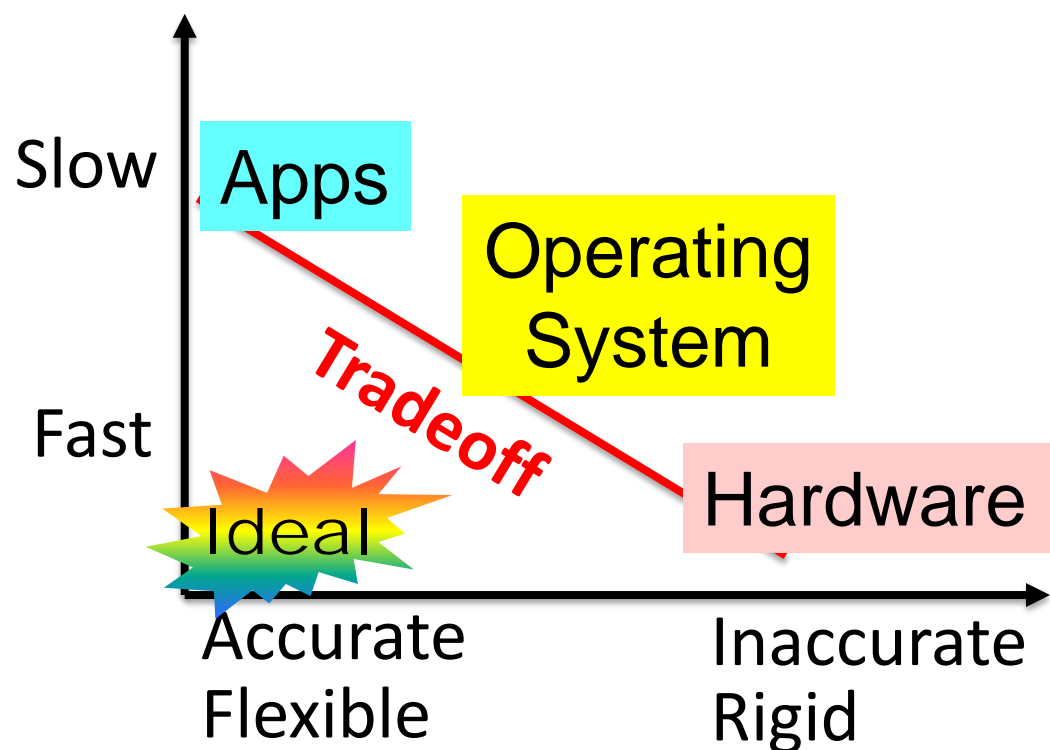
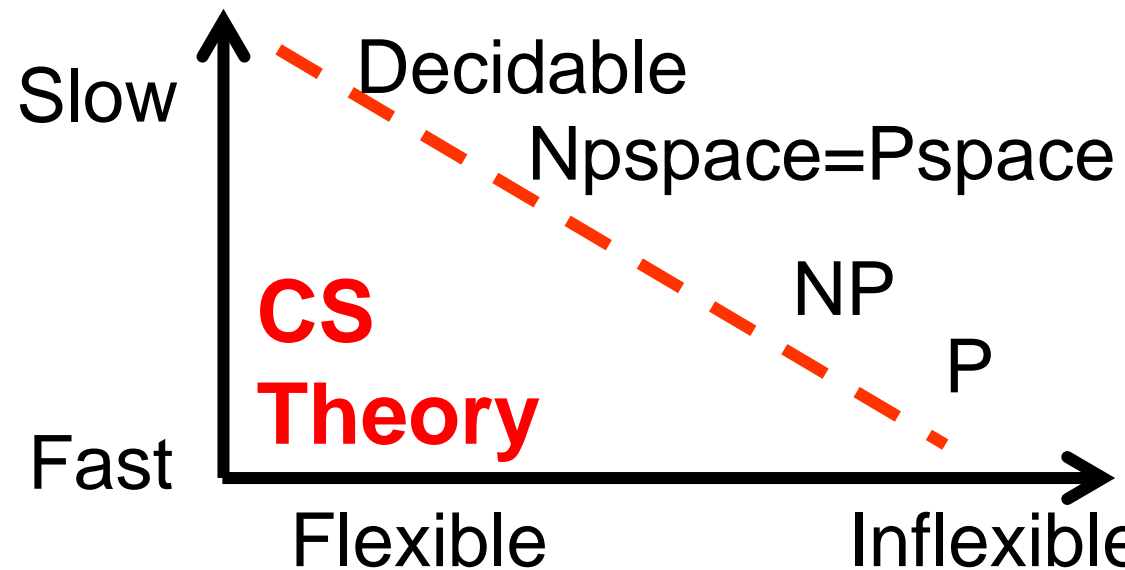
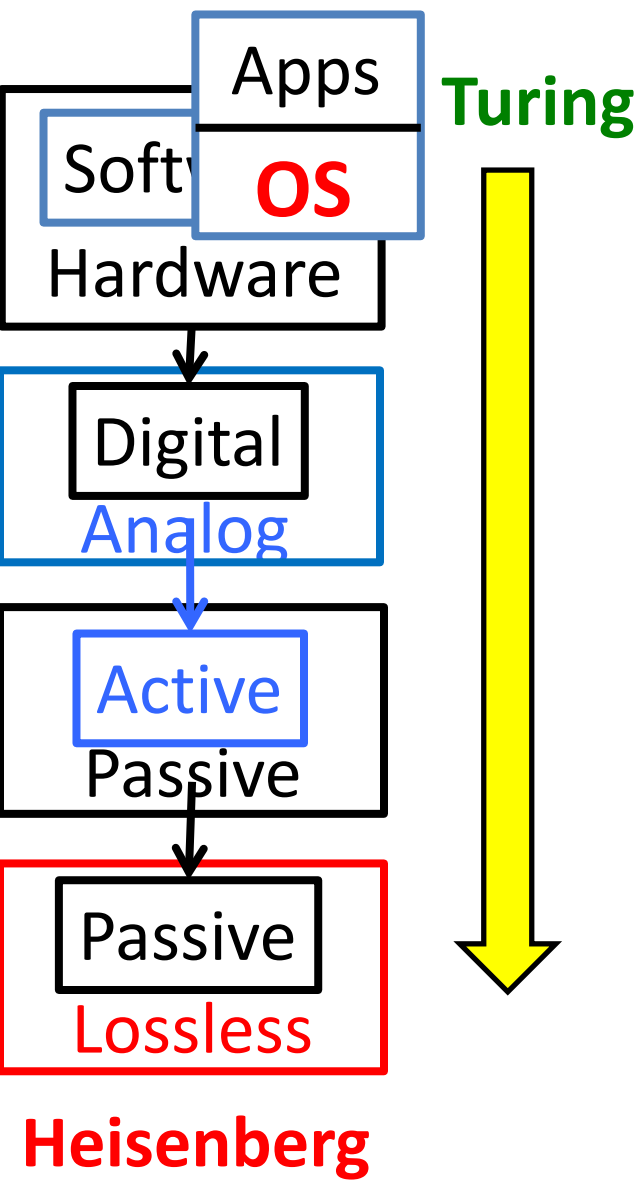


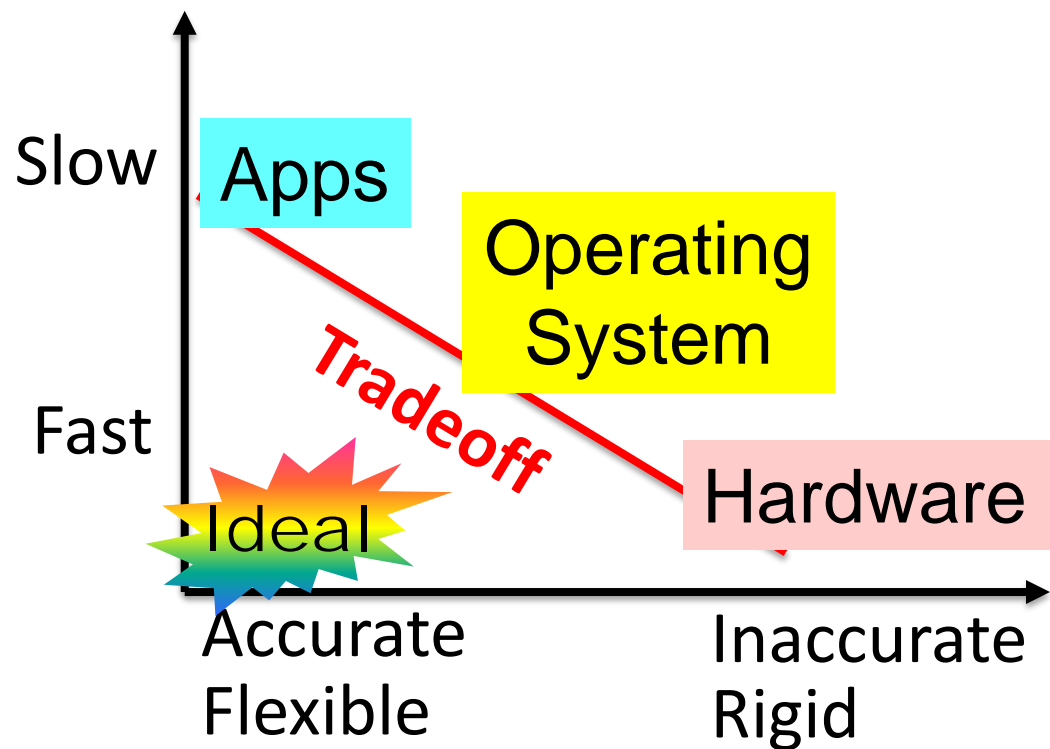
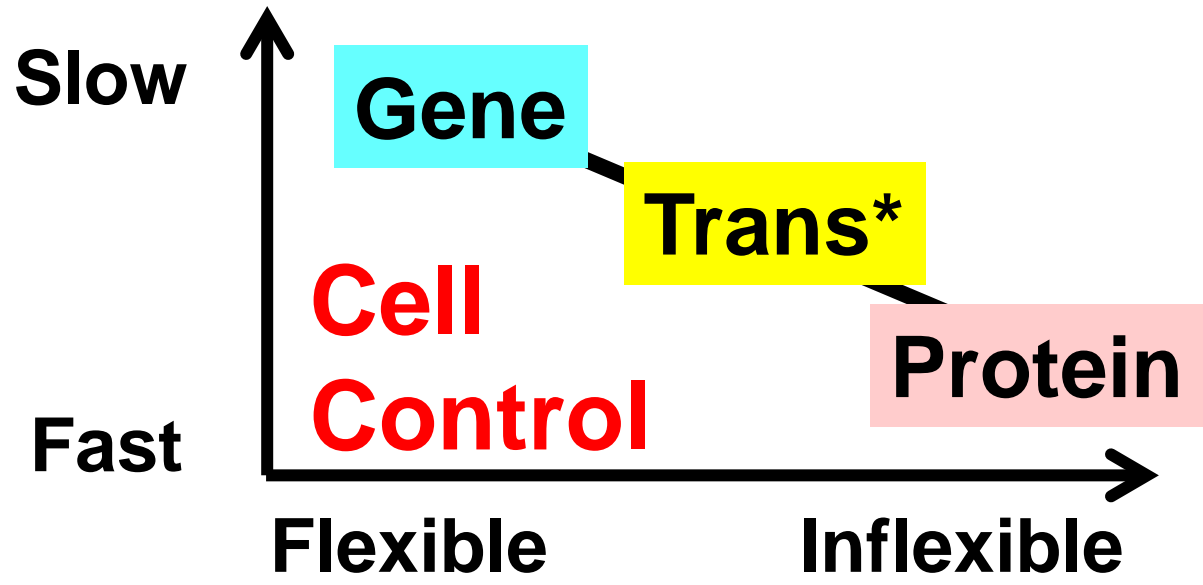
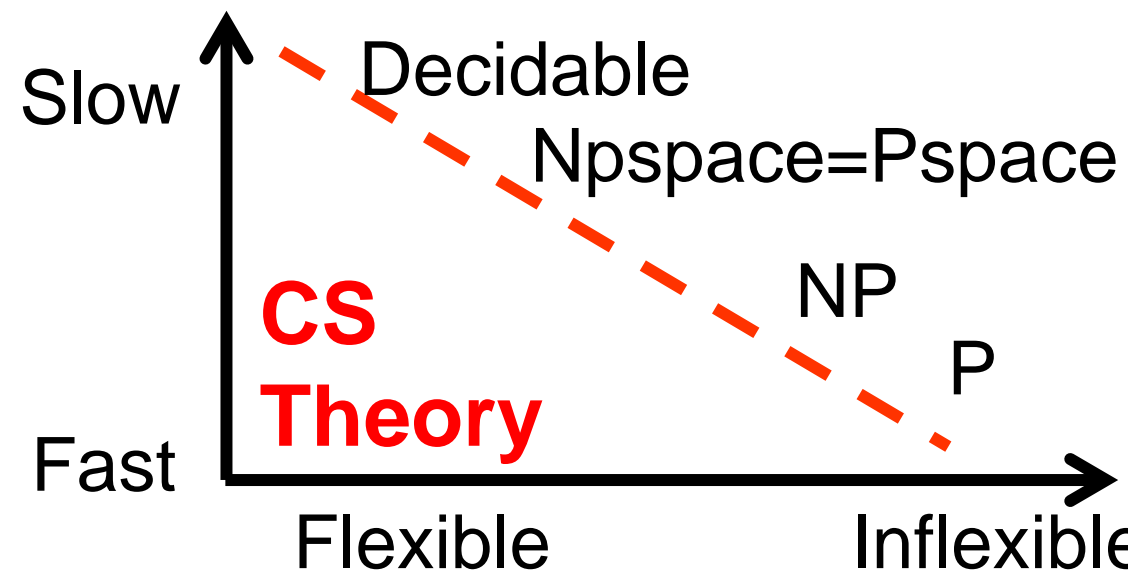
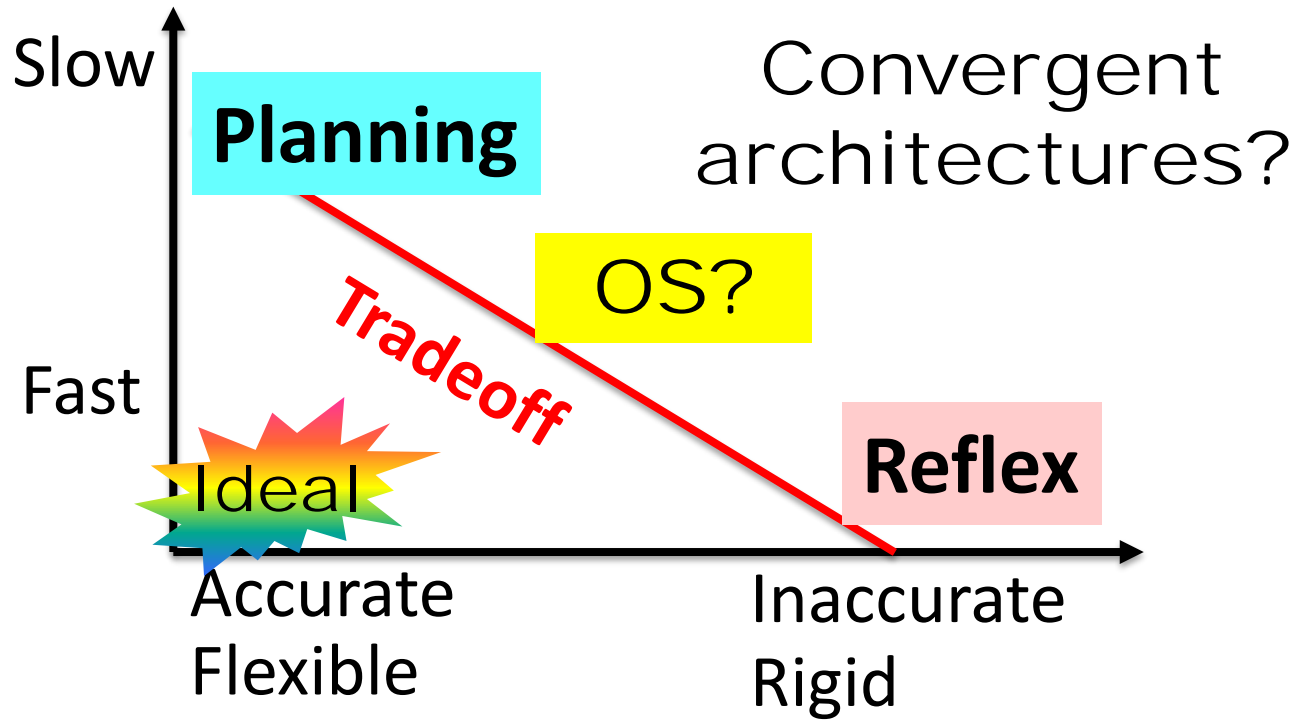
Implications

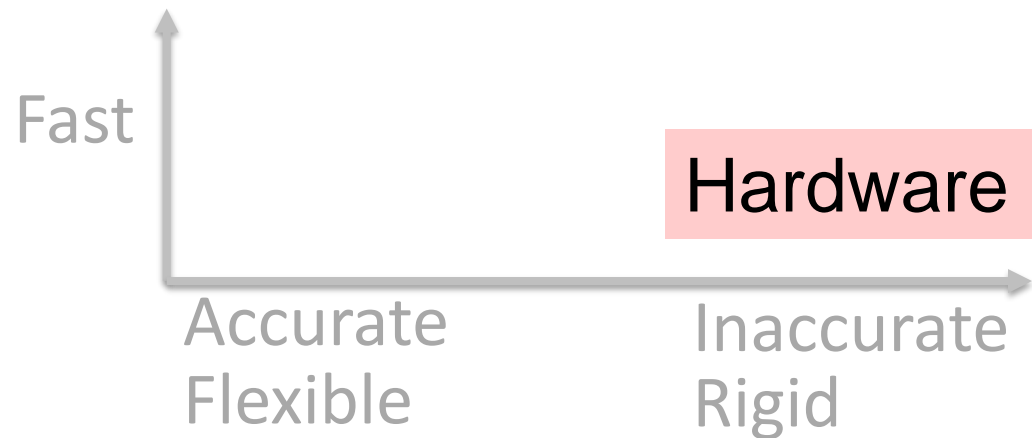
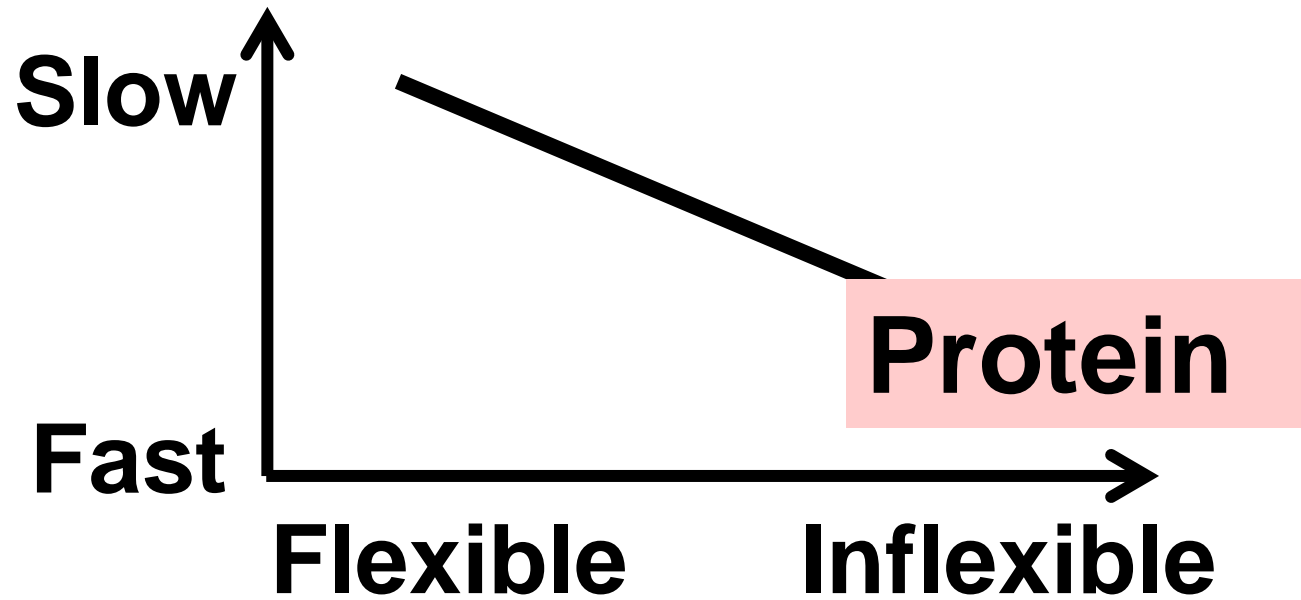
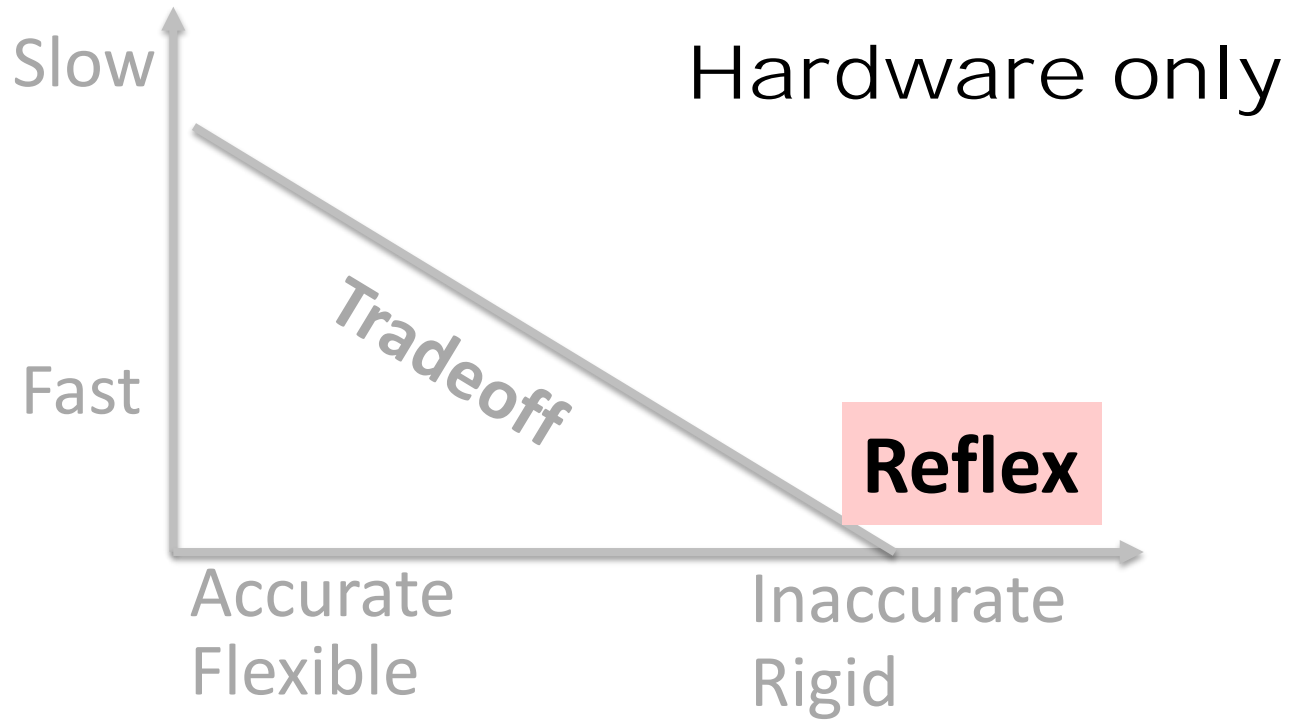
- Large, thin, nonconvex everywhere...
- TMs and UTMs are perfectly repeatable
- But perfectly unpredictable
- Undecidable: Will a TM halt? Is a TM a UTM? Does a TM do X (for almost any X)?
- Easy to make UTMs, but hard to recognize.
- Is anything decidable? Yes, NOT about TMs.
- Time/delay/latency is most precious resource (expensive and limiting)



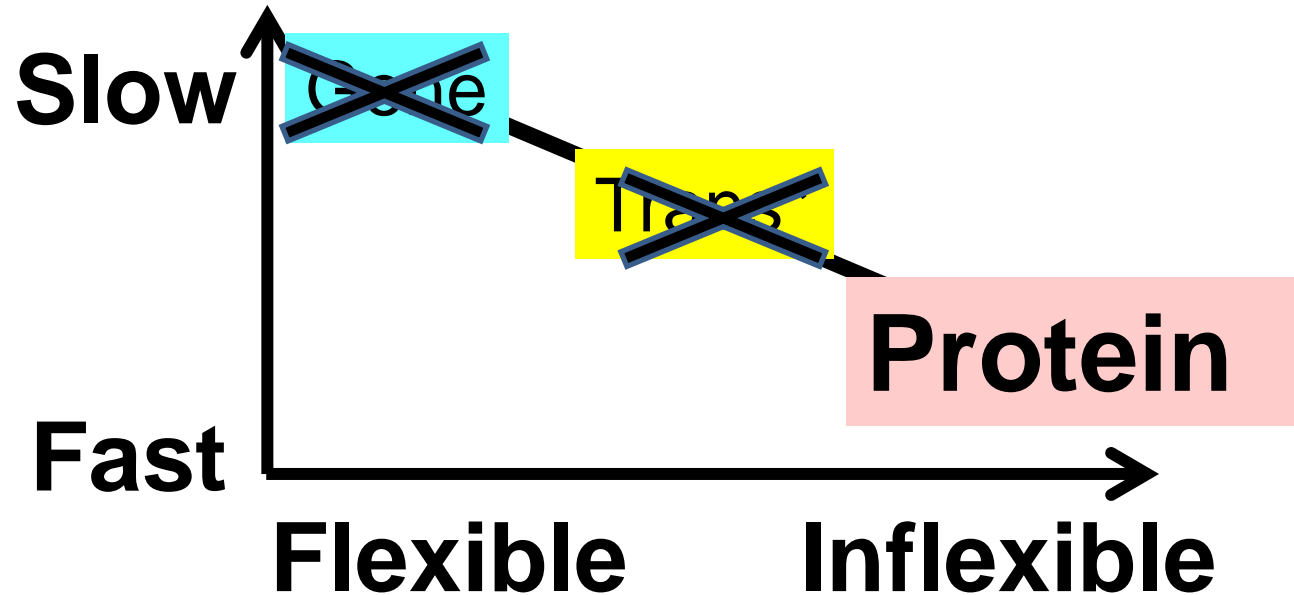
Virtualization







Hardware only



Mammals

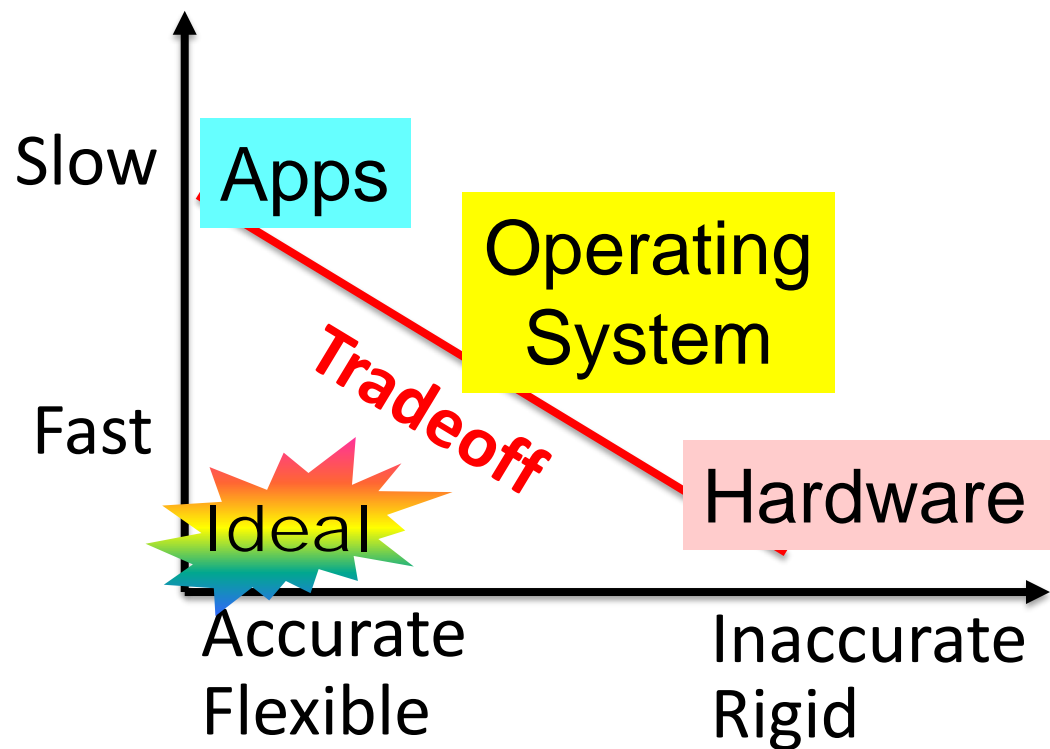
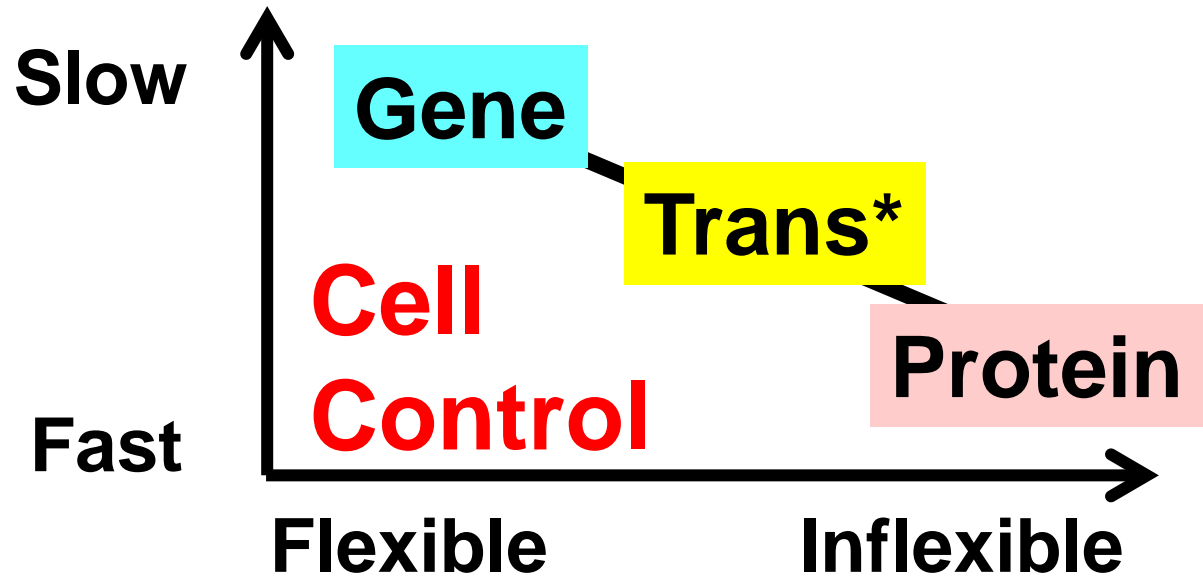
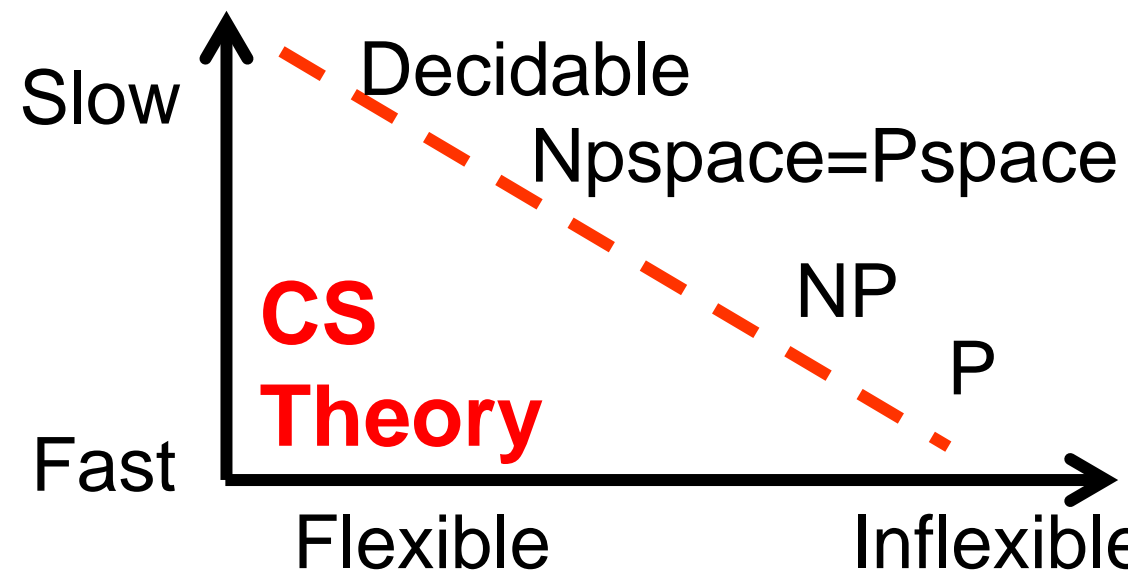
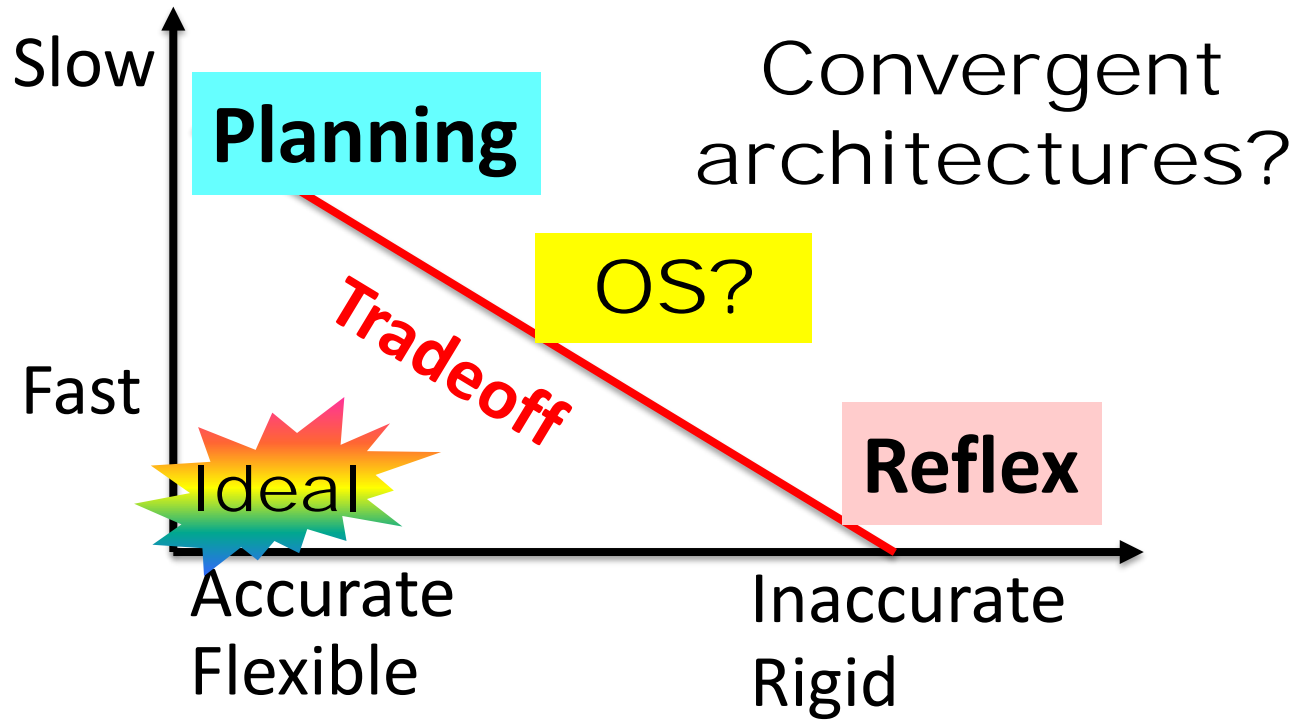
- Erythrocytes (RBC)
- Platelets
- Eye lens fibers
- Skin periphery

Micro-wasps

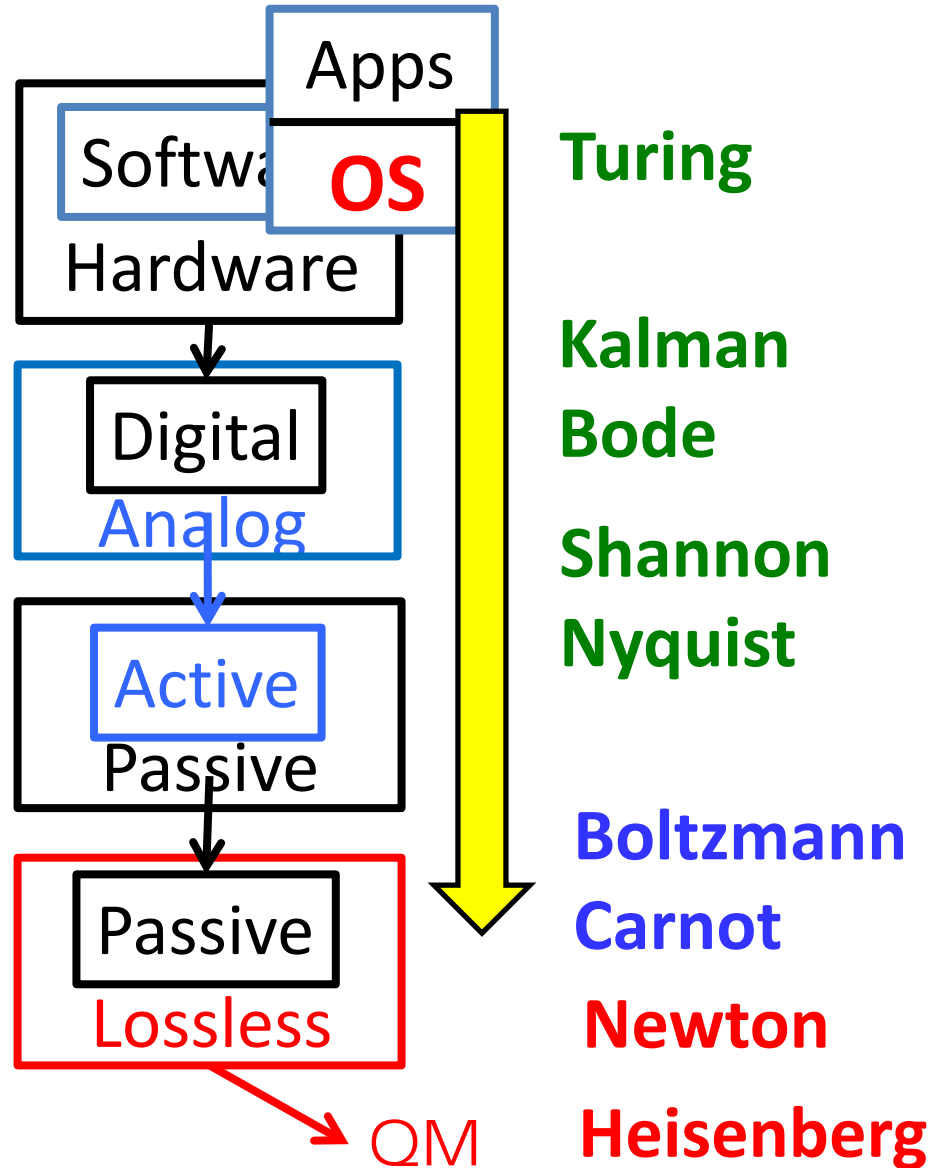
- Neurons

Plants

- Sieve tubes of phloem

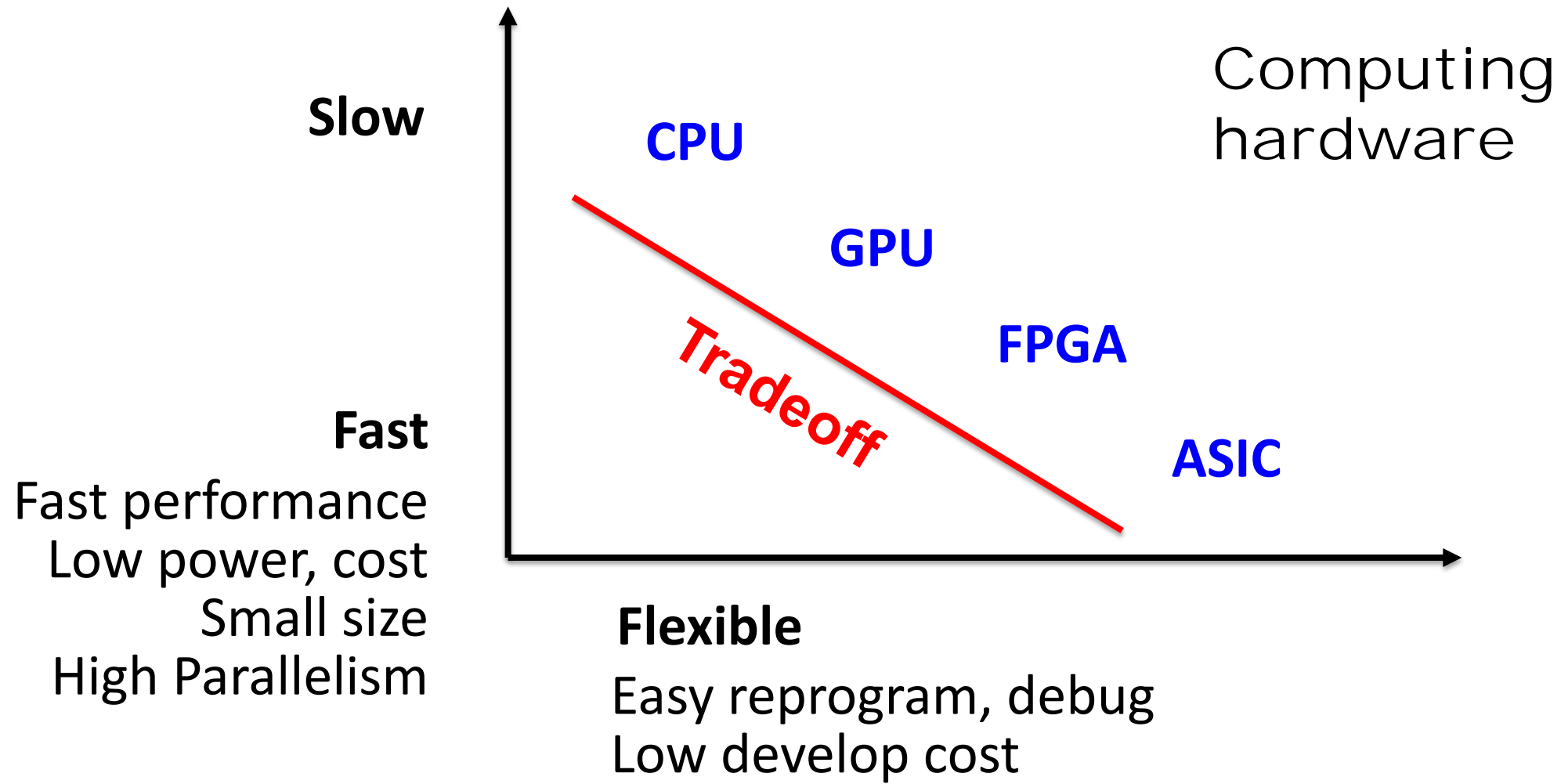


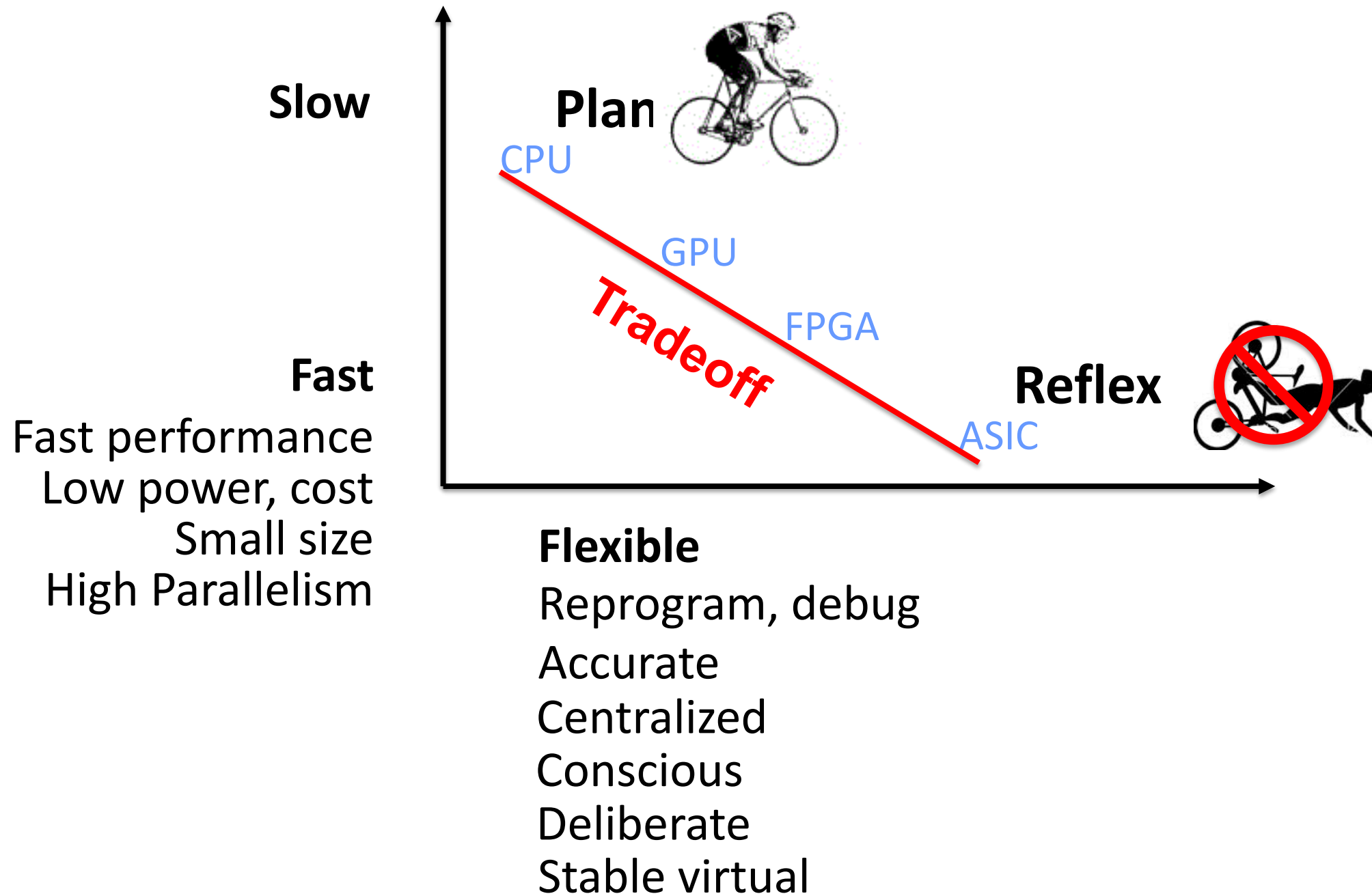
Virtualization education

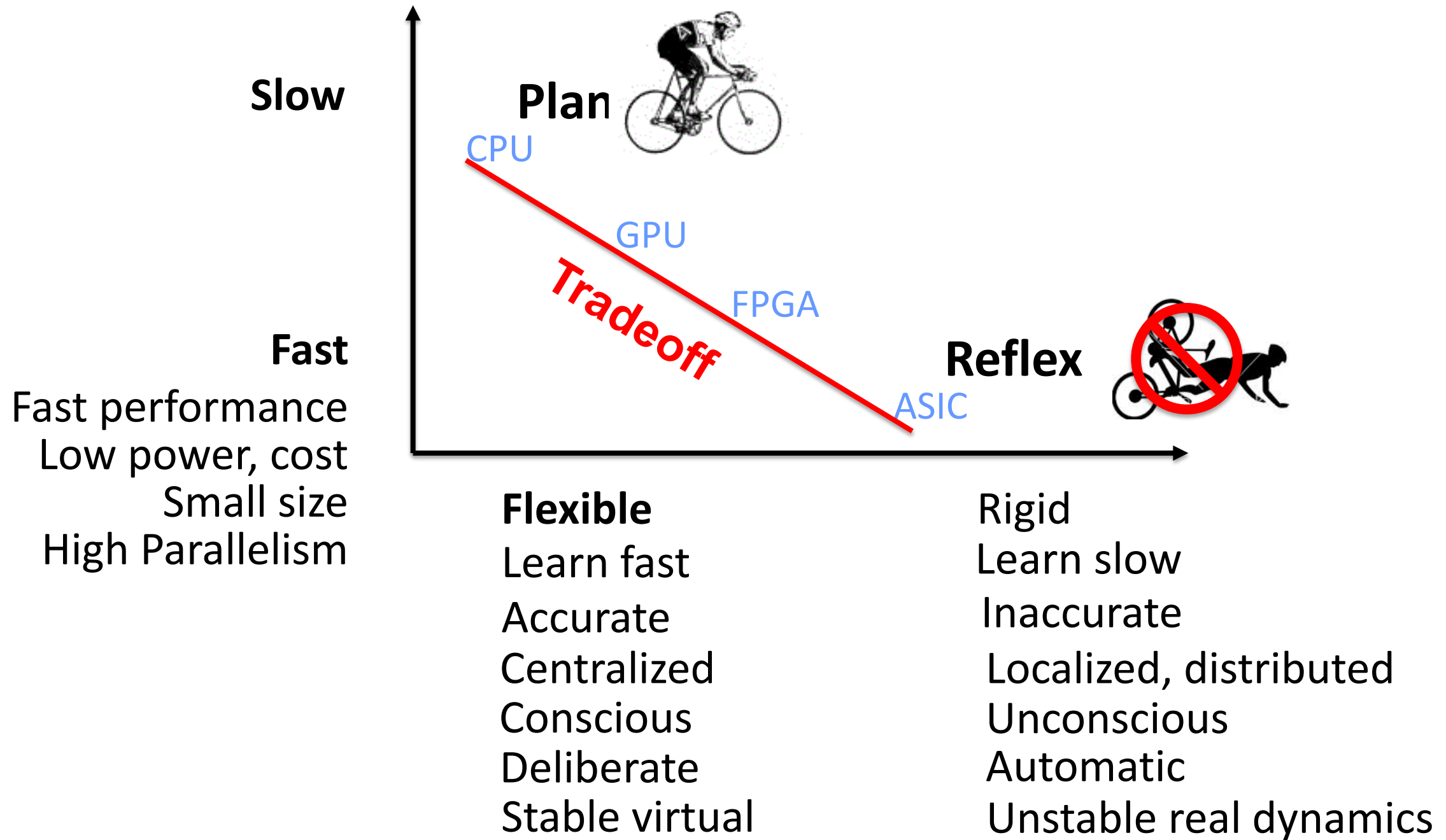


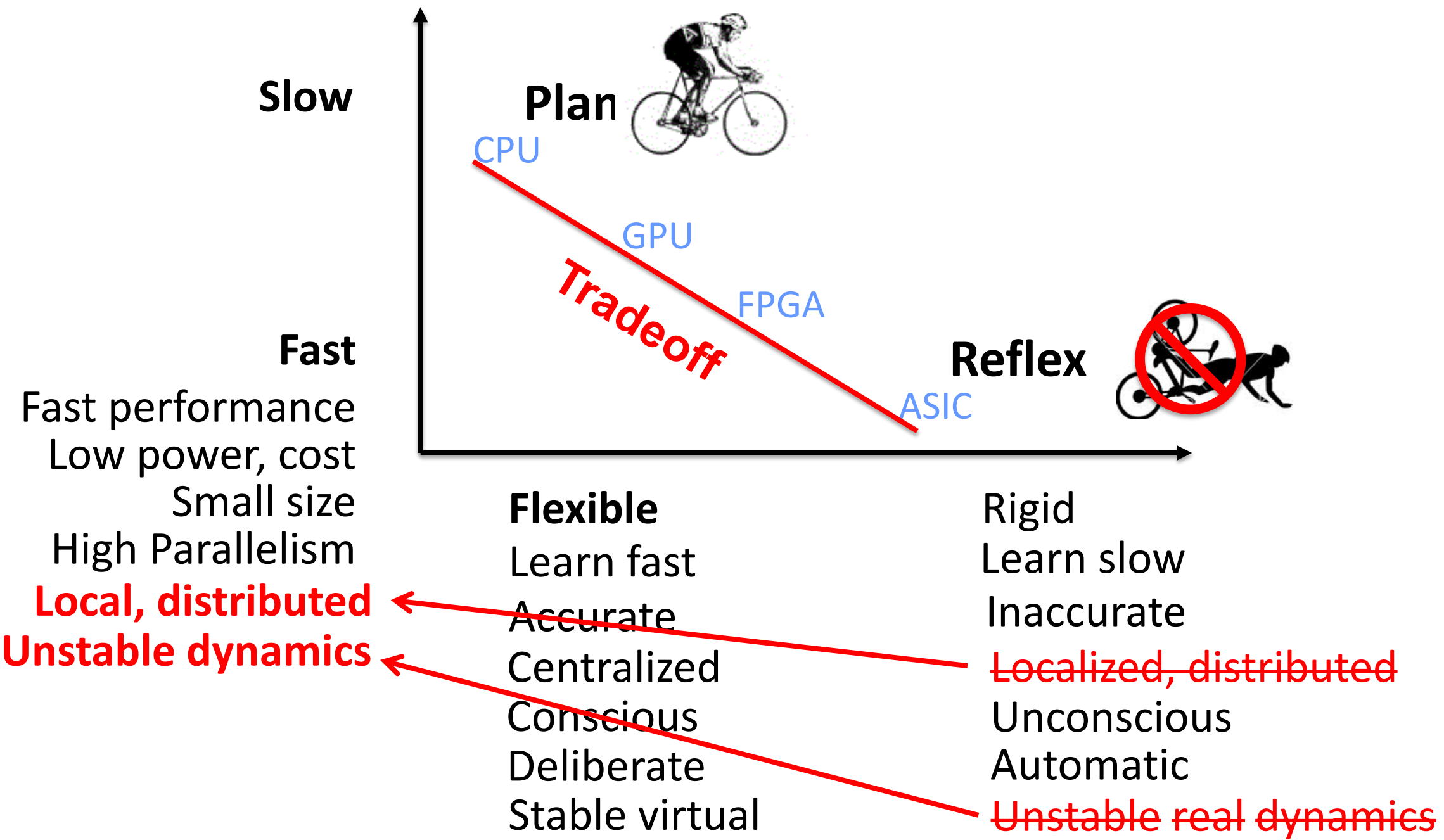
Math Abstract

- Start with Turing
- A lot has already been done
- A few gaps near the bottom
- Have time domain versions of Bode and extensions
- Have redo of stat mech: lossless to passive
- Have classical version of Heisenberg using Kalman
- Need more work on passive to active



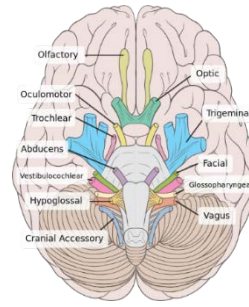






Slow

Plan



OS?

Tradeoff

Reflex



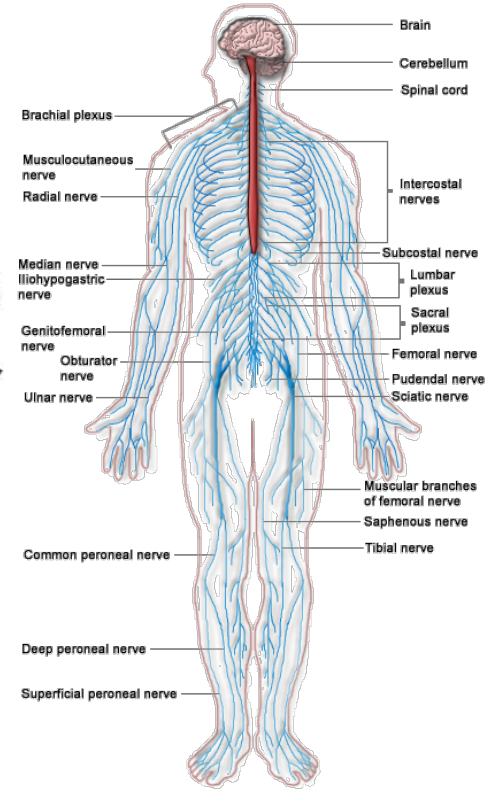
Fast

Fast performance
Low power, cost
Small size
High Parallelism
Local, distributed
Unstable dynamics

Flexible

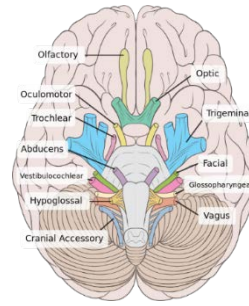
Learn fast
Accurate
Conscious
Deliberate
Centralized
Stable virtual

Rigid
Learn slow
Inaccurate
Unconscious
Automatic



Slow

Plan



Fast

Fast performance
Low power, cost
Small size
High Parallelism
Local, distributed
Unstable dynamics

Tradeoff

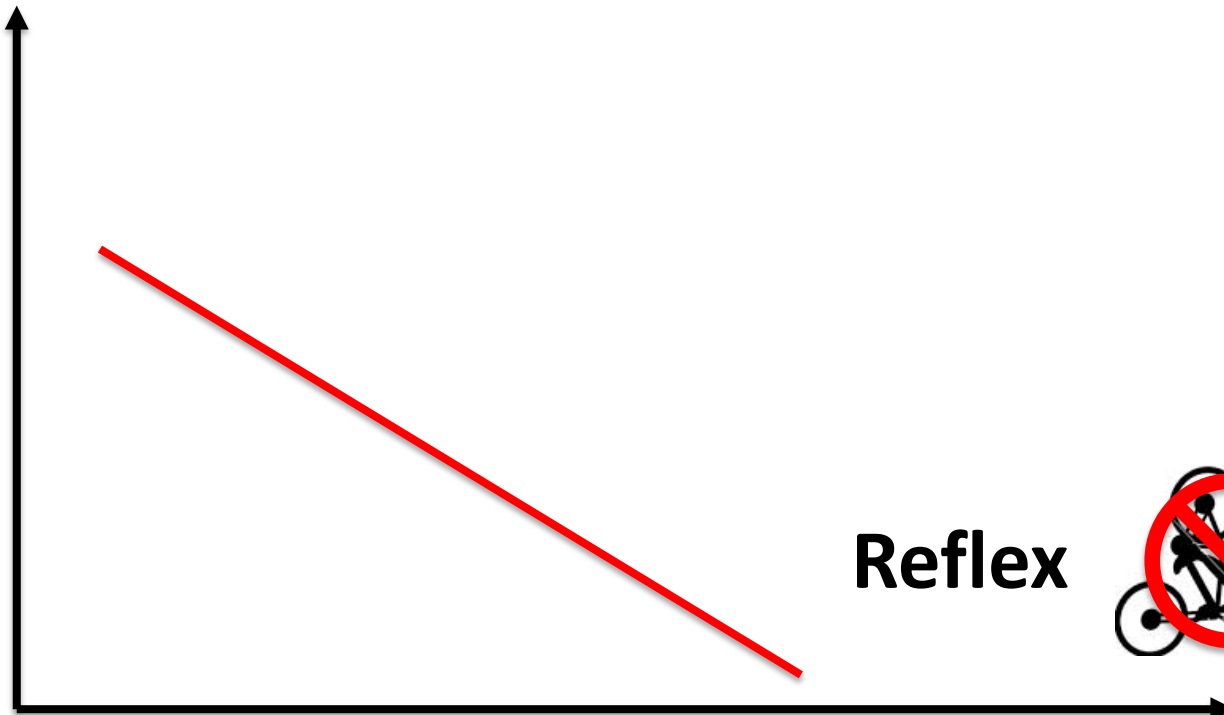
Flexible

Learn fast
Accurate
Conscious
Deliberate
Centralized
Stable virtual

Slow

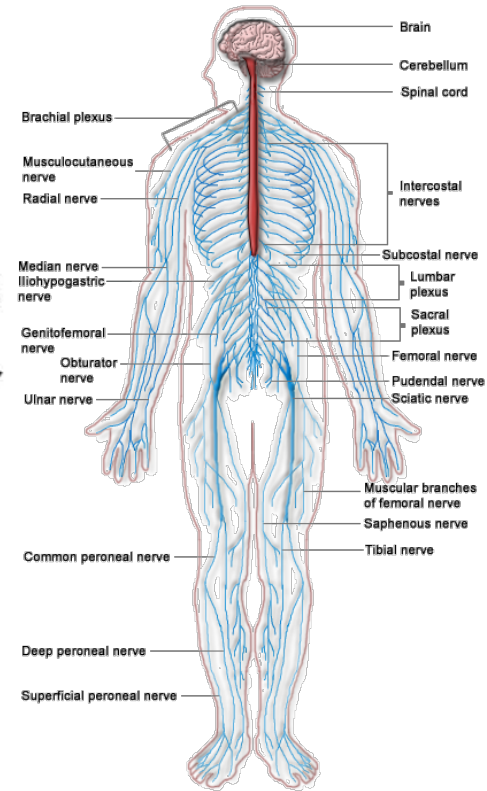
Fast

Fast performance
Low power, cost
Small size
High Parallelism
Local, distributed
Unstable dynamics



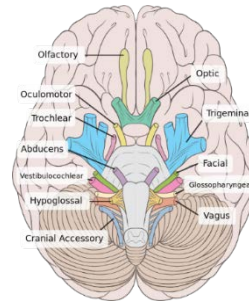
Reflex

Rigid
Learn slow
Inaccurate
Unconscious
Automatic



Slow

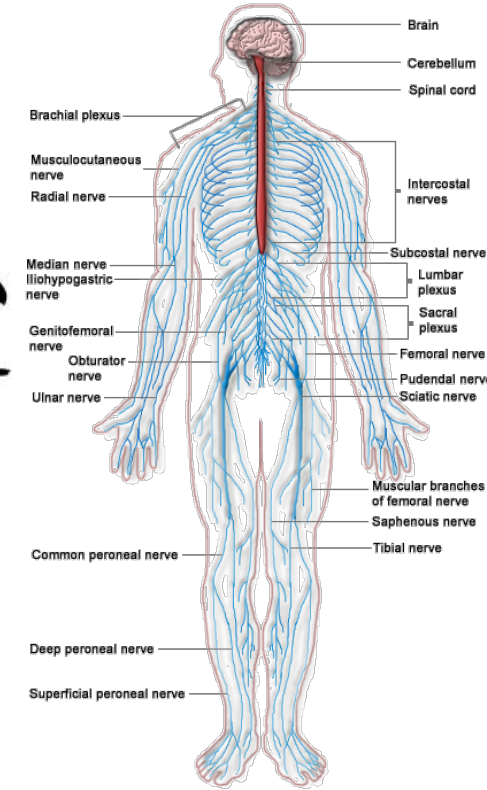
Plan



OS?

Tradeoff

Reflex



Fast

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Learn slow
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Slow

Plan

OS?

Fast

Reflex

Tradeoff

Fast performance
Low power, cost
Small size
High Parallelism

Flexible

Learn fast
Accurate
Conscious

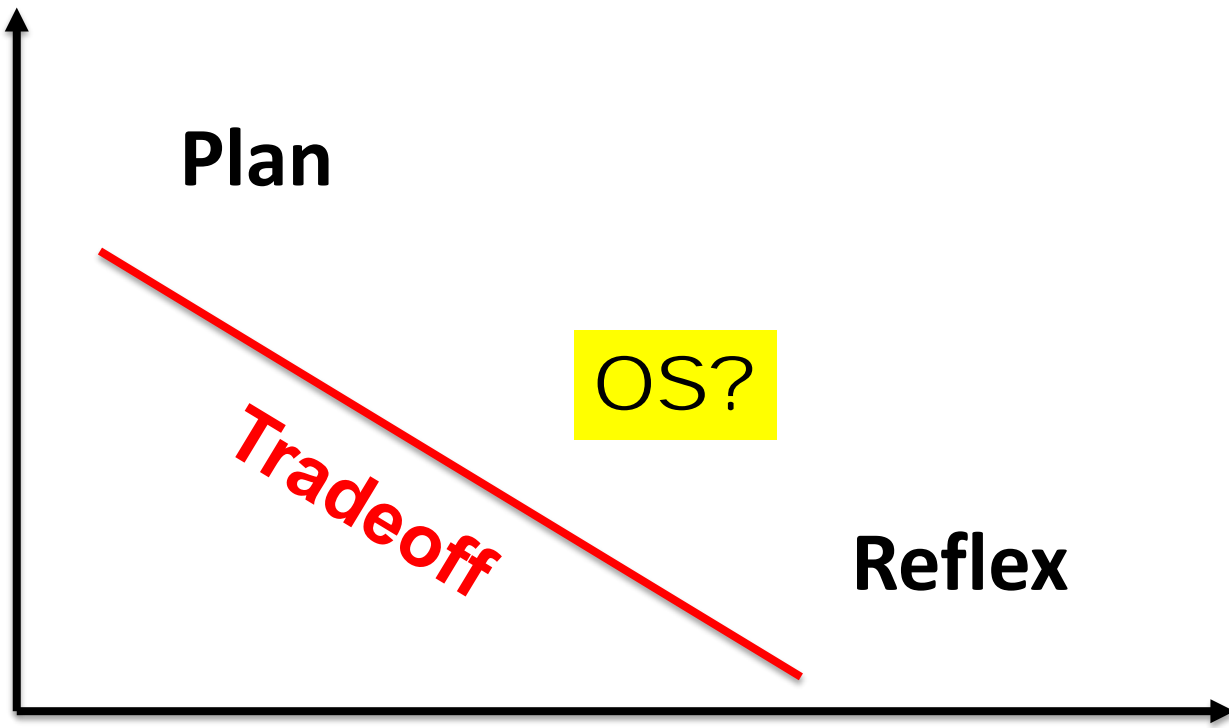
Deliberate

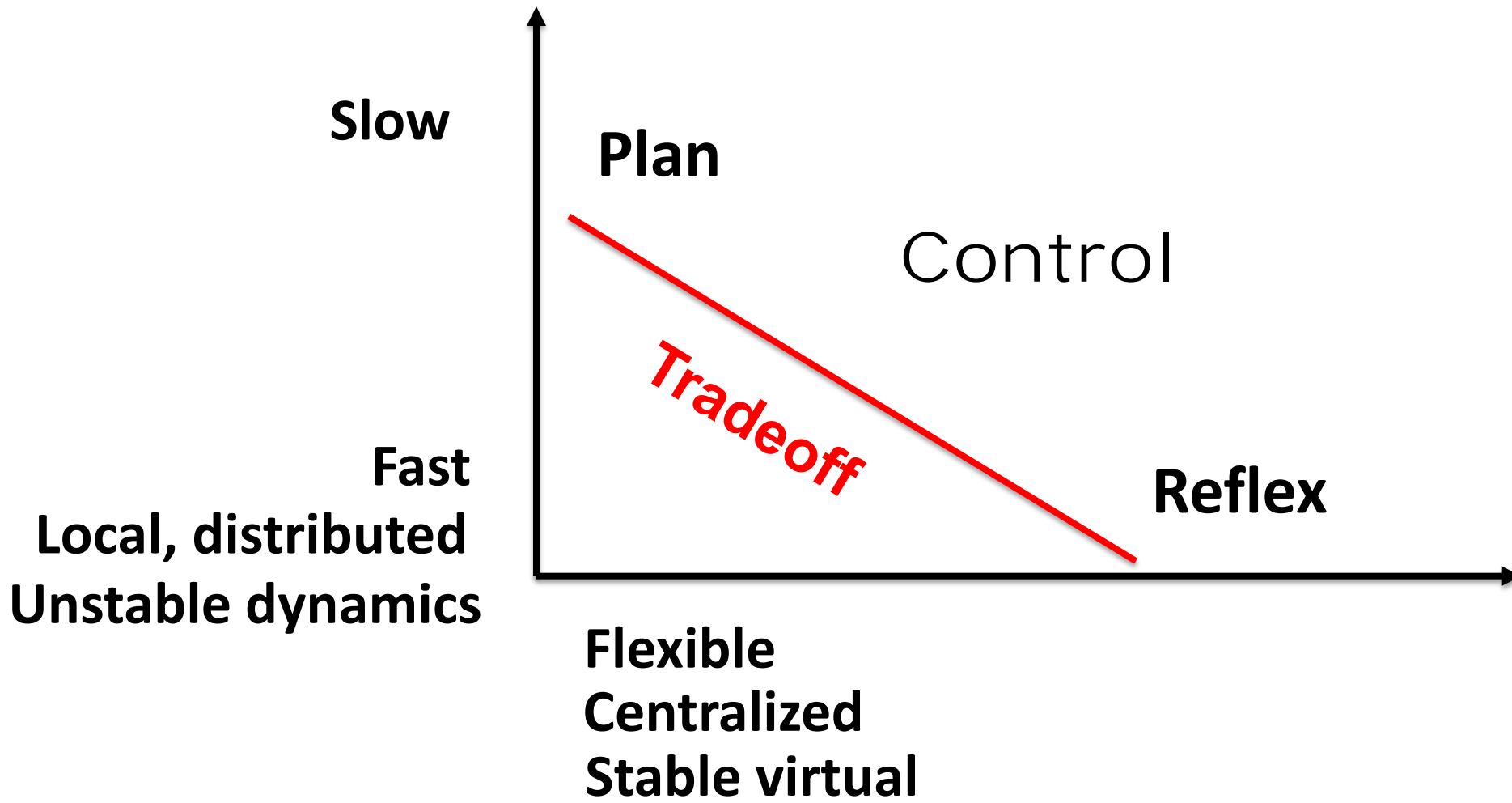
Centralized

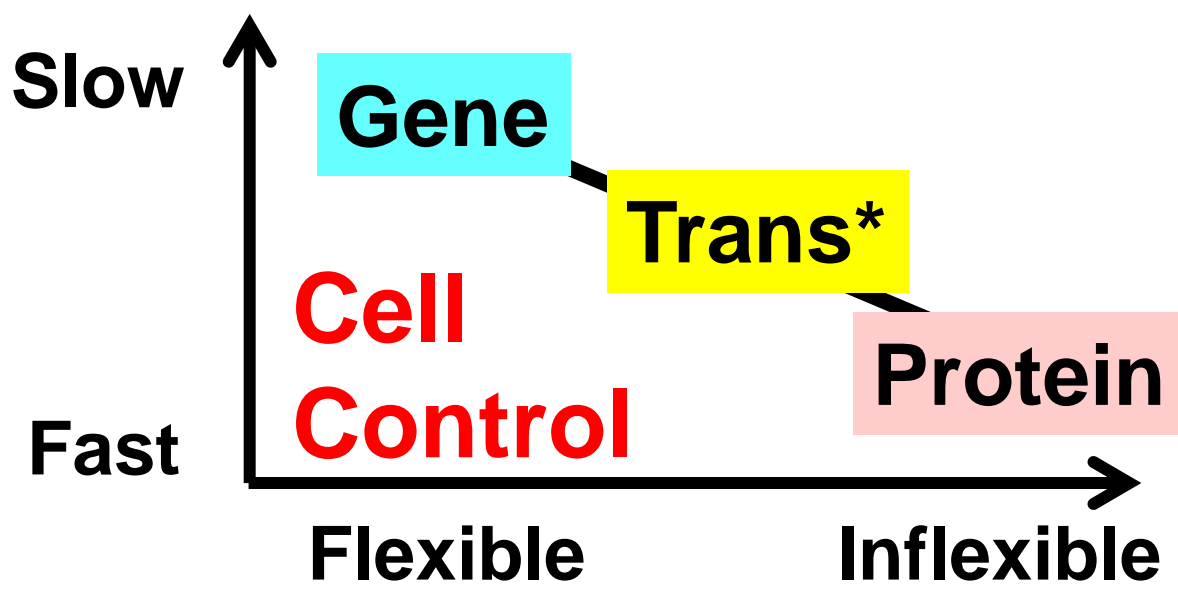
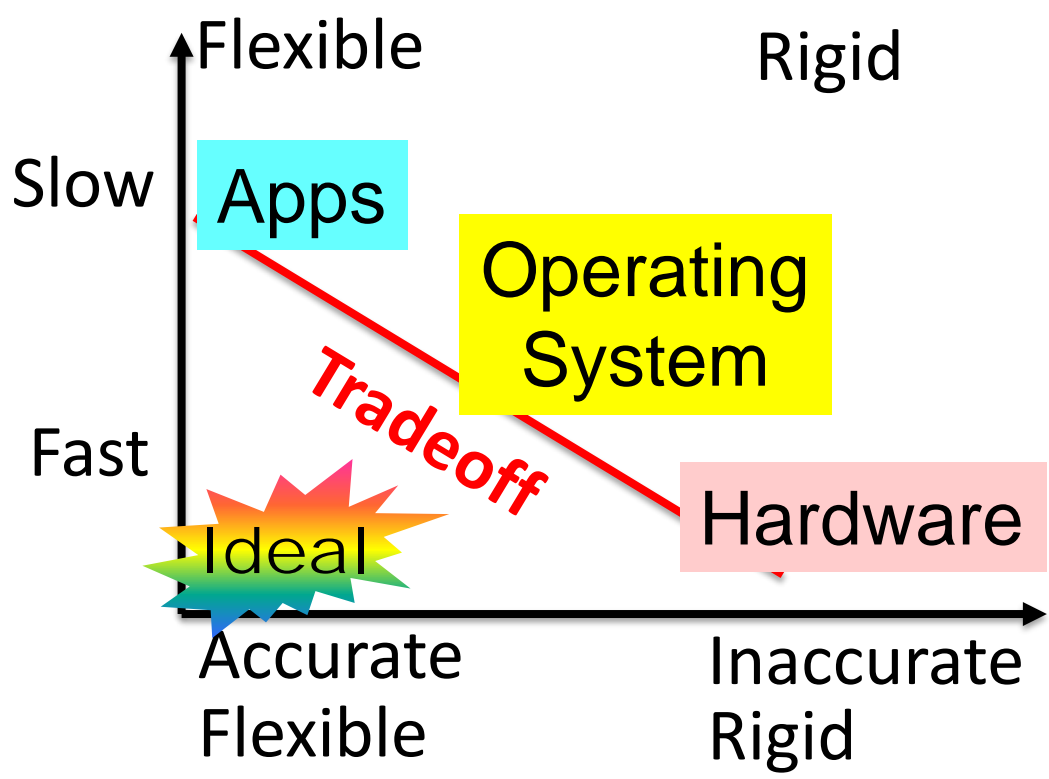
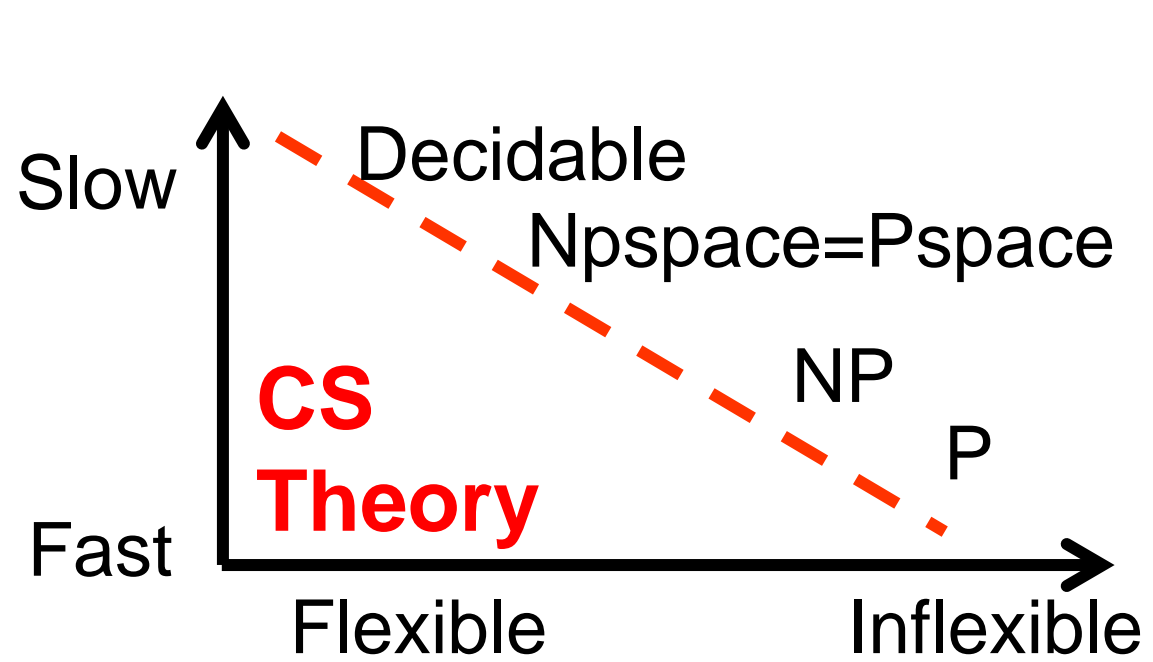
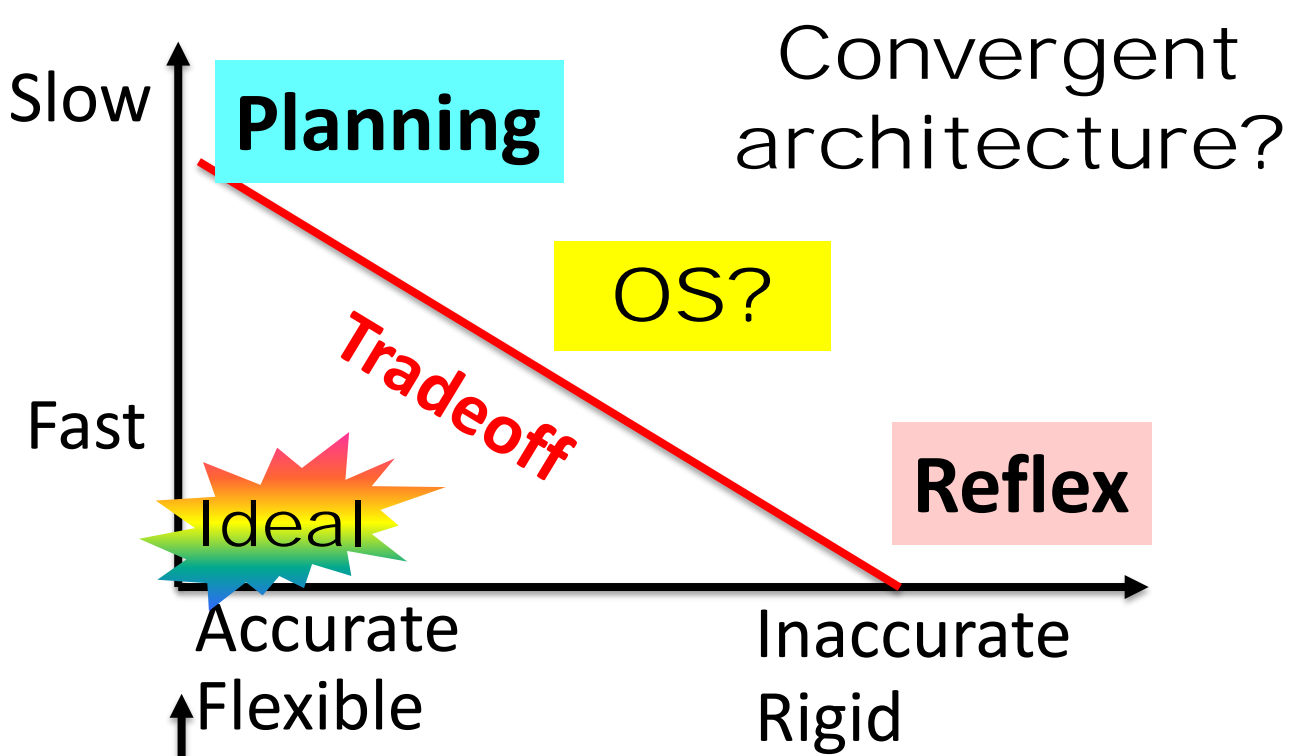
Stable virtual

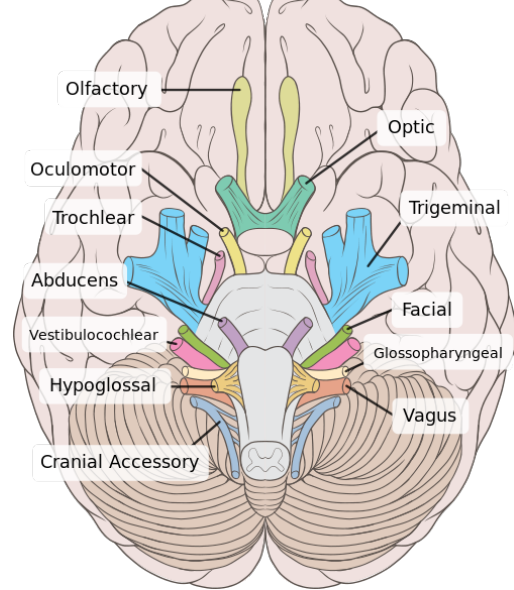
Local, distributed

Unstable dynamics

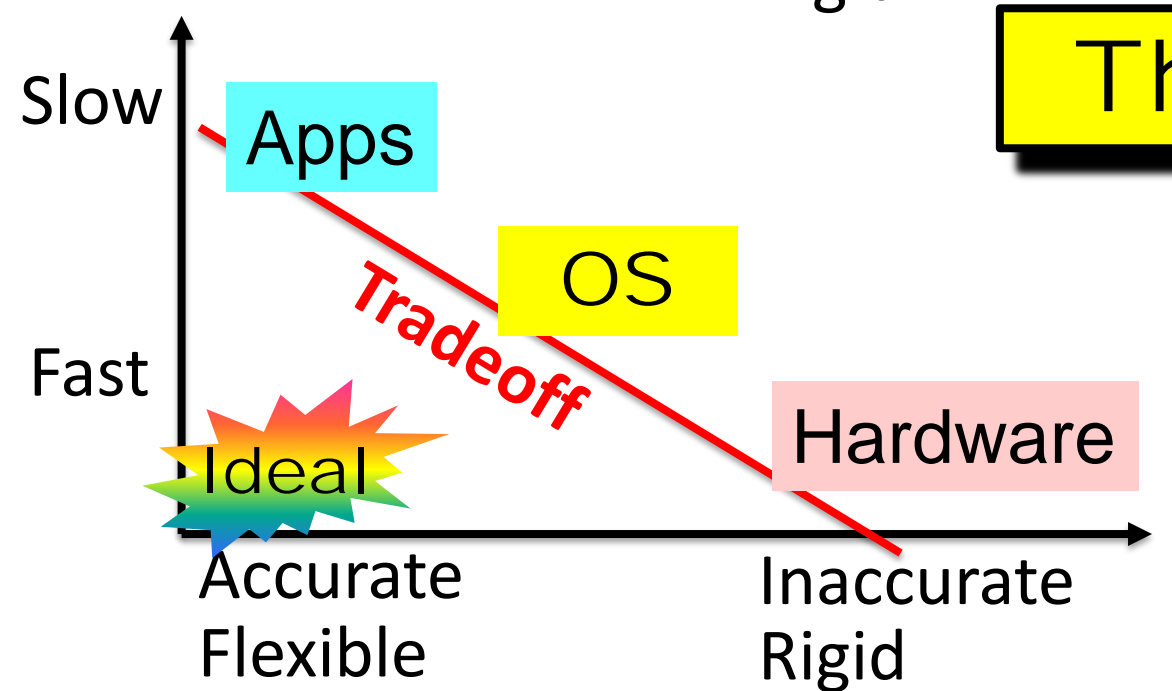




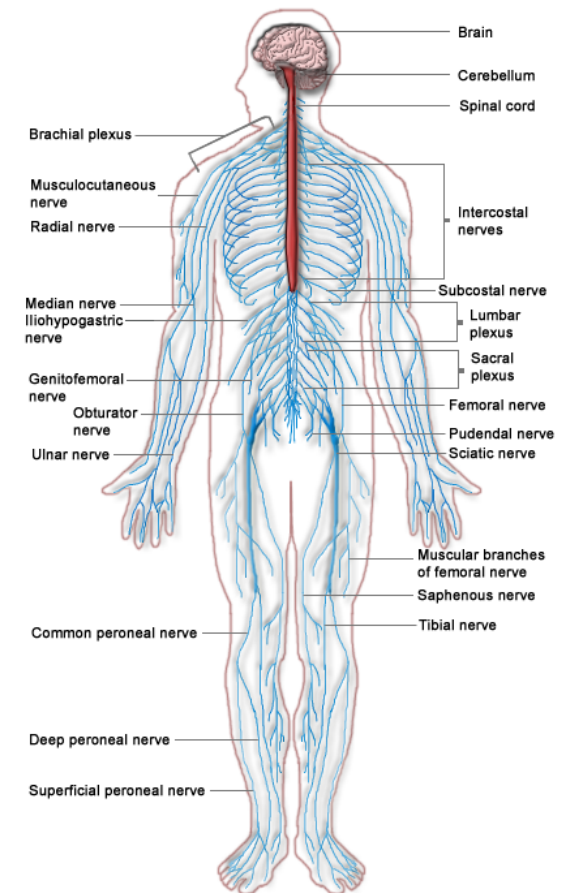




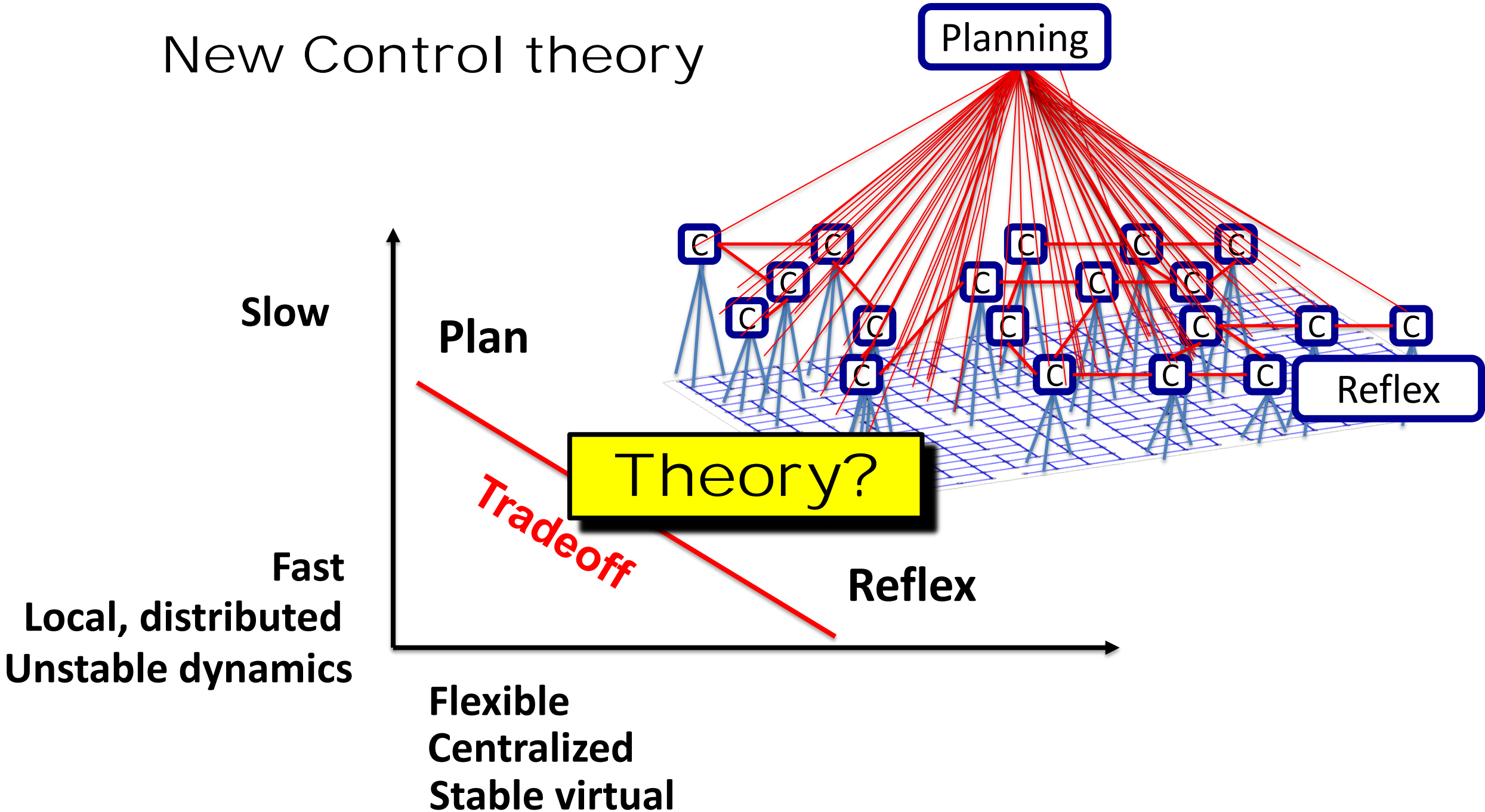
Convergent architecture?



Theory?

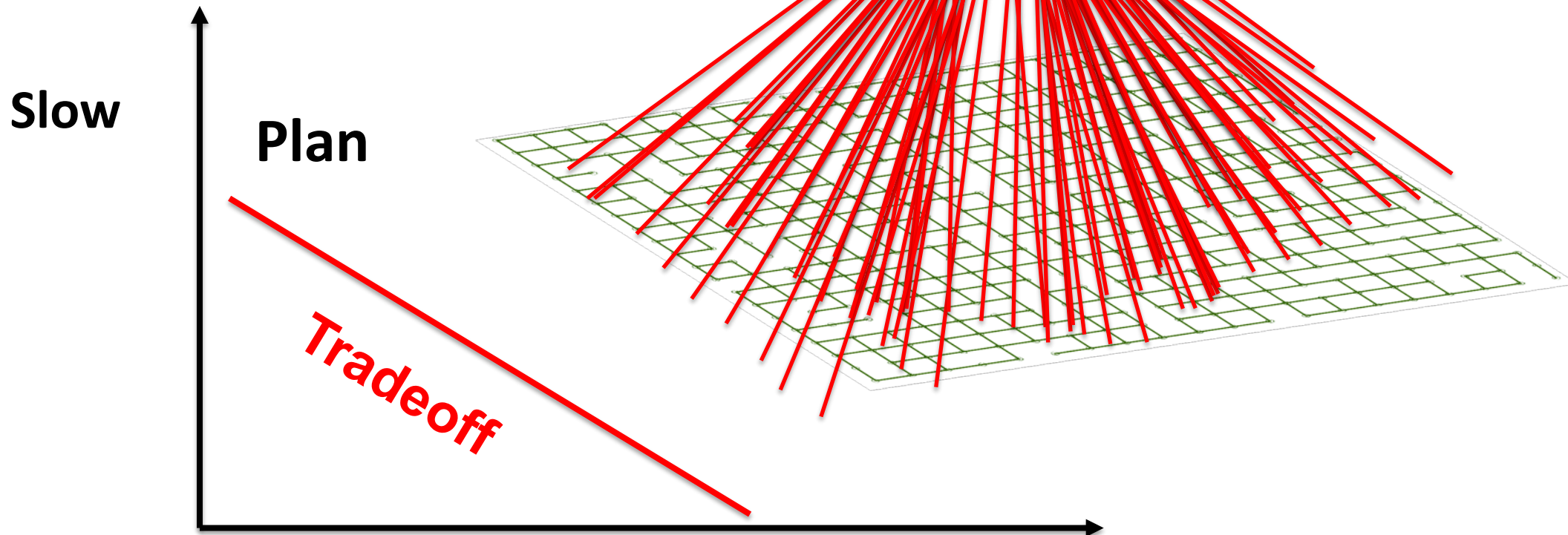


New Control theory



Control

Controller



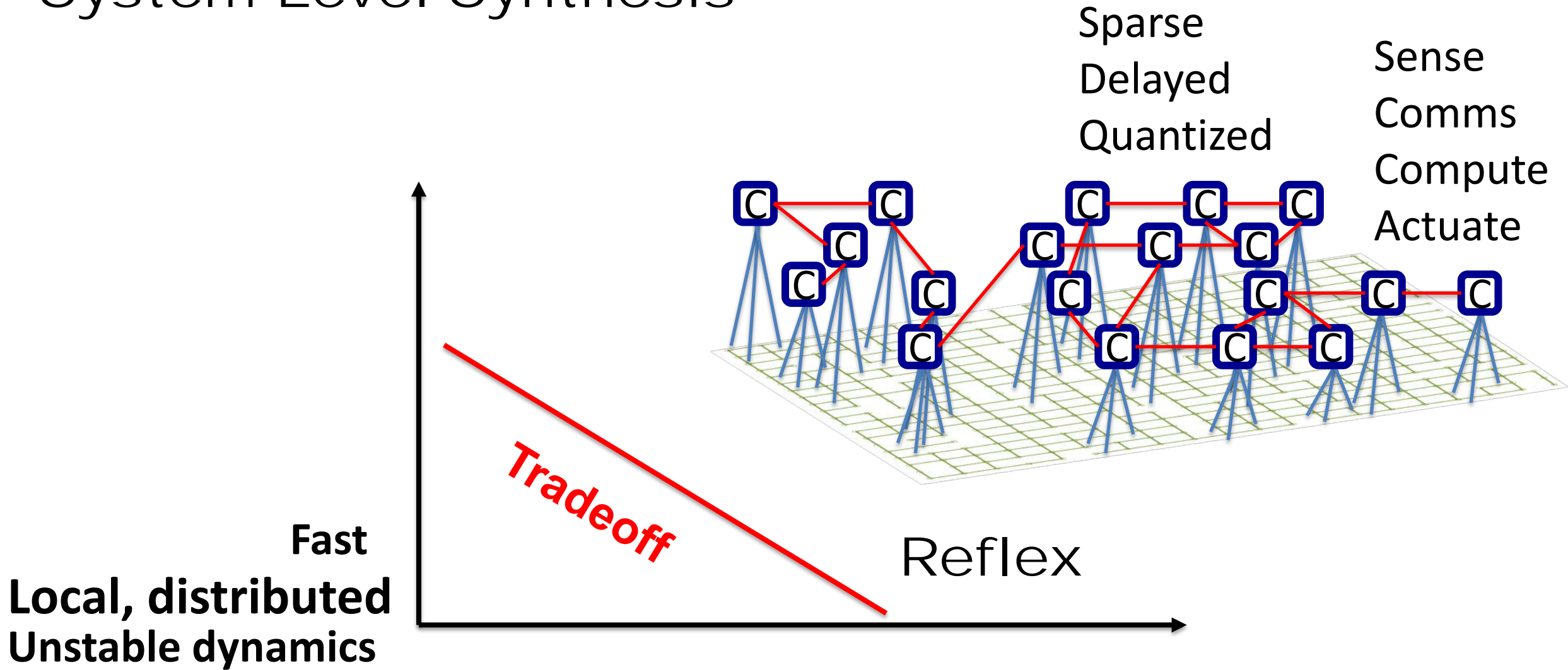
Slow

Plan

Tradeoff

Flexible
Centralized
Stable virtual

System Level Synthesis



System
Level

Synthesis

Wang and Matni

Slow

Plan

Layered

Sparse

Delayed

Quantized

Sense

Comms

Compute

Act

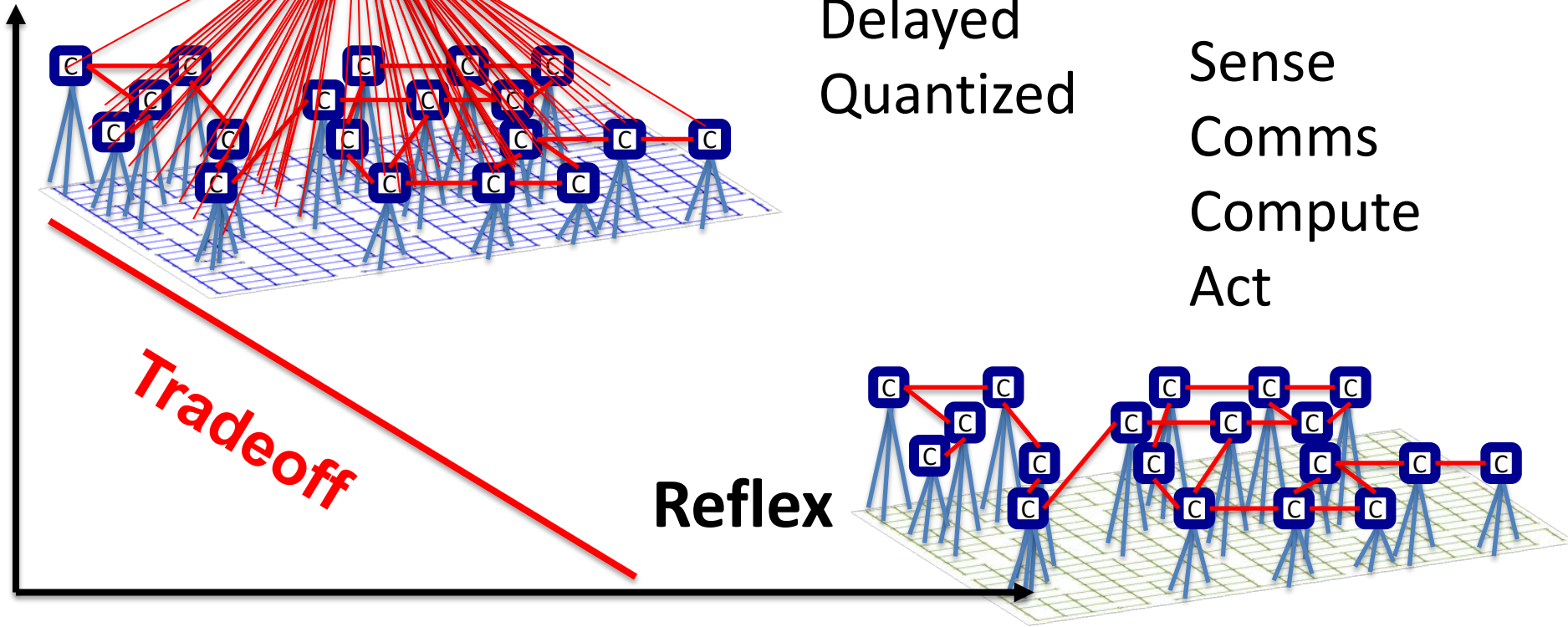
Tradeoff

Fast

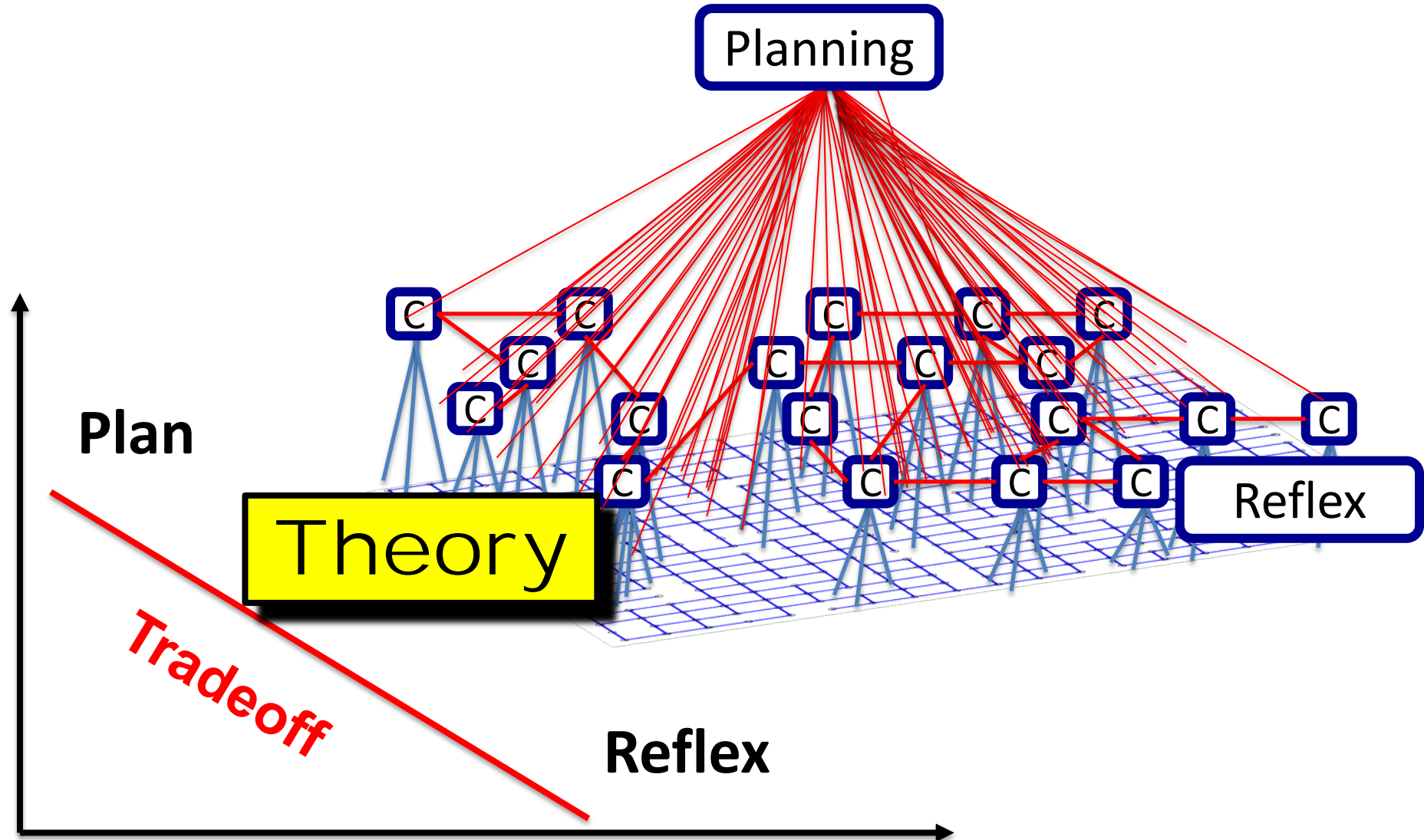
Reflex

Local, distributed
Unstable dynamics

Flexible
Centralized
Stable virtual



System
Level
Synthesis
Wang and Matni



Slow

Plan

Theory

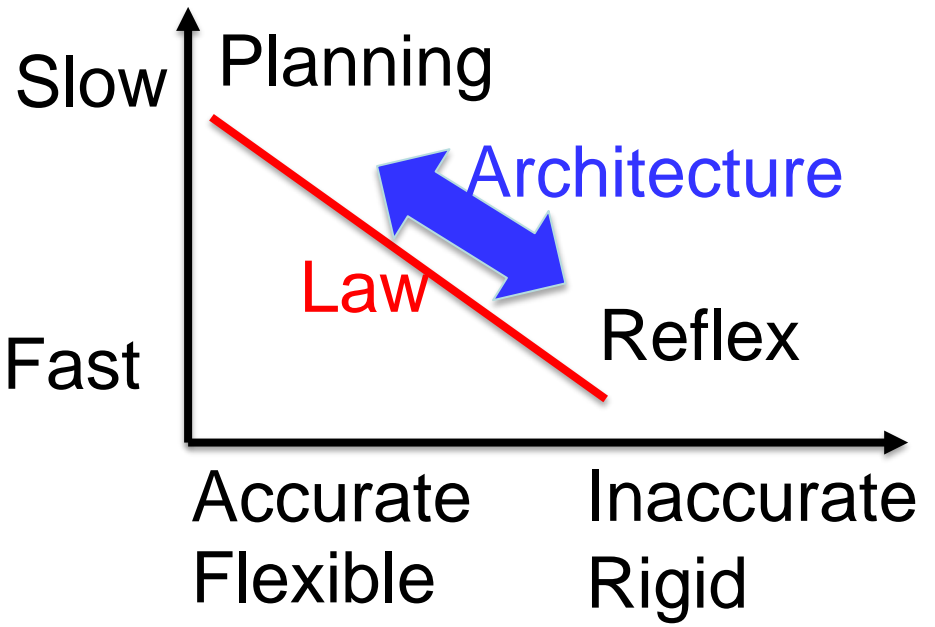
Reflex

Fast

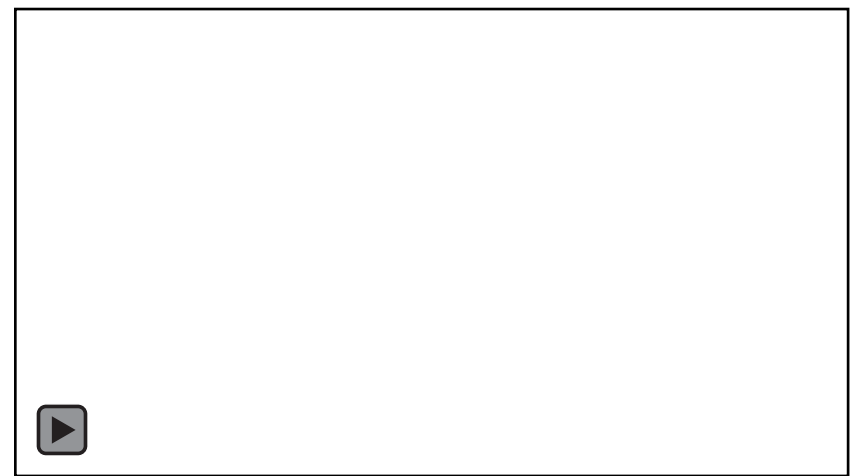
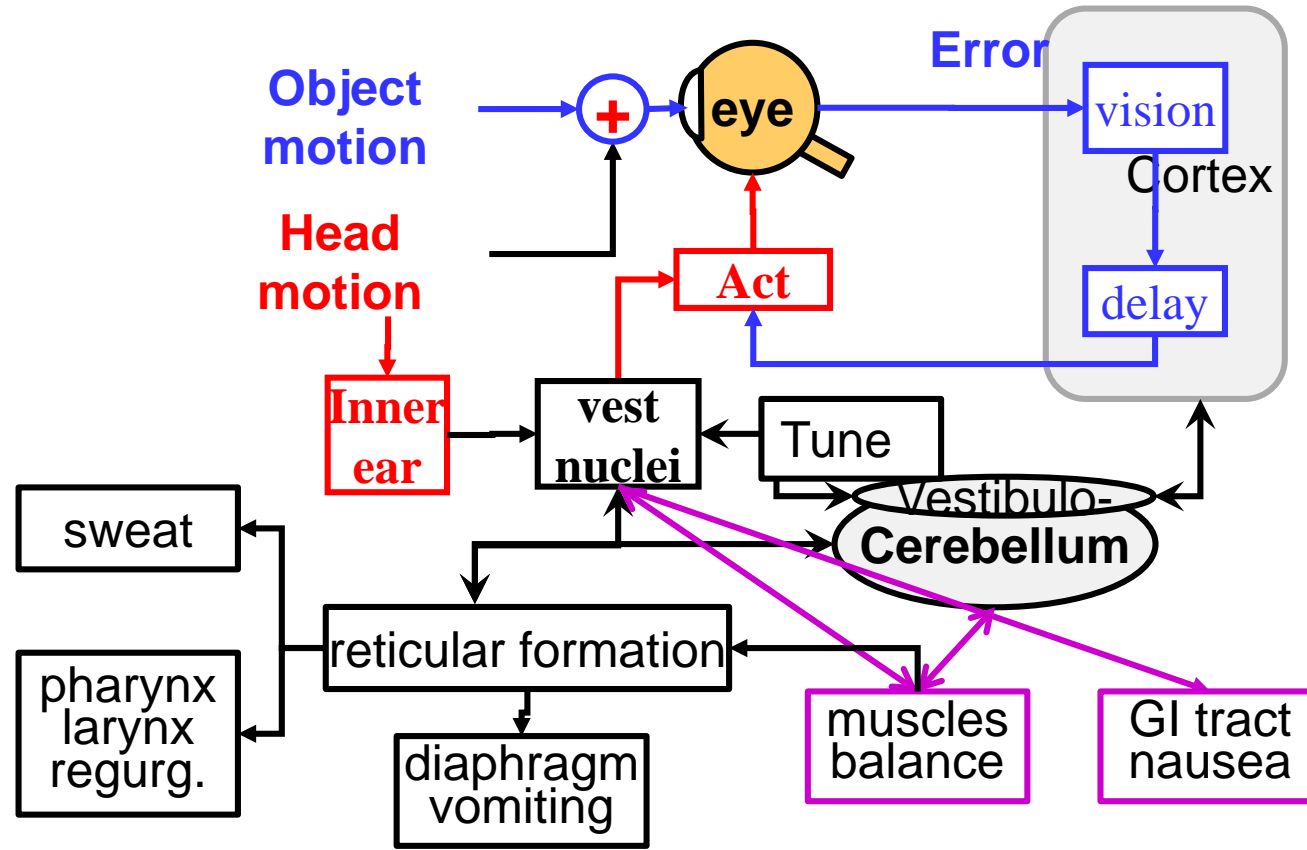
Reflex

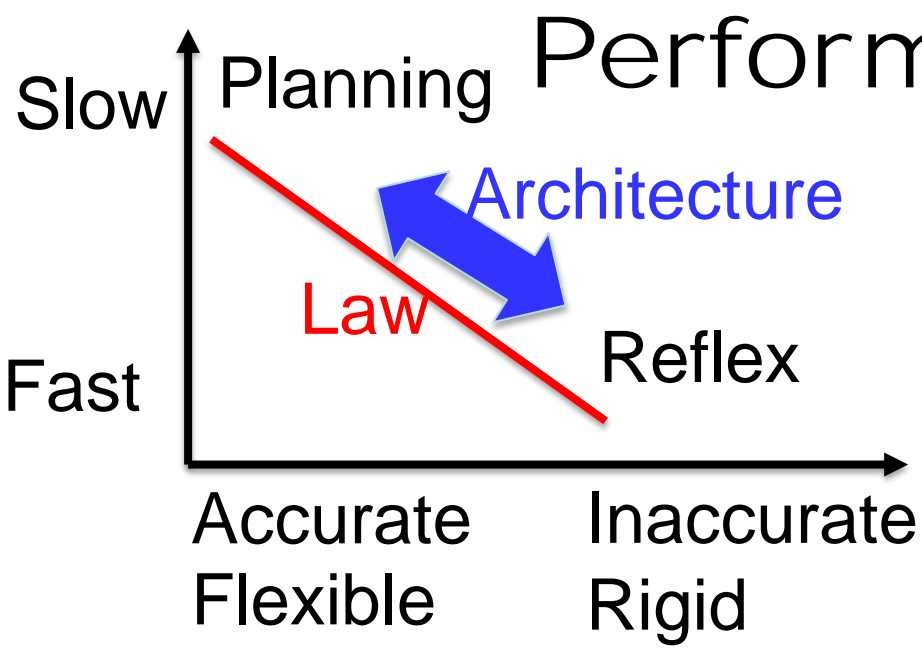
Local, distributed
Unstable dynamics

Flexible
Centralized
Stable virtual

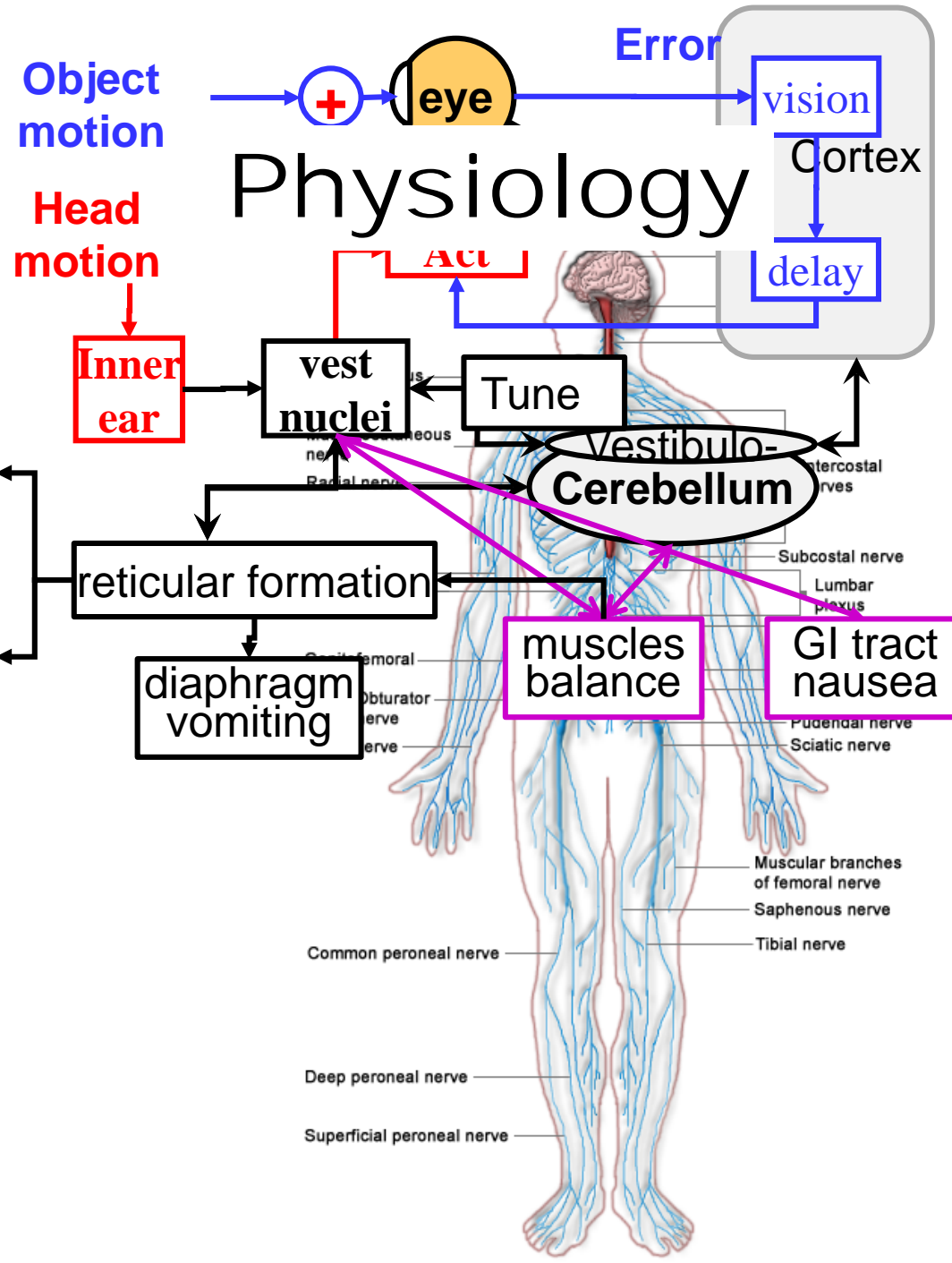
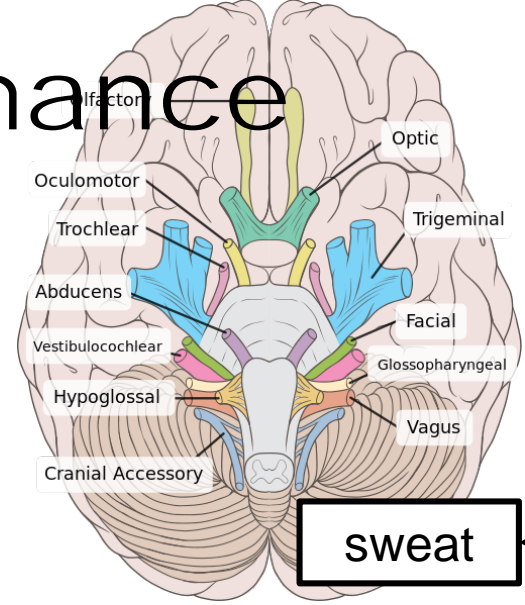


Planning
Balance
Reflex
Motion sickness



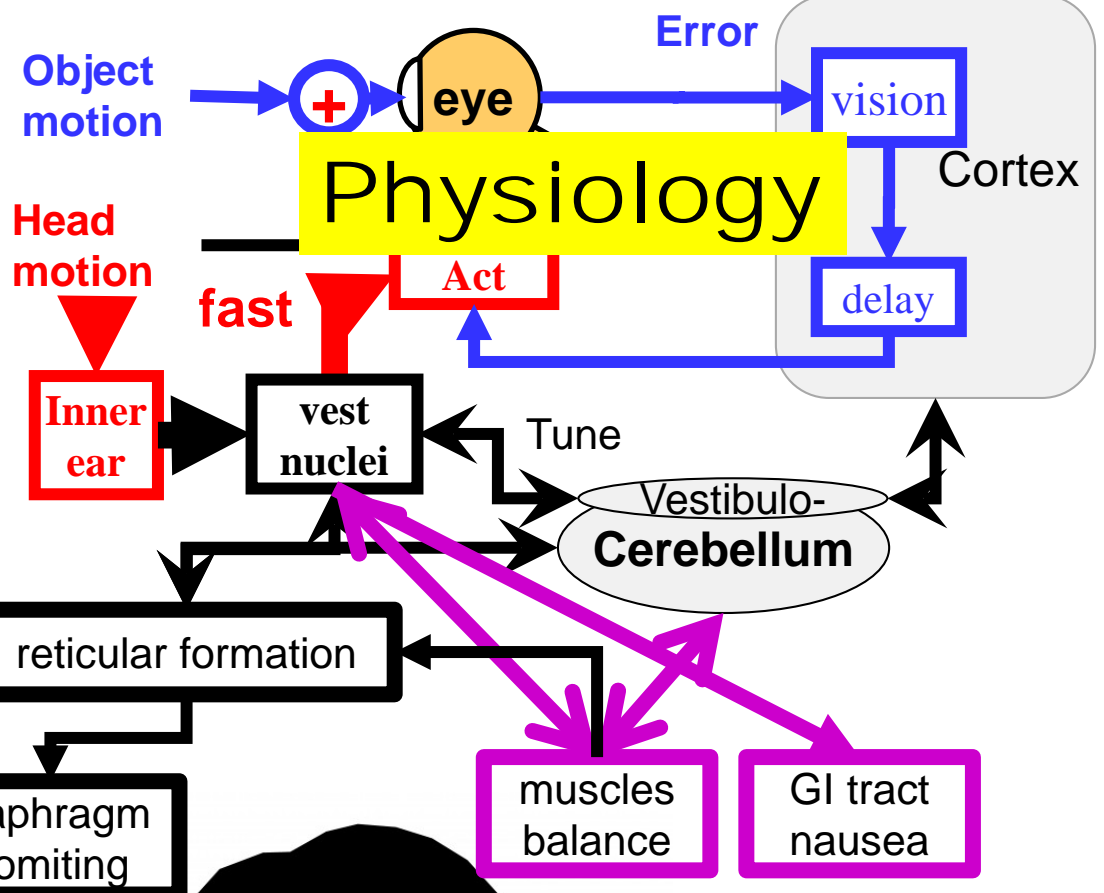


Planning
Balance
Reflex
Motion sickness



Performance

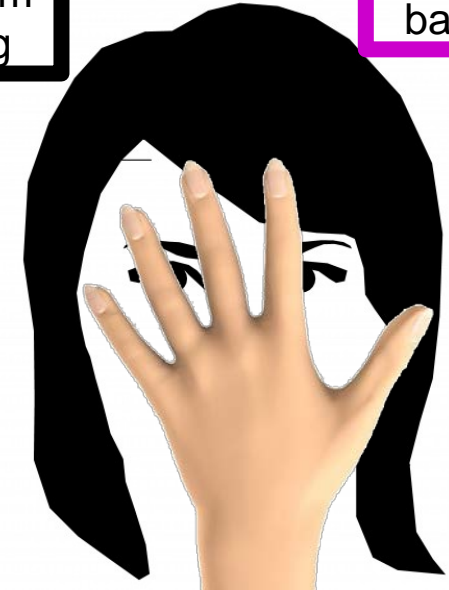
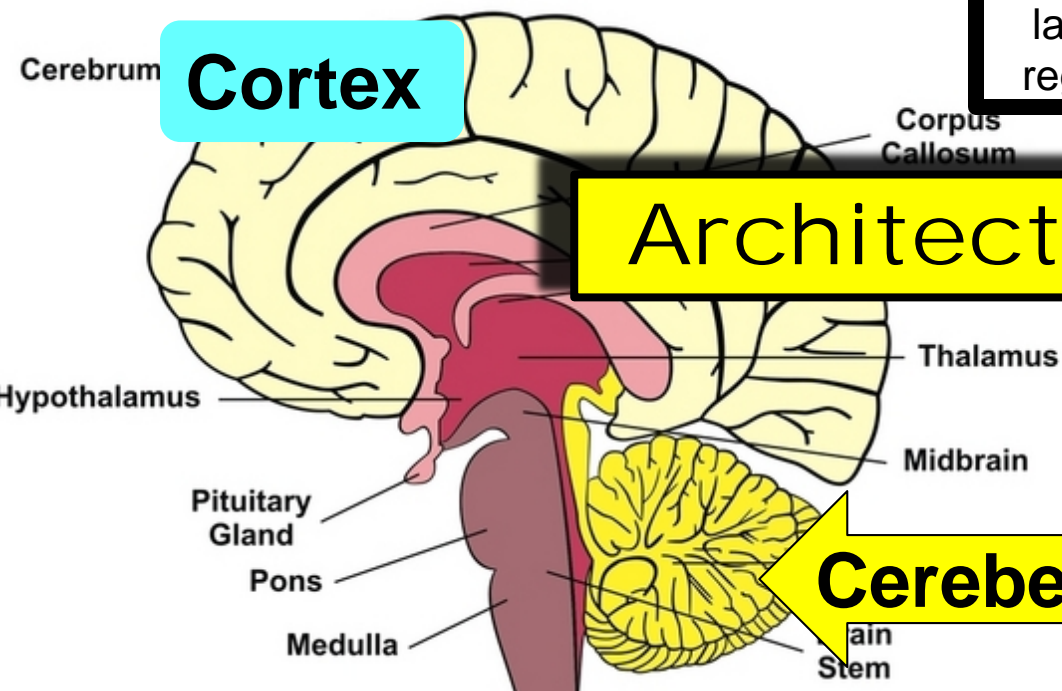
Vision, VOR
(reflex), balance,
motion sickness



Cortex

Architecture

Cerebellum



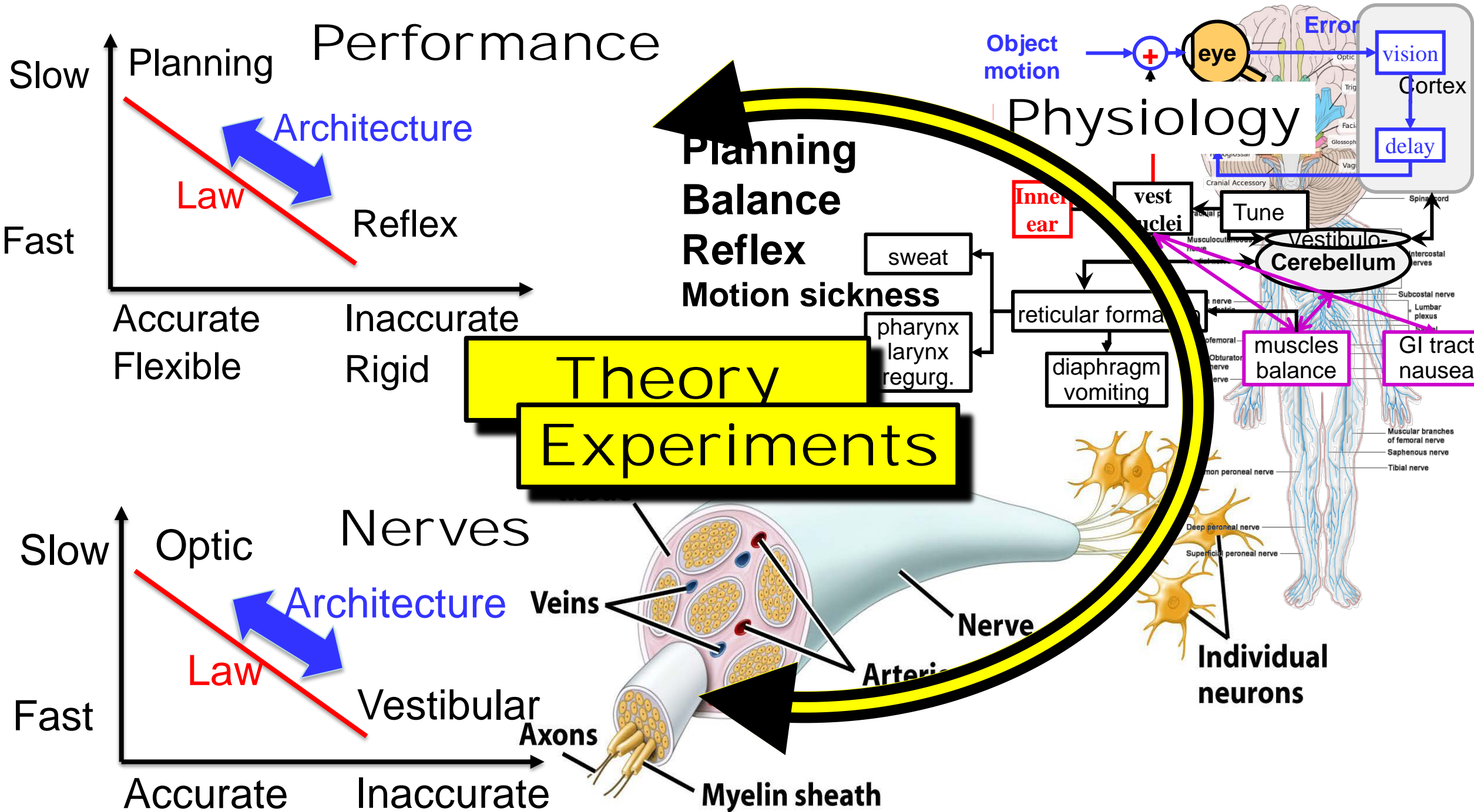
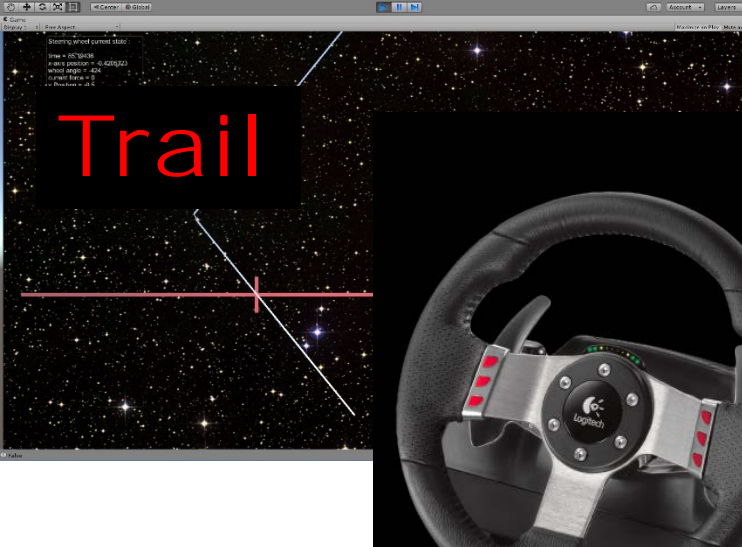


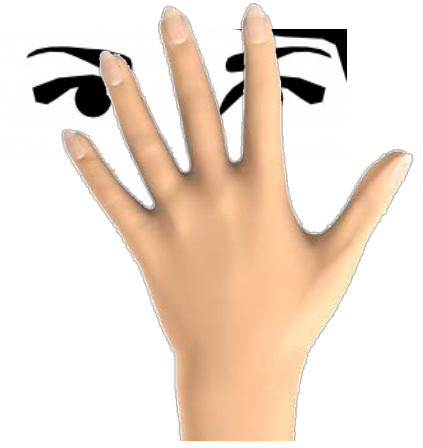
Figure 25-1b Discover Biology 3/e



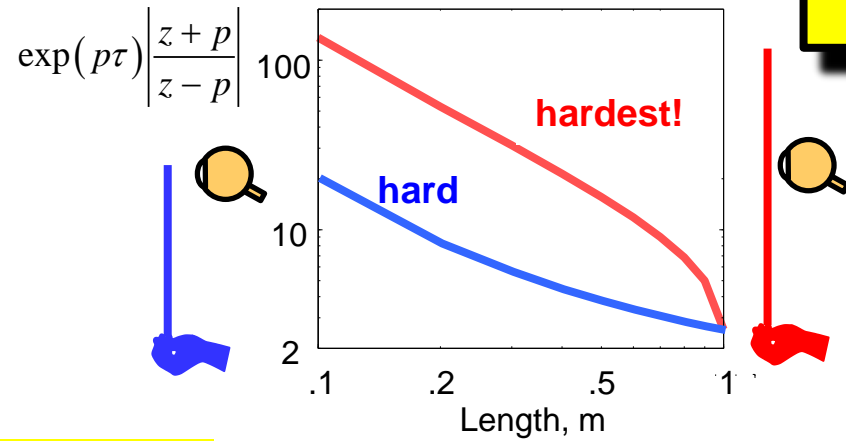
Bumps

Object motion

Slow

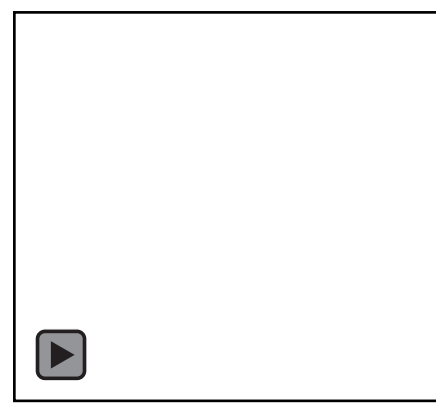


Experiments



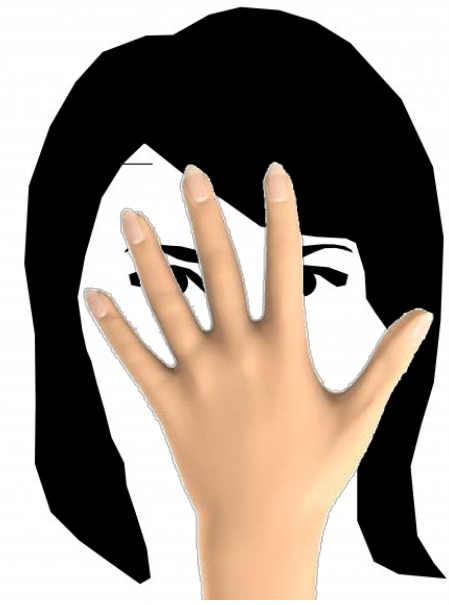
Waterbed

$$\left. \exp\left(\int \ln|T|\right) \right\|T\|_{\infty} \geq \exp(p\tau) \frac{z+p}{z-p}$$



Head motion

Fast



Trail

Theory

Experiments

Object motion

Slow



- Video biking game with trails and bumps
- **Balancing stick (inverted pendulum)**
- Vision and VOR with object and head motion
- Balancing body with vision, vestibular, and proprioception

$\exp(p\tau)$

2
0.1

- Quantitative match with theory (but equipment)
- Qualitative (but easy to do live demos)
- **Both**

$\exp(\int)$

$\|T\|_\infty$

Waterbed

**Easy to read
slow text**

.5 Hz

Note: This doesn't work
in video format, so this
experiment to be done
using .pptx format.

1 Hz

**Easy to read
slow text**

**Hard to read
fast text**

2 Hz

3 Hz

**Hard to read
fast text**

Easy to read
slow text

.5 Hz

1 Hz

Easy to read
slow text

Hard to read
fast text

2 Hz

3 Hz

Hard to read
fast text



Shake your
head "no" as
fast as you can

Easy to read
slow text

.5 Hz

1 Hz

Easy to read
slow text

Hard to read
fast text

2 Hz

3 Hz

Hard to read
fast text



Shake your
head "no" as
fast as you can

Why?

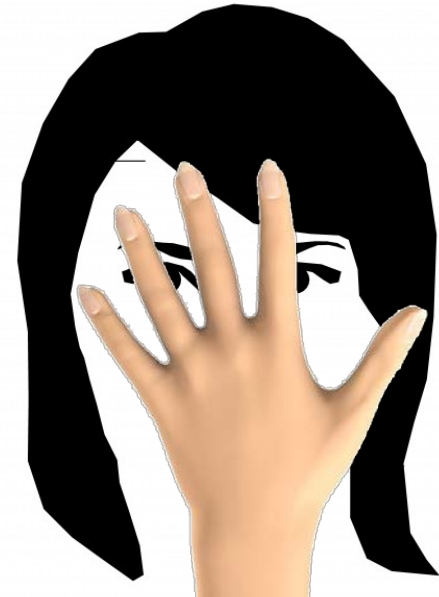


**Object
motion**

Slow

**Head
motion**

Fast



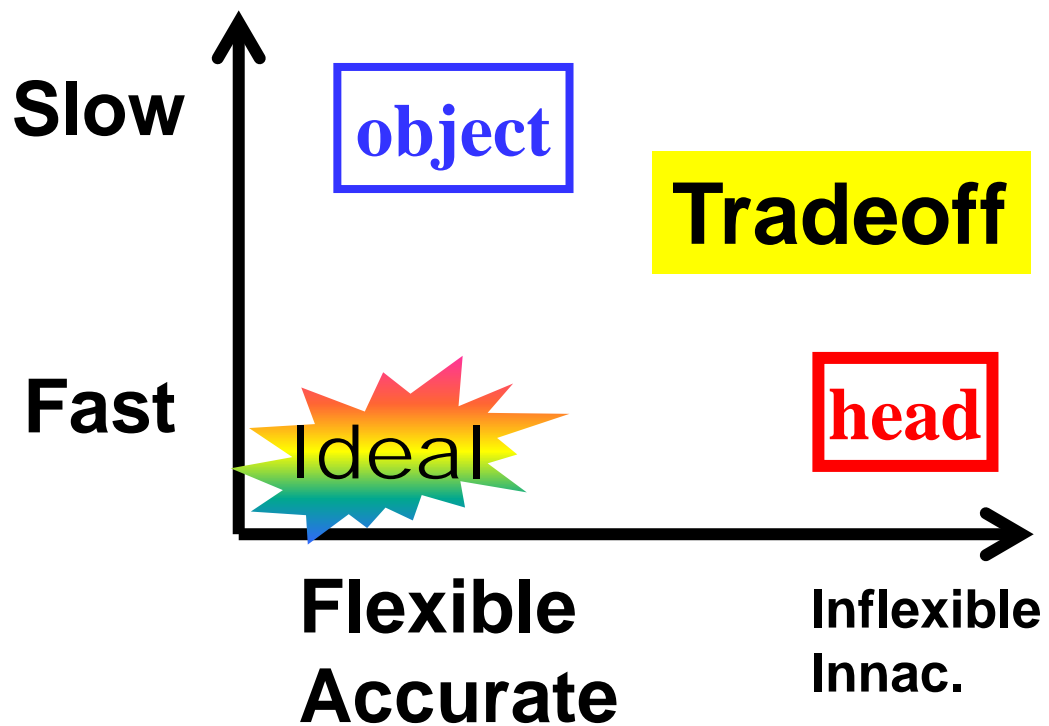
System/envirom behavior
Extreme diversity



**Object
motion**

Slow

Why? How?



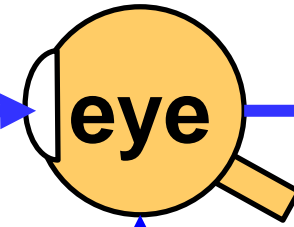
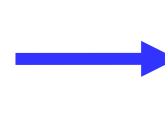
**Head
motion**

Fast





Object motion



Error



Cortex

slow



Slow

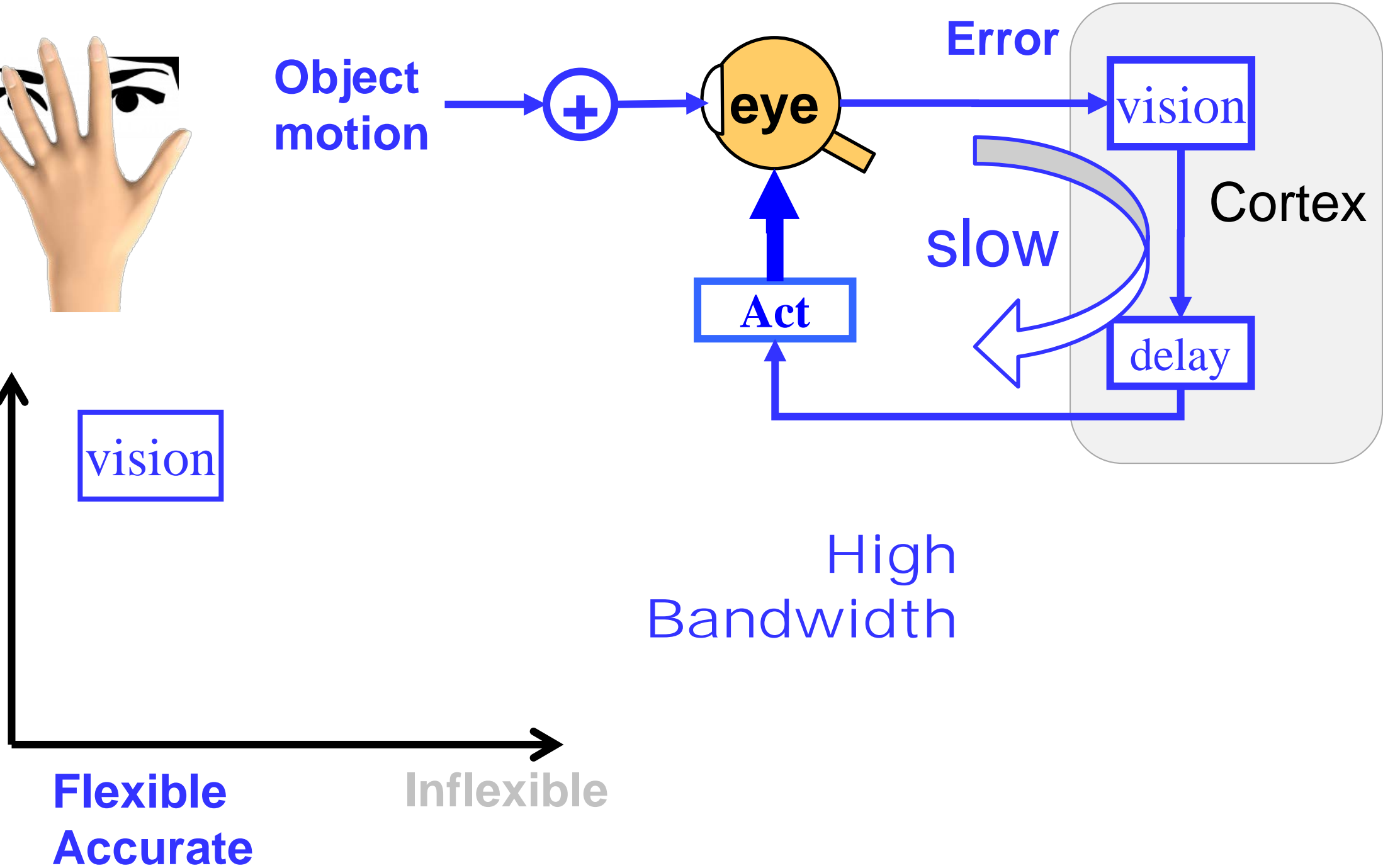


Fast

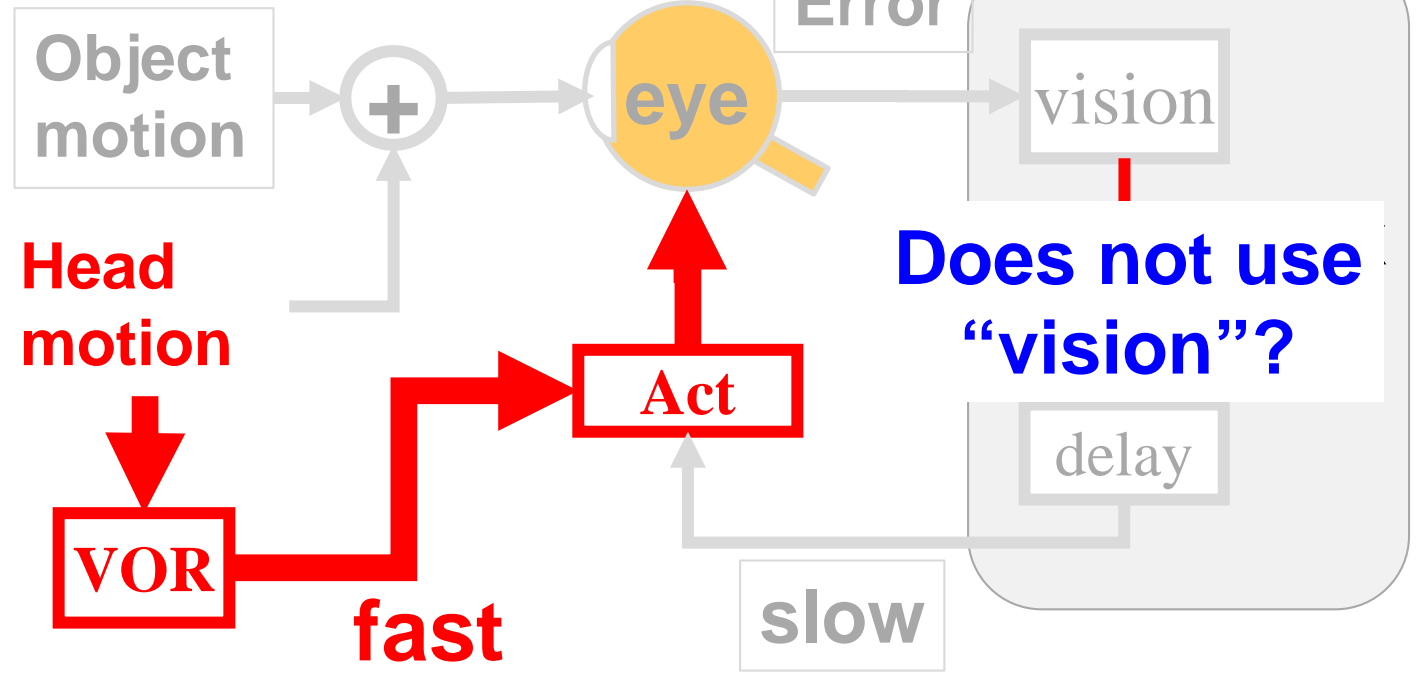
Flexible
Accurate

Inflexible

High
Bandwidth



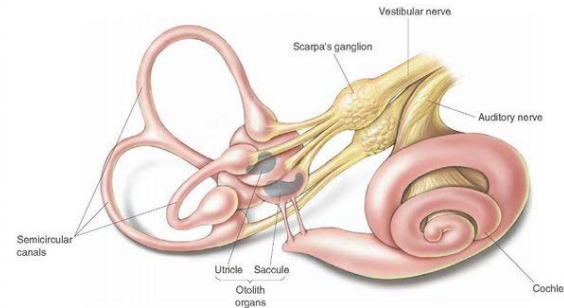
Low delay



Slow

vision

Fast

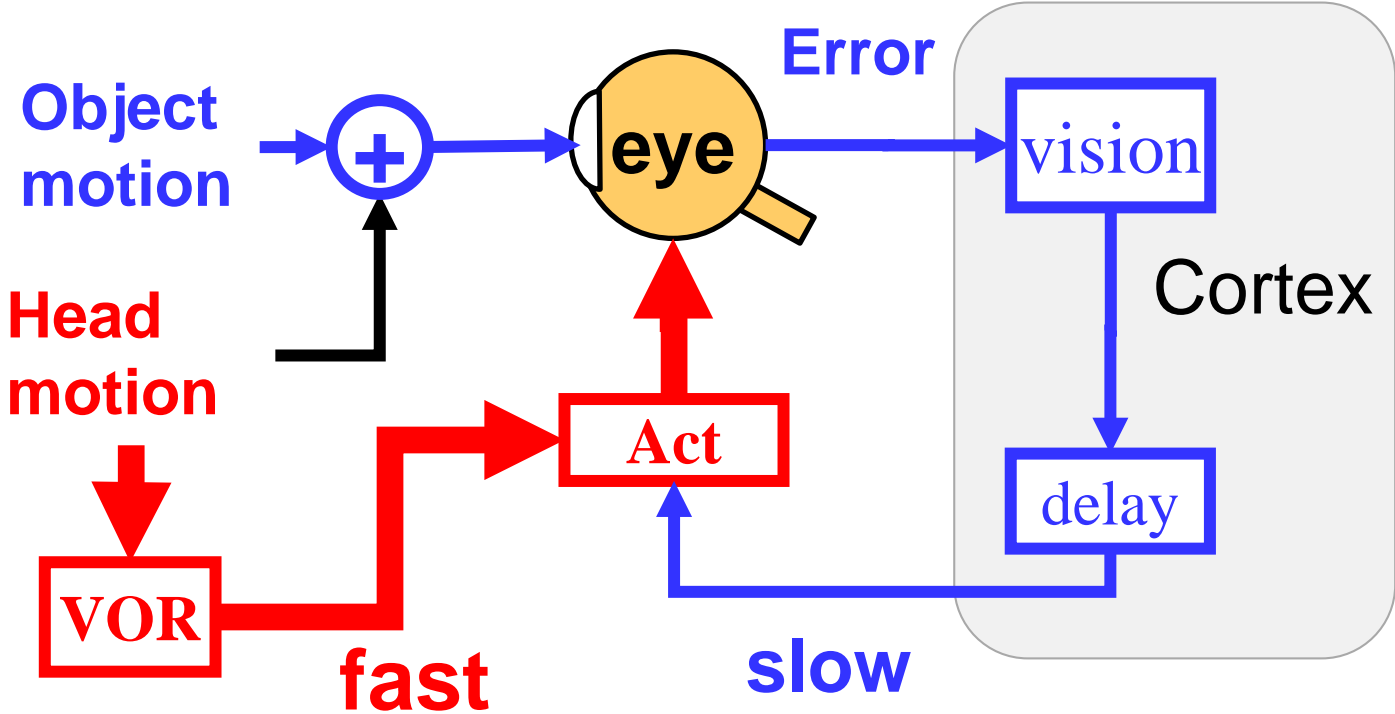


Flexible

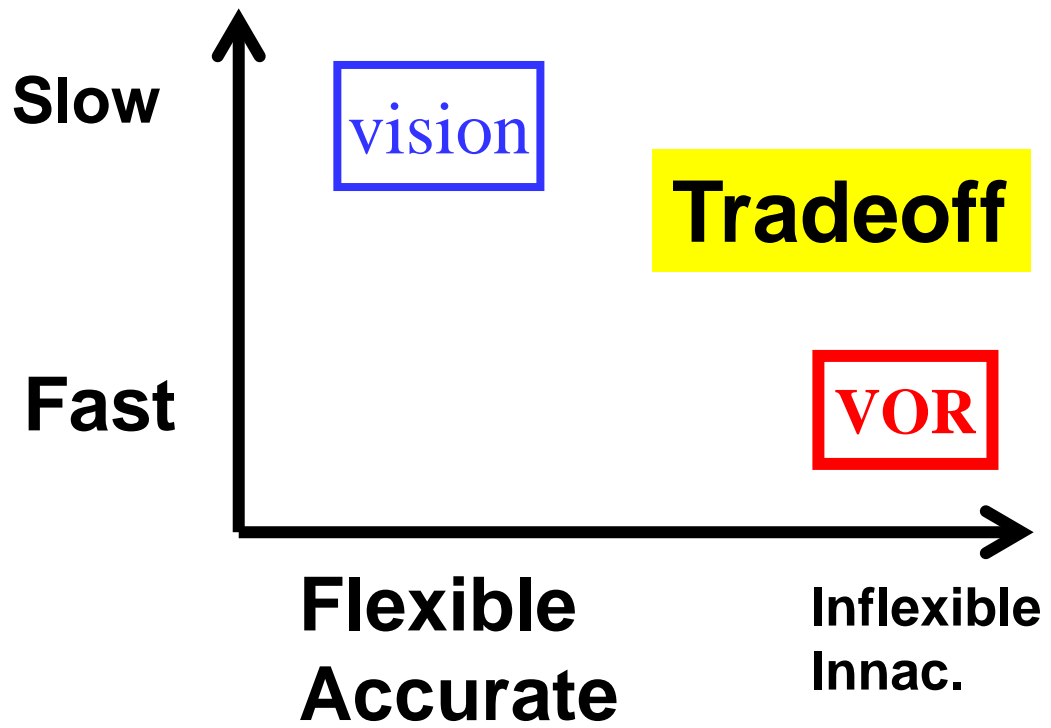
Inflexible
Inaccurate

Vestibular
Ocular
Reflex
(VOR)

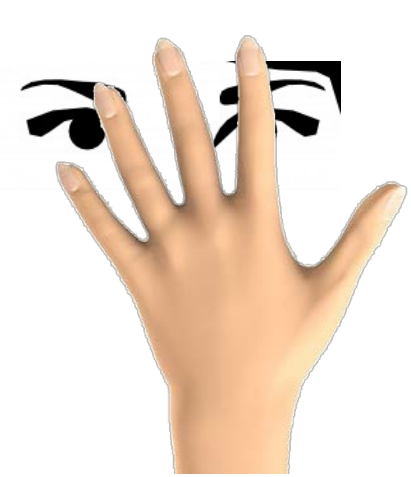
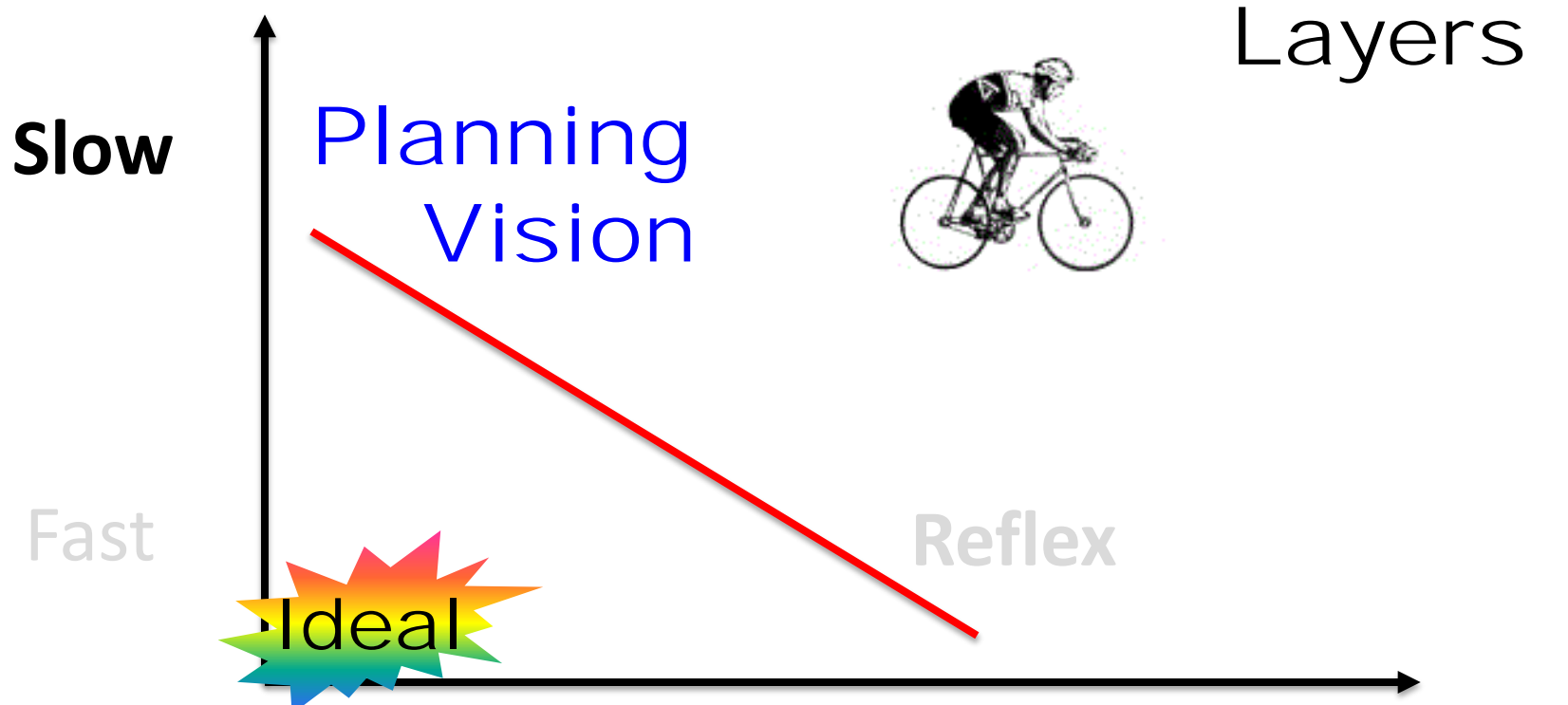
Mechanism



Minimal cartoon



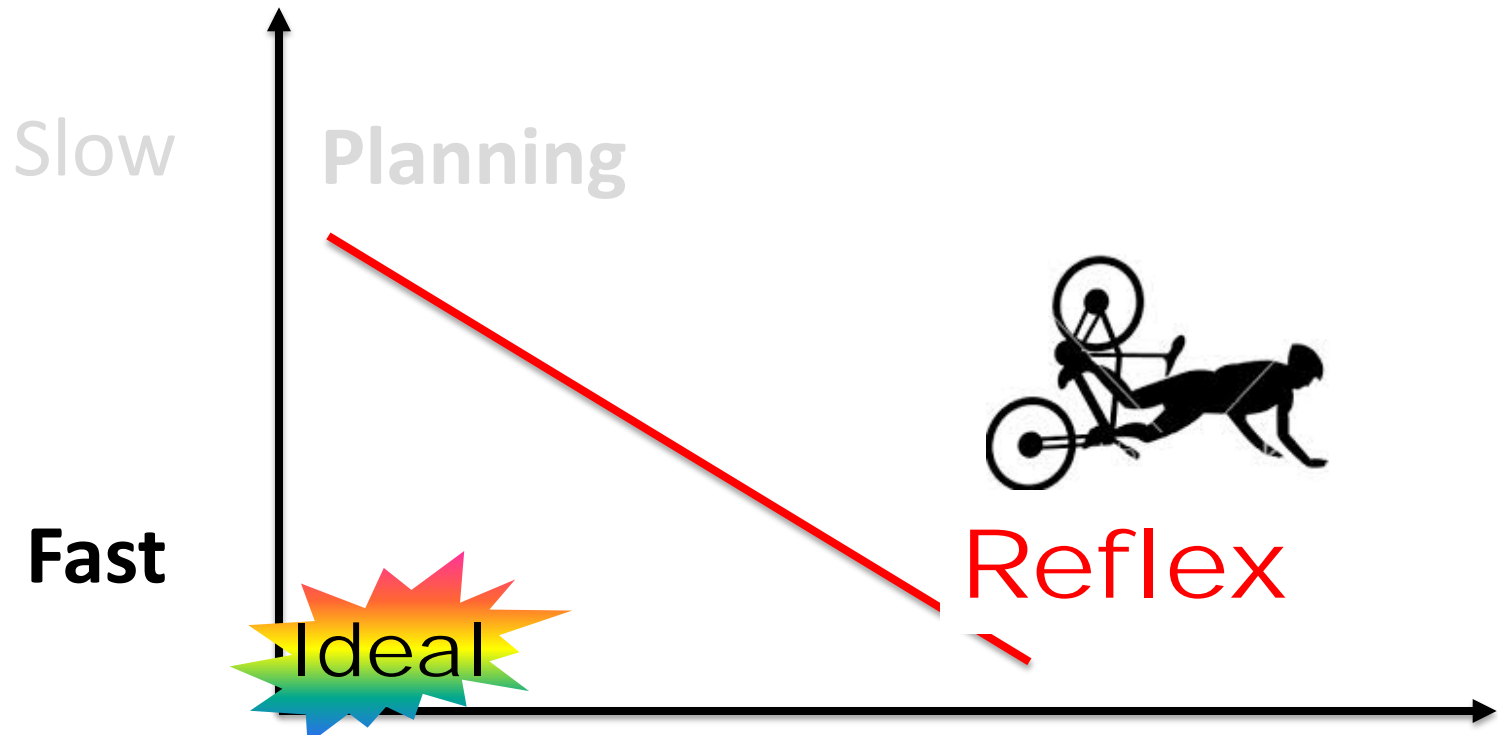
Why?



Object motion
Slow

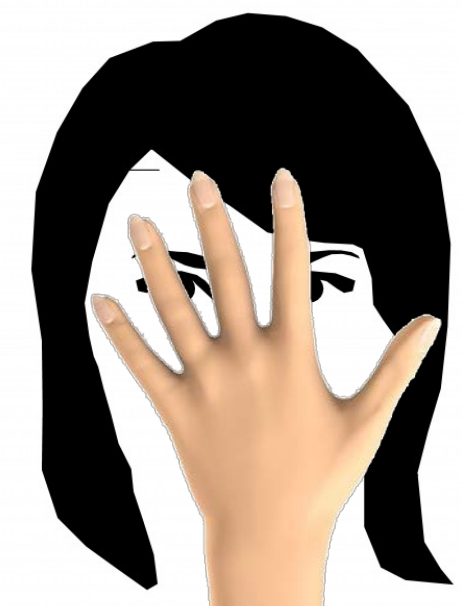
Accurate
Flexible
Centralized
Conscious
Deliberate
Stable virtual

Inaccurate
Rigid
Localized, distributed
Unconscious
Automatic
Unstable real dynamics



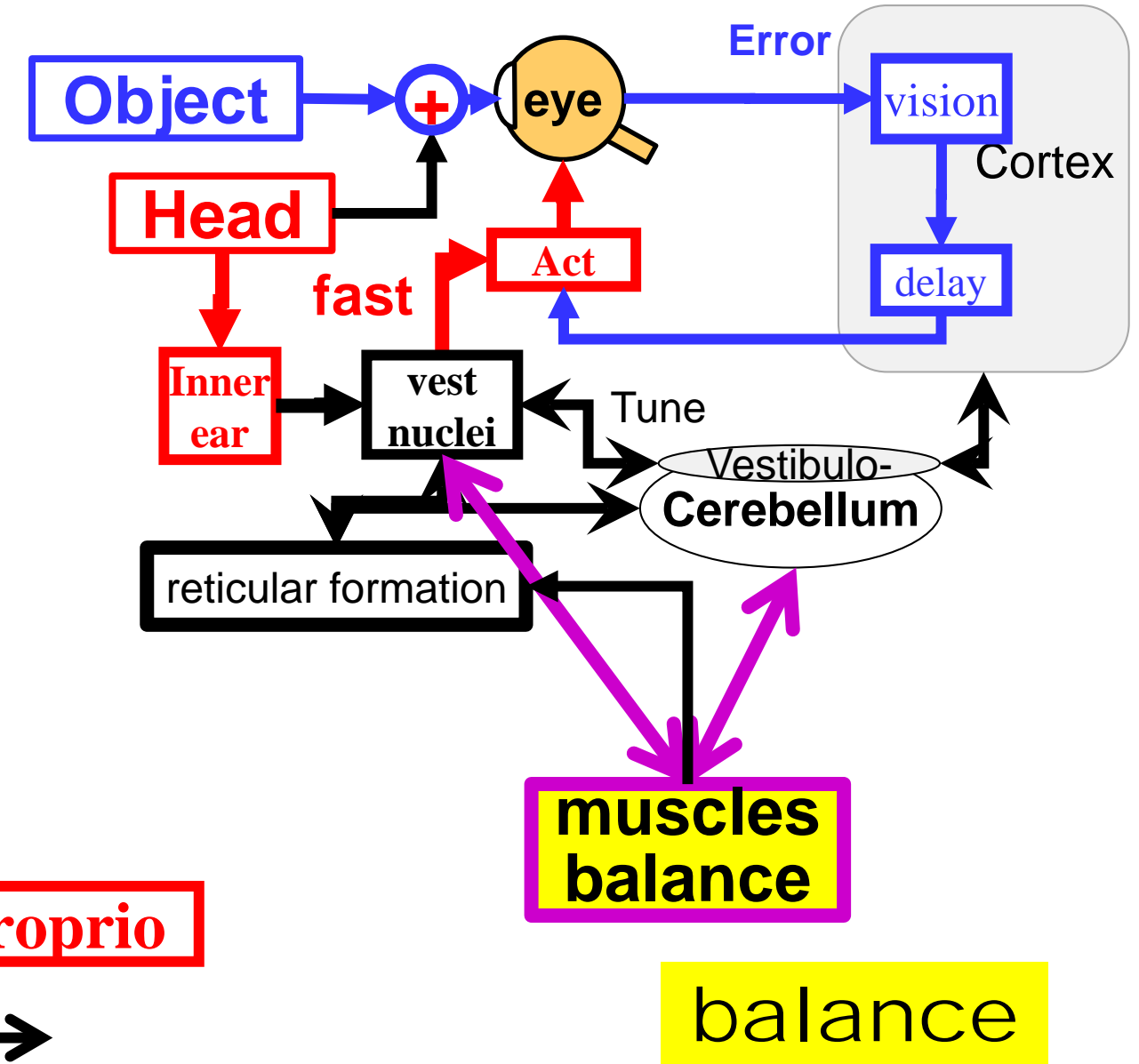
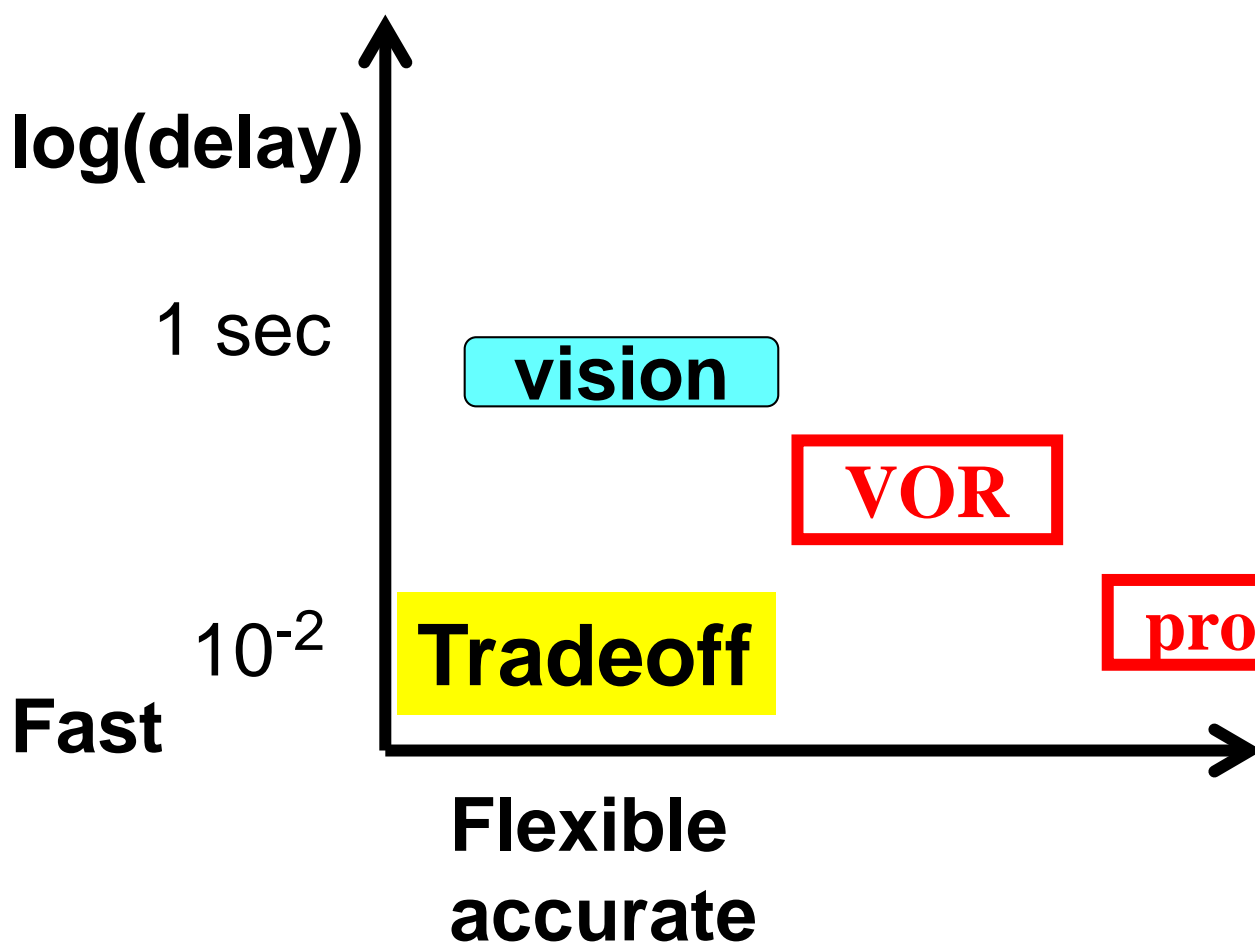
Head motion

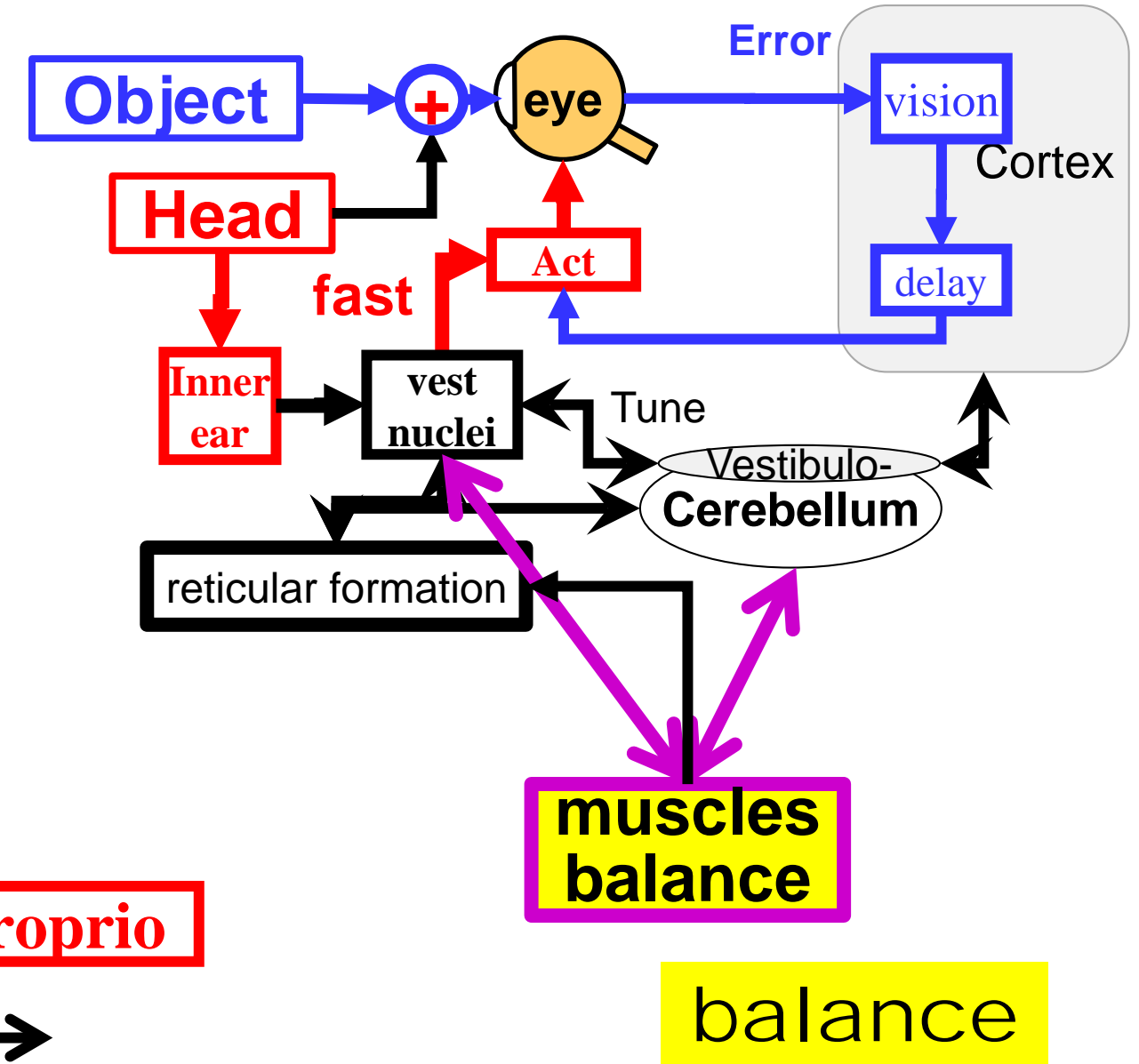
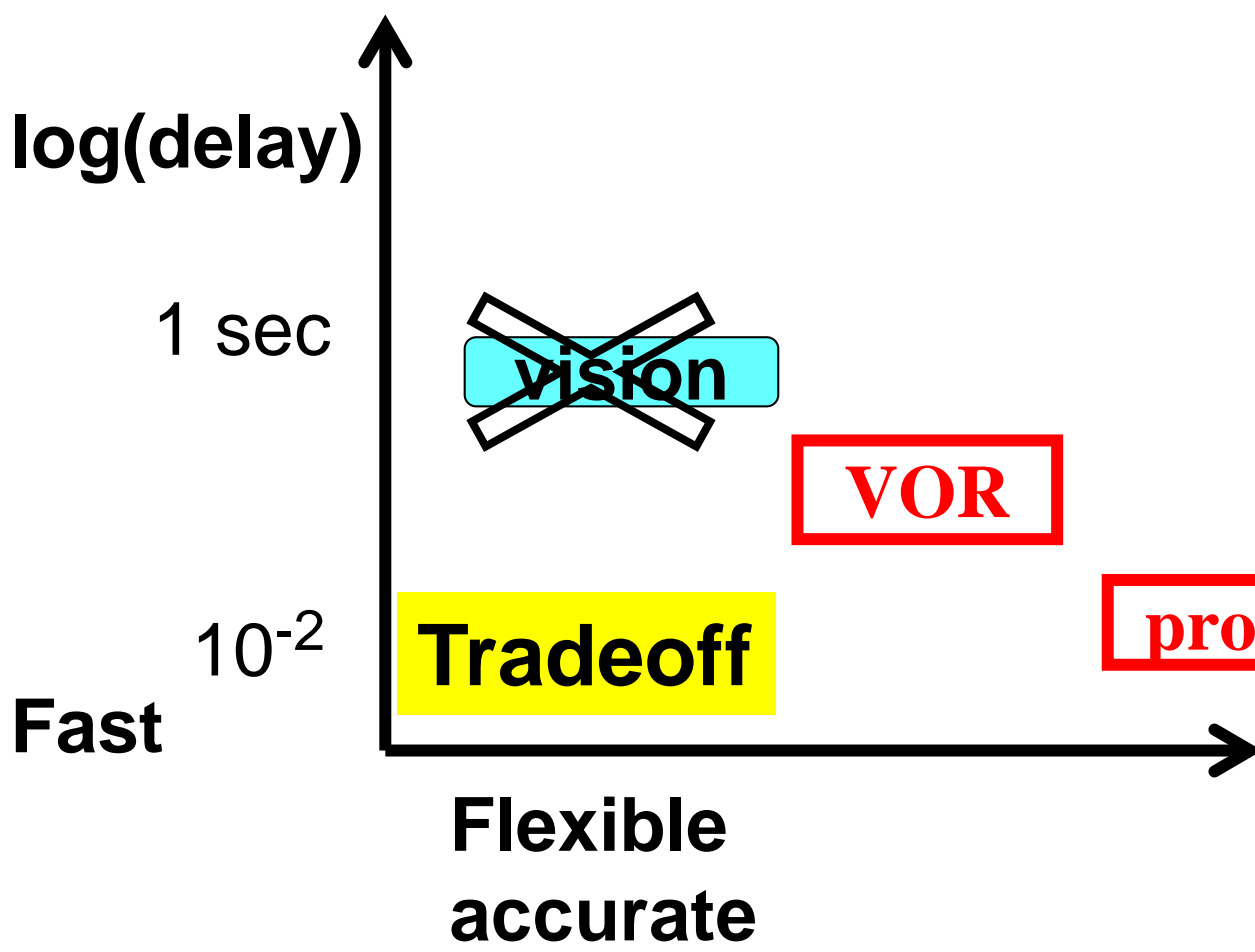
Fast

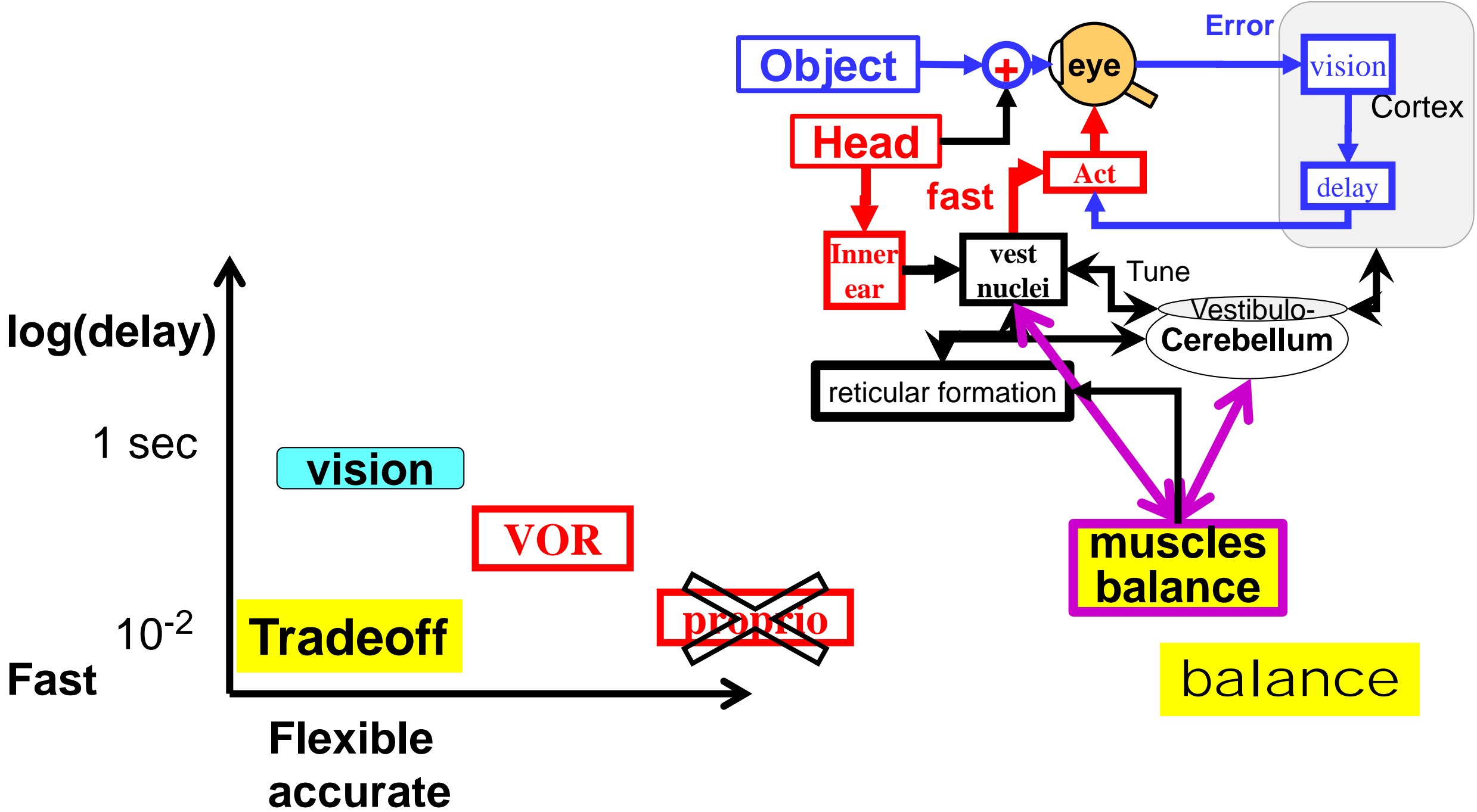


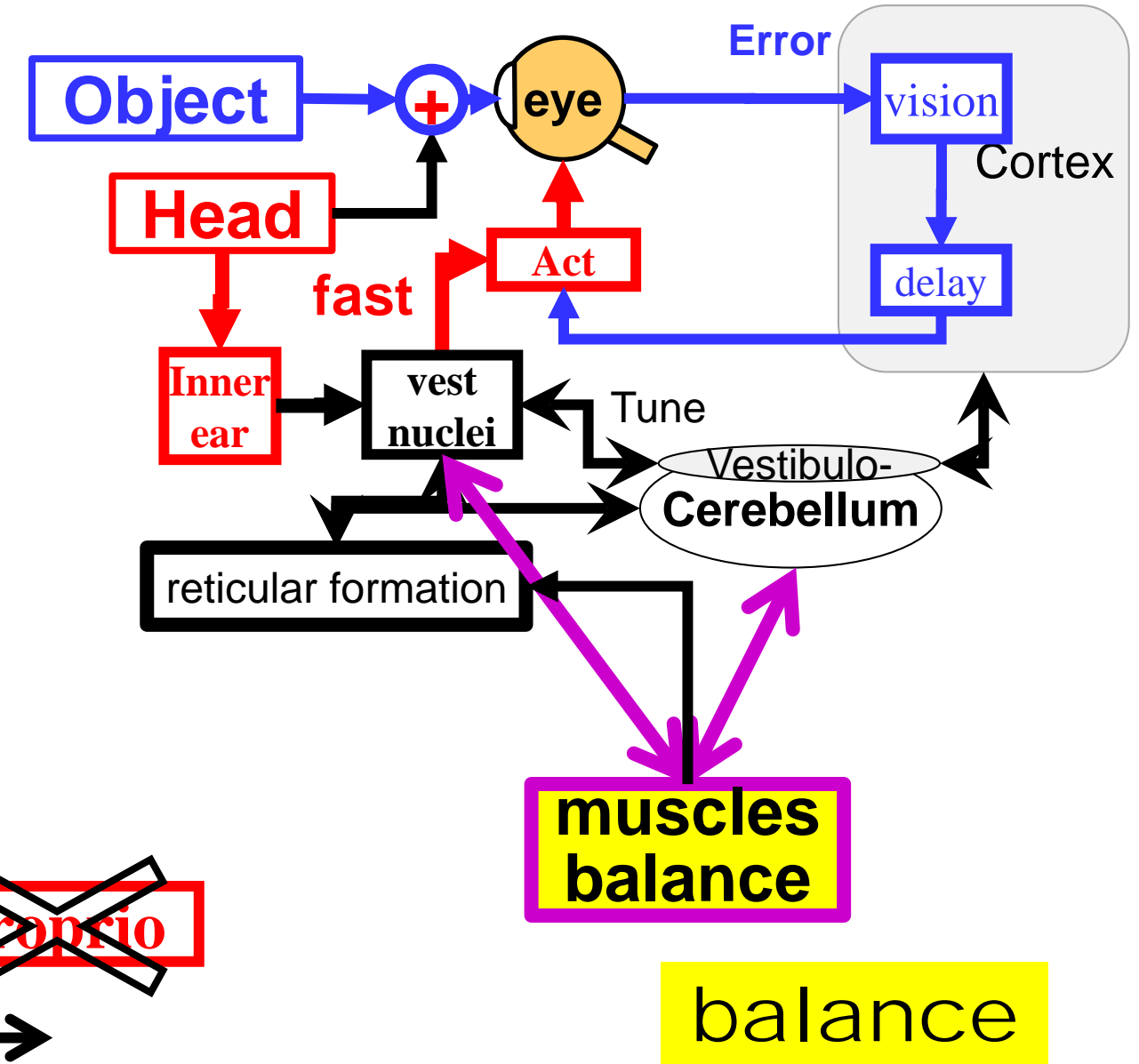
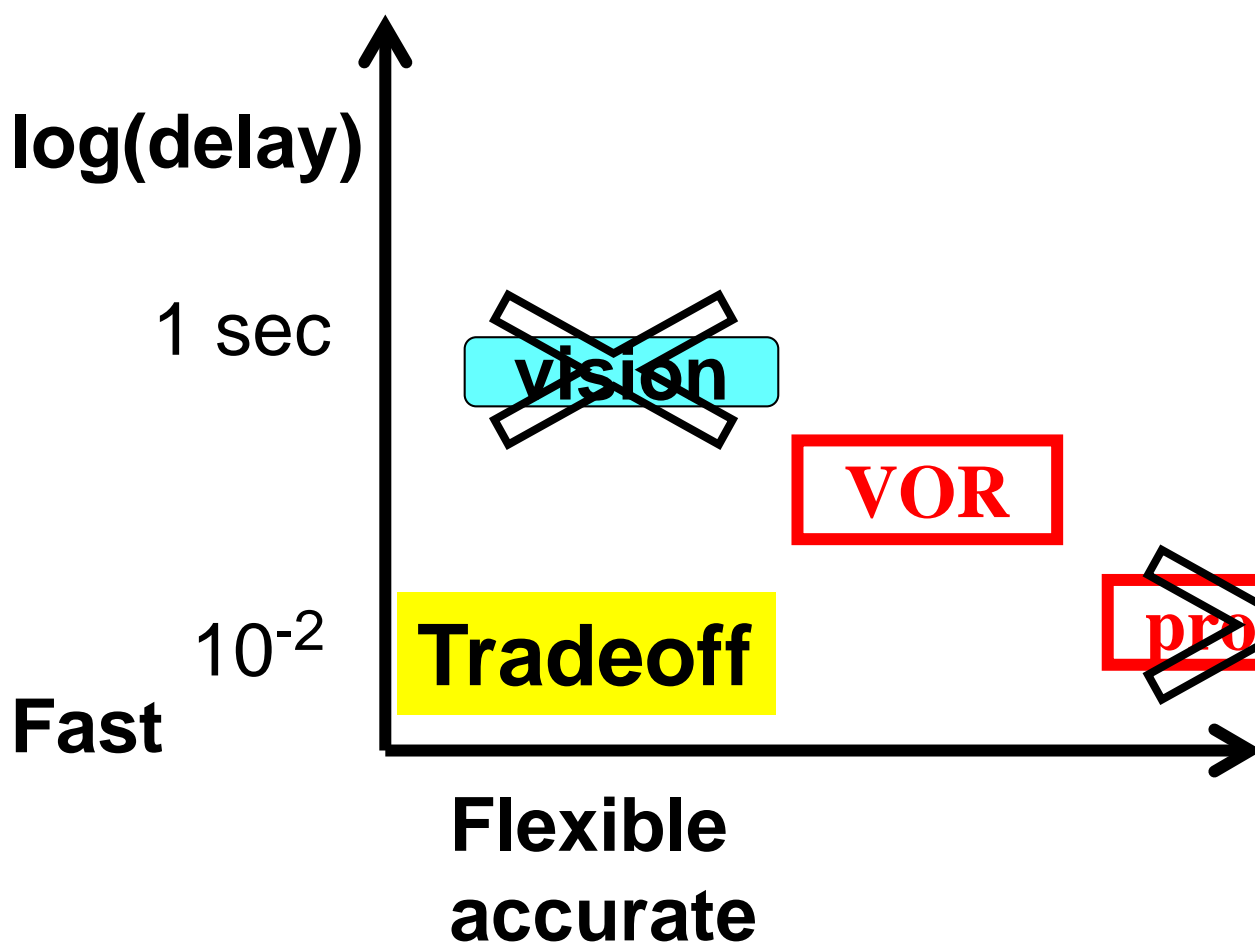
Accurate
Flexible
Centralized
Conscious
Deliberate
Stable virtual

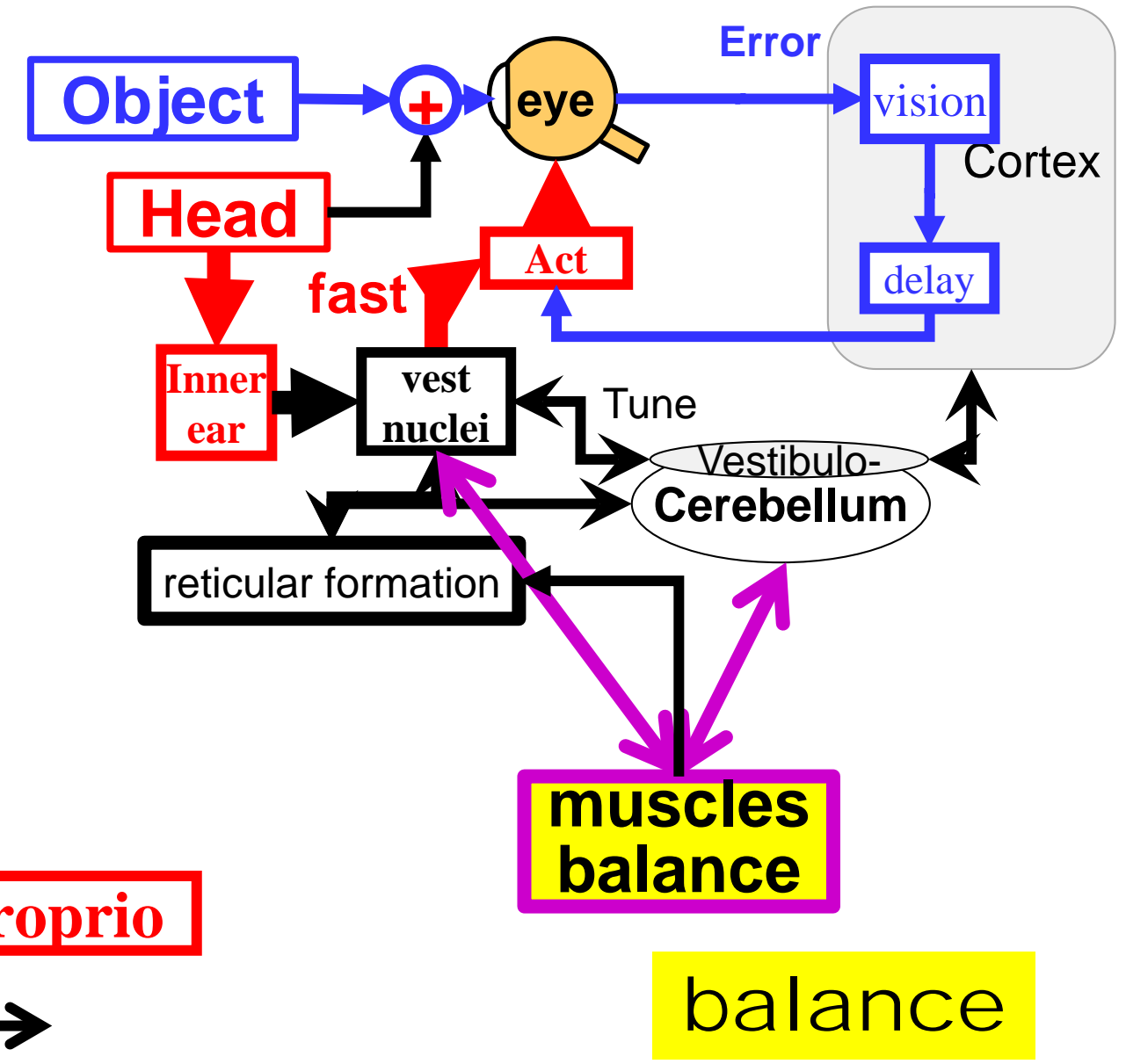
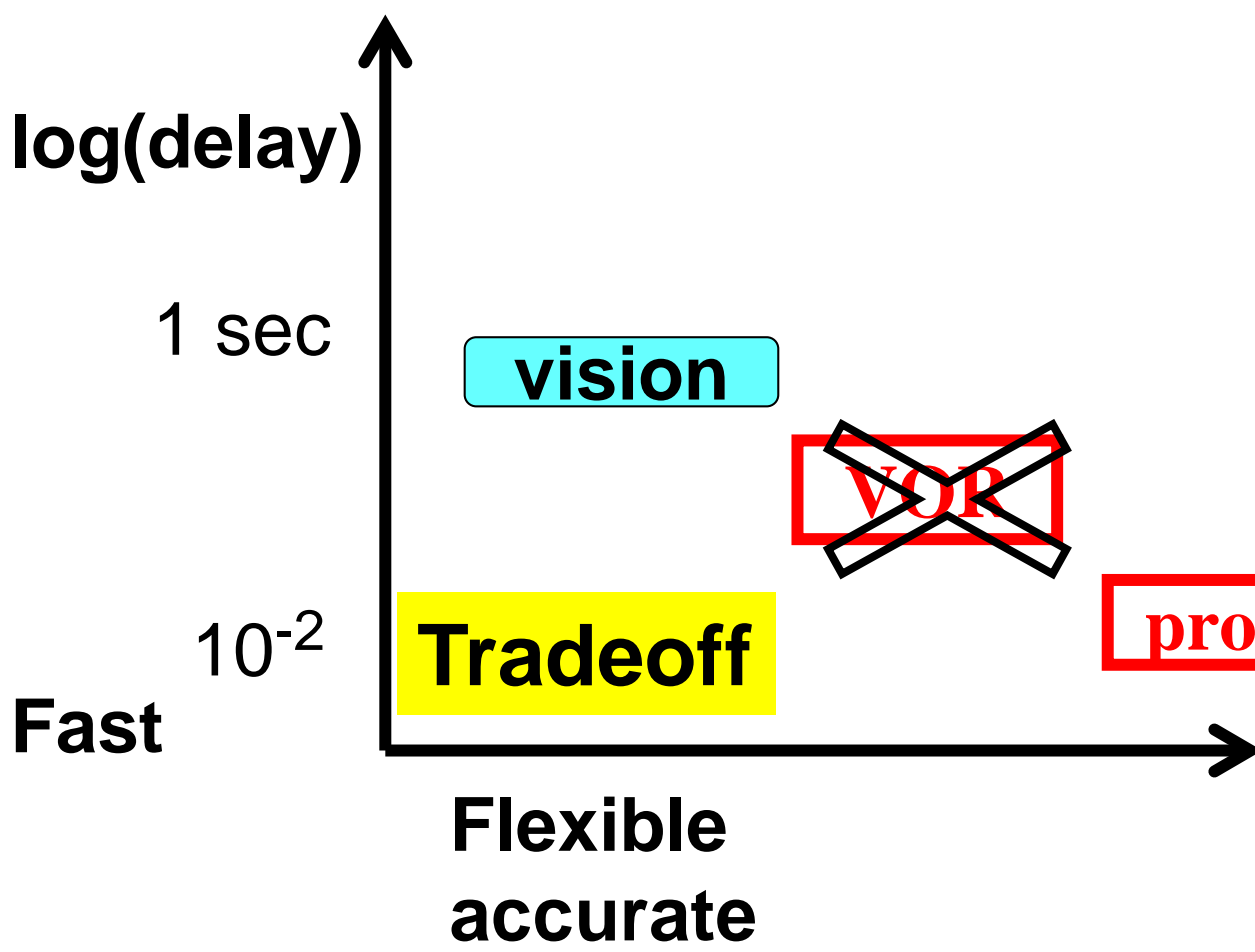
Inaccurate
Rigid
Localized, distributed
Unconscious
Automatic
Unstable real dynamics



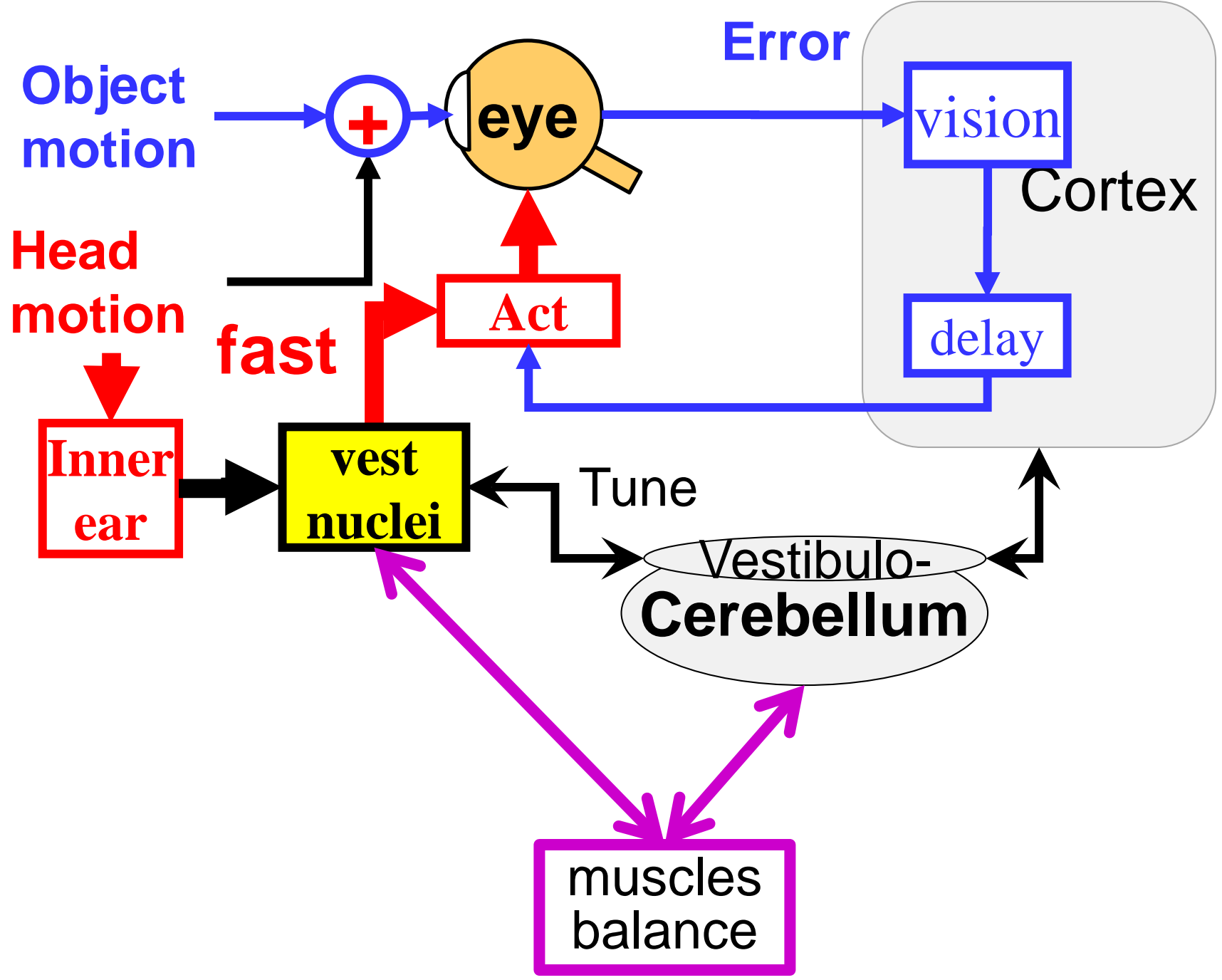








motion sickness?



motion sickness

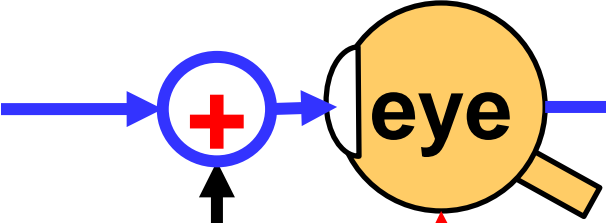
sweat

pharynx
larynx
regurg.

diaphragm
vomiting

Object motion

Head motion



Error

vision

Cortex

delay

Act

fast

Inner ear

vest nuclei

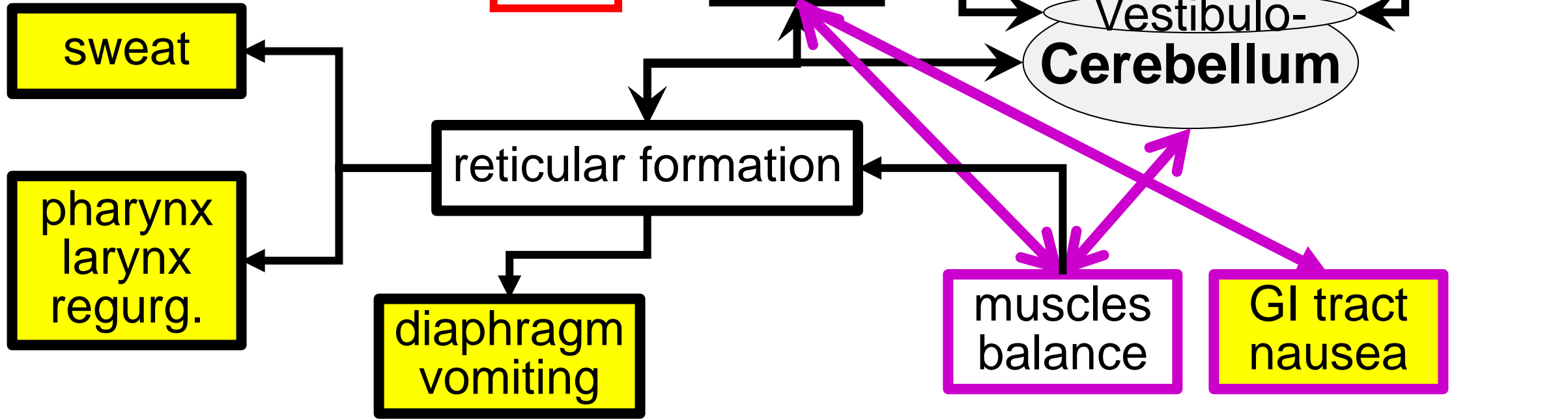
Tune

Vestibulo-Cerebellum

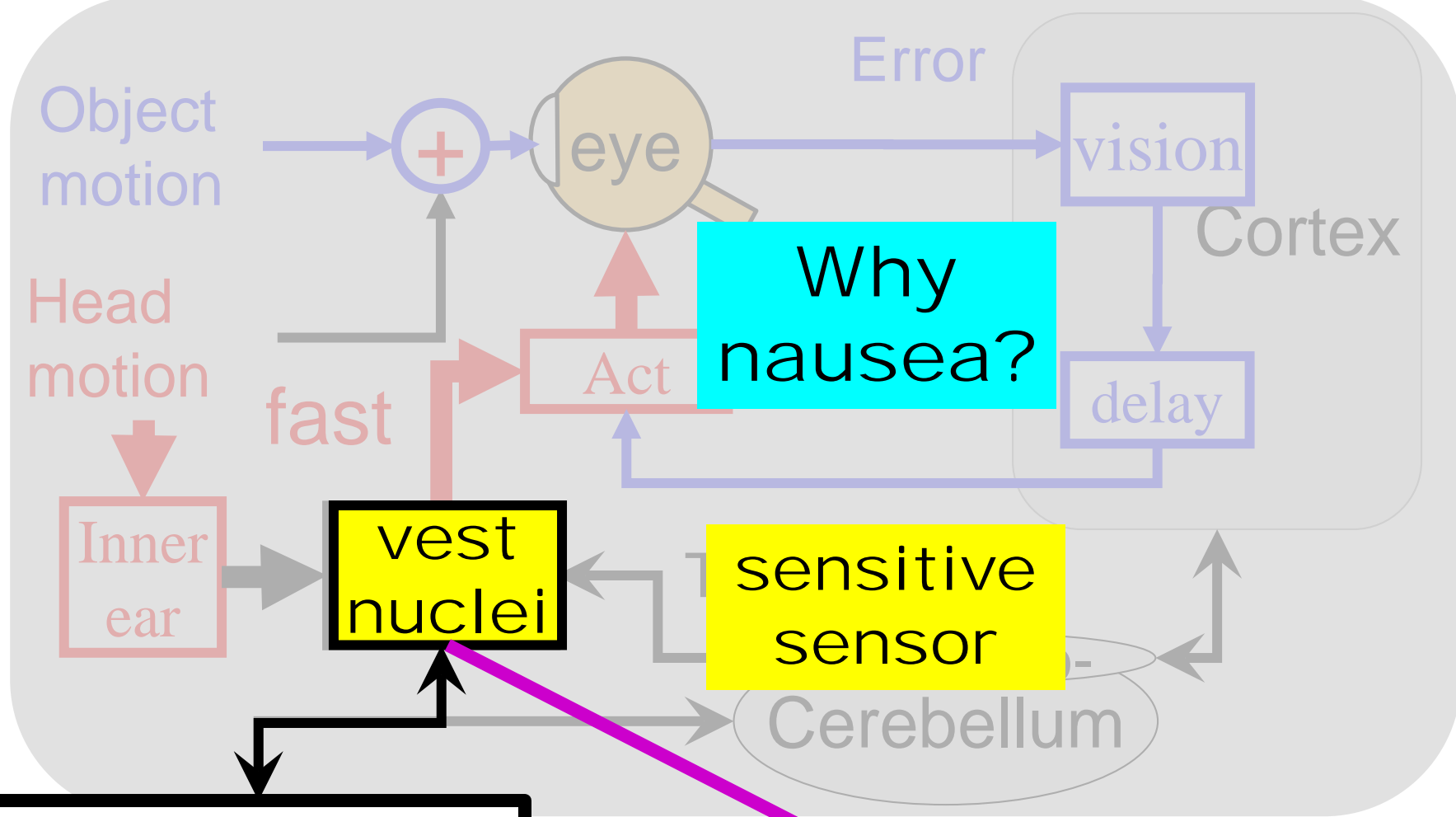
reticular formation

muscles balance

GI tract
nausea



motion sickness



sweat

pharynx
larynx
regurg.

diaphragm
vomiting

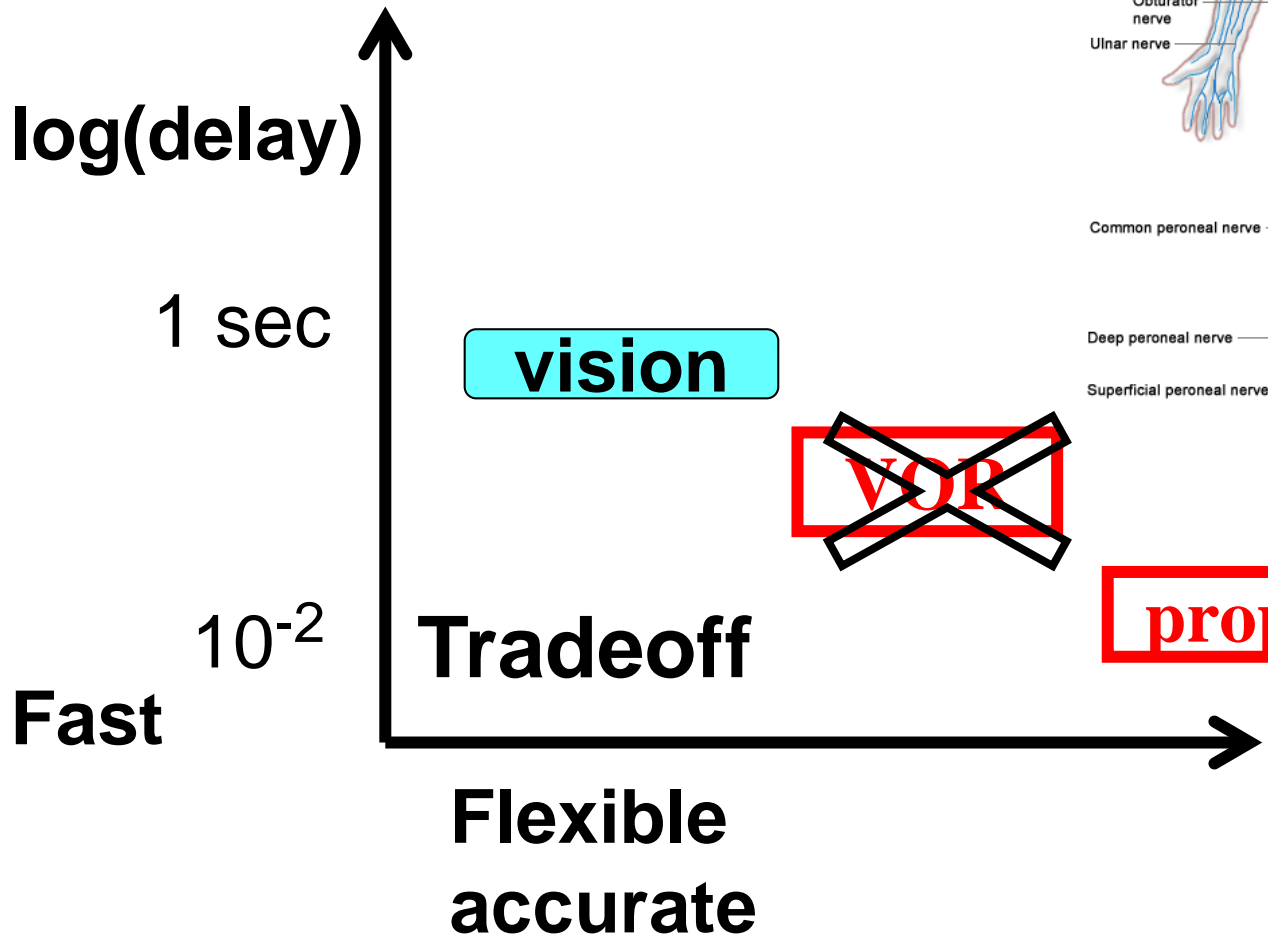
reticular formation

sensitive sensor

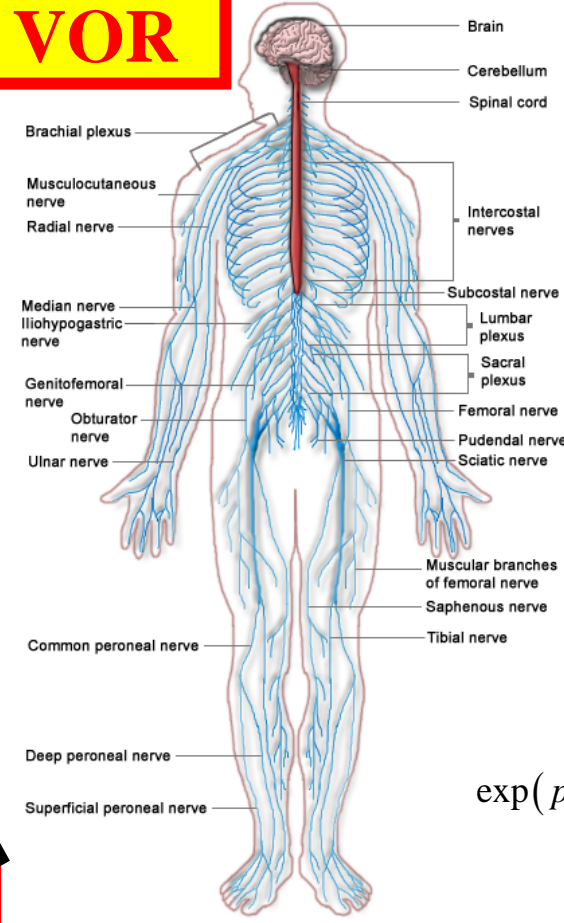
Cerebellum

GI tract
nausea

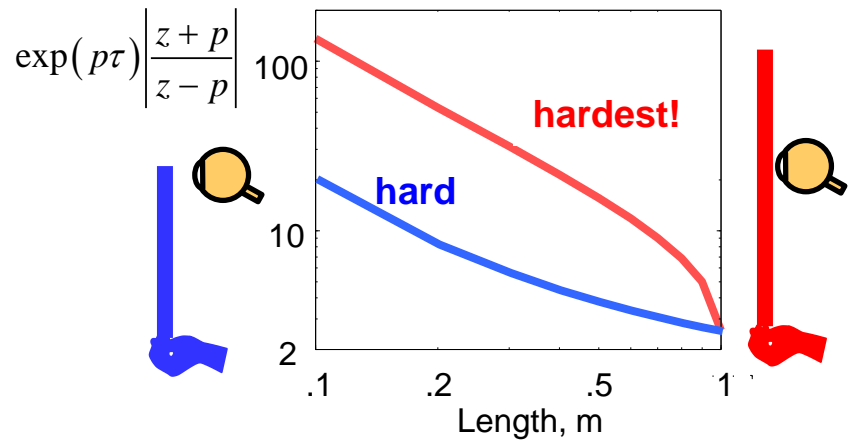
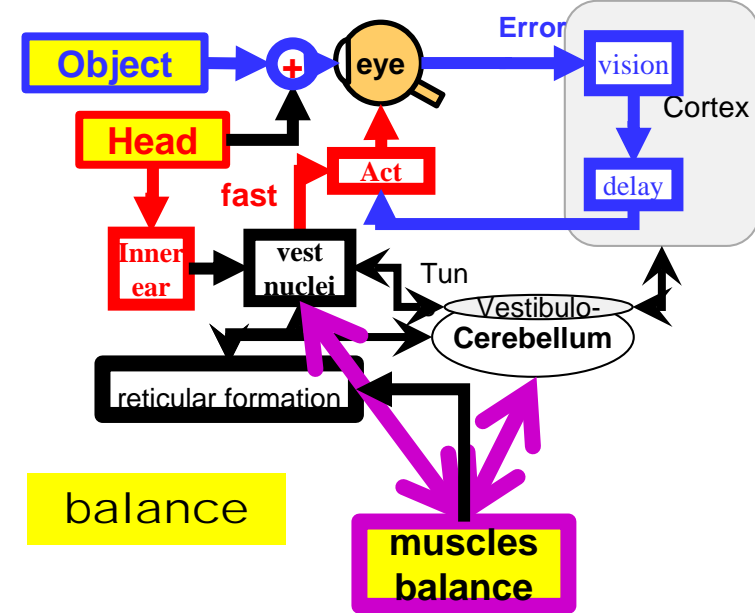
Need sensor that is fast and high. Why?



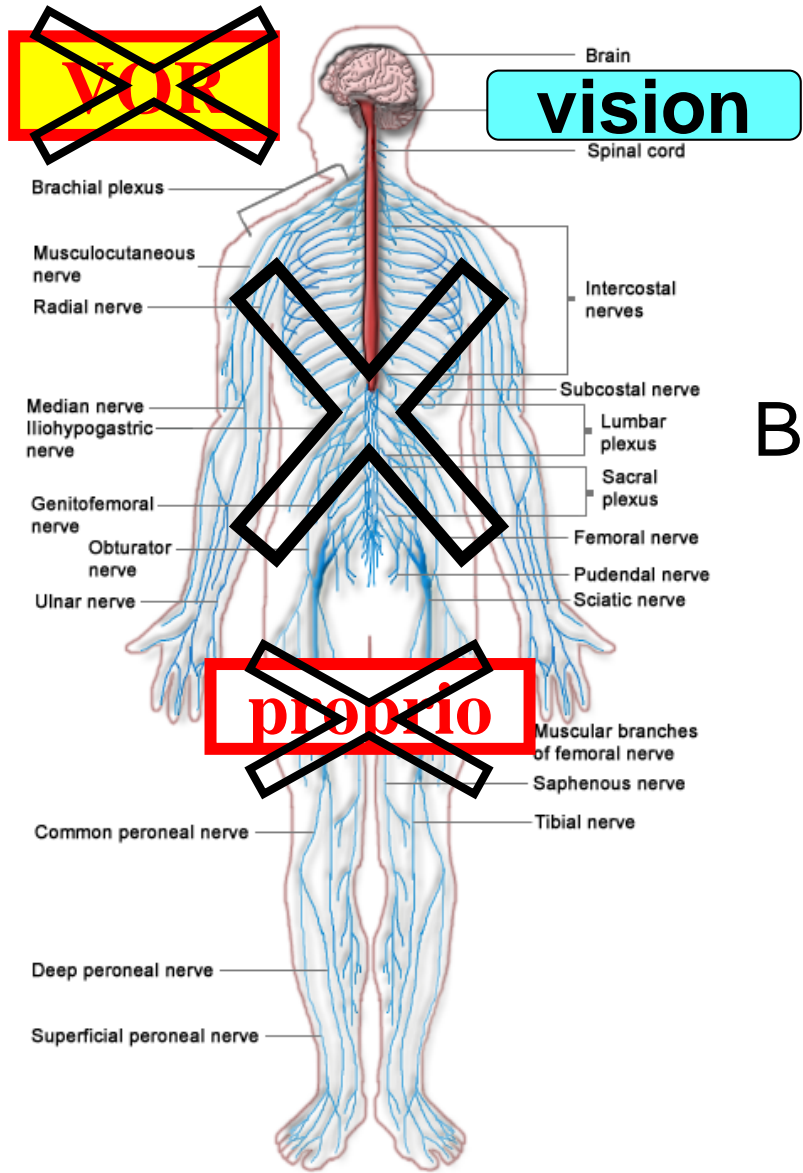
VOR



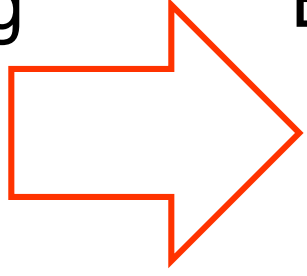
proprio



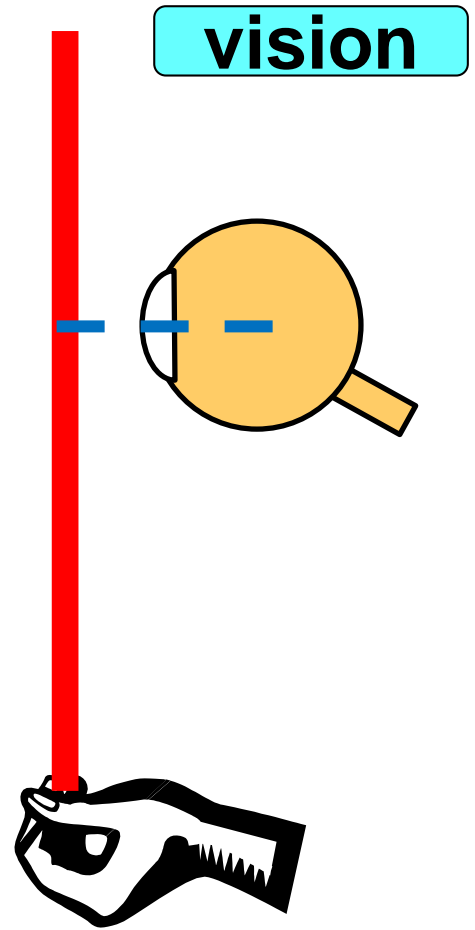
Waterbed $\left. \begin{matrix} \exp\left(\int \ln|T|\right) \\ \|T\|_\infty \end{matrix} \right\} \geq \exp(p\tau) \left| \frac{z+p}{z-p} \right|$

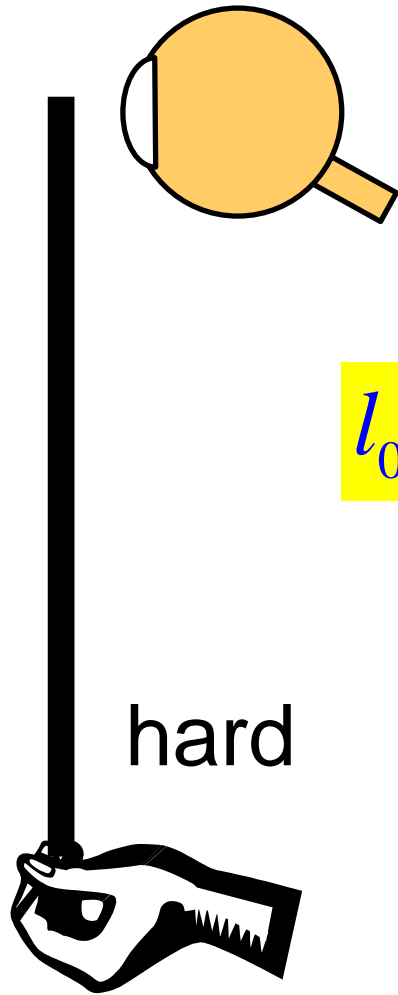


Balancing bodies



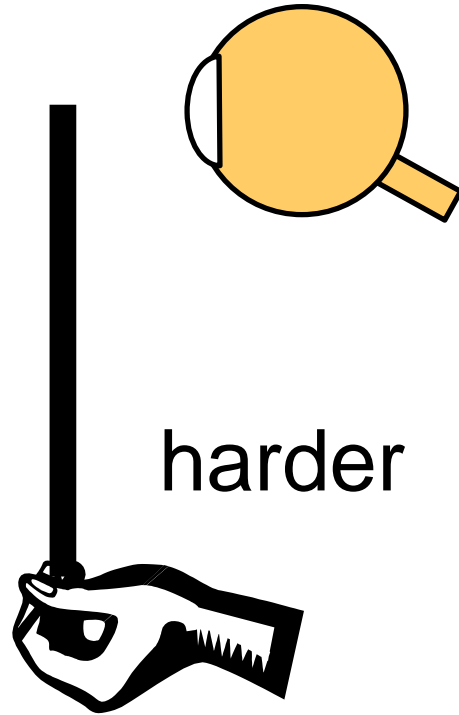
Balancing sticks





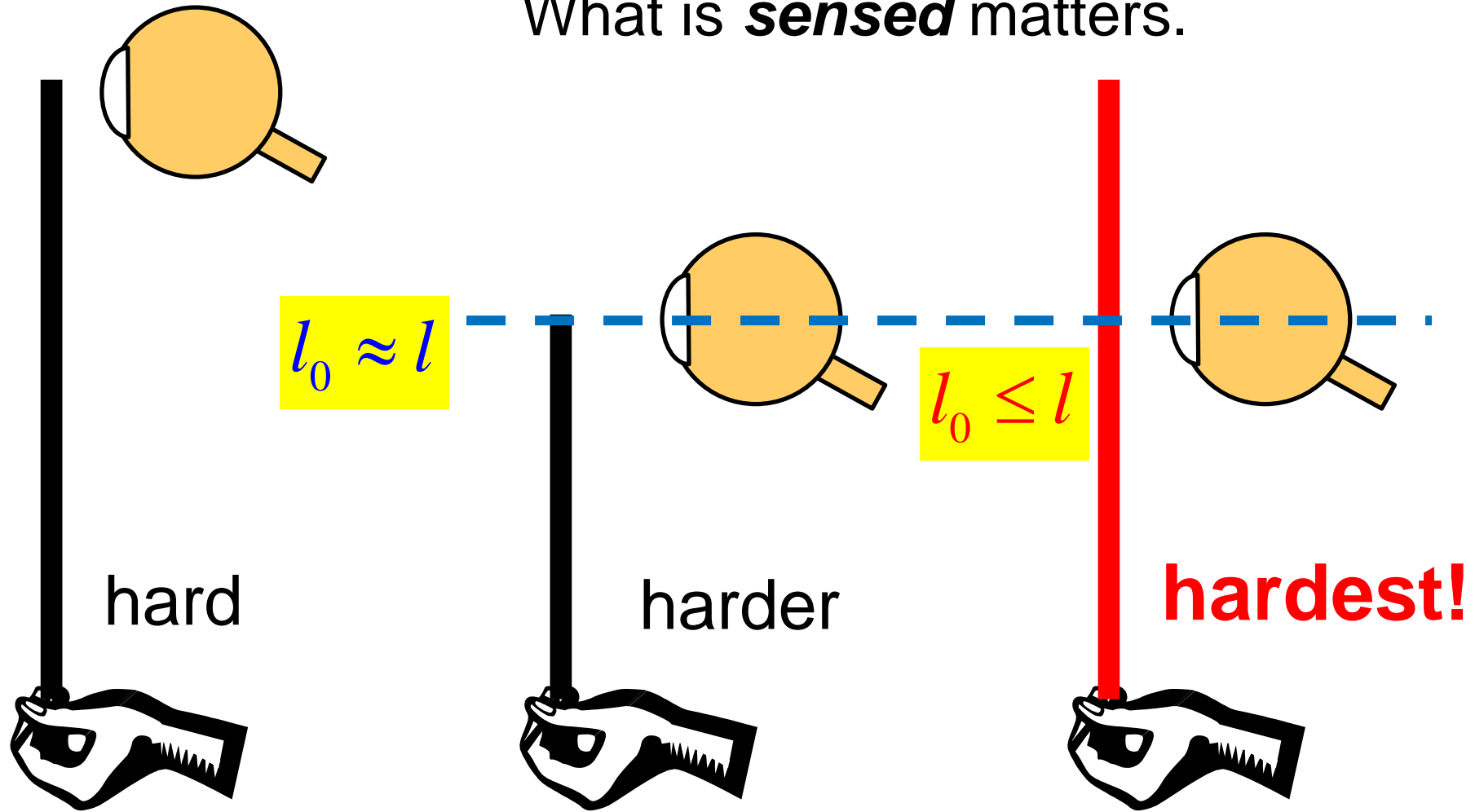
hard

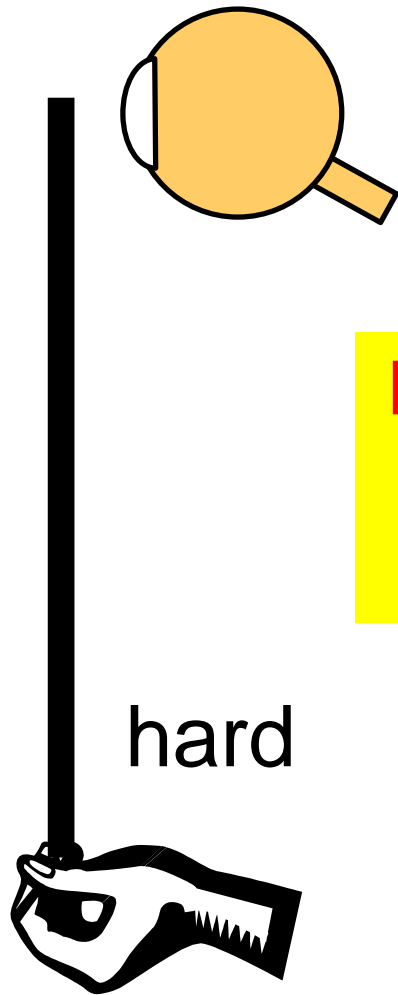
$$l_0 \approx l$$



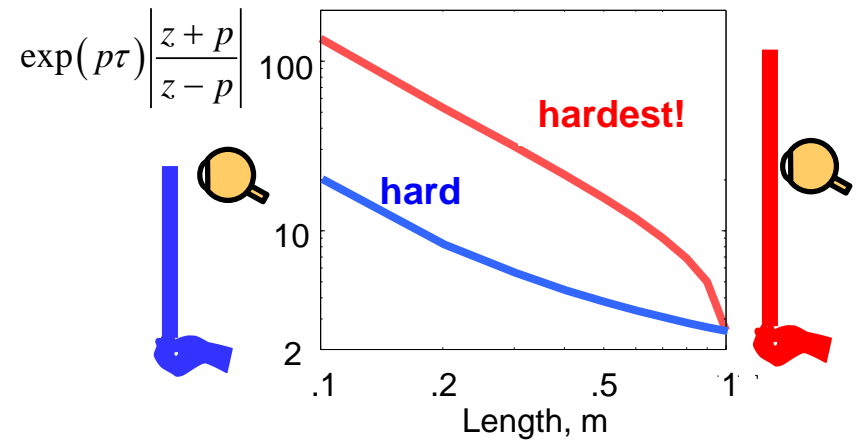
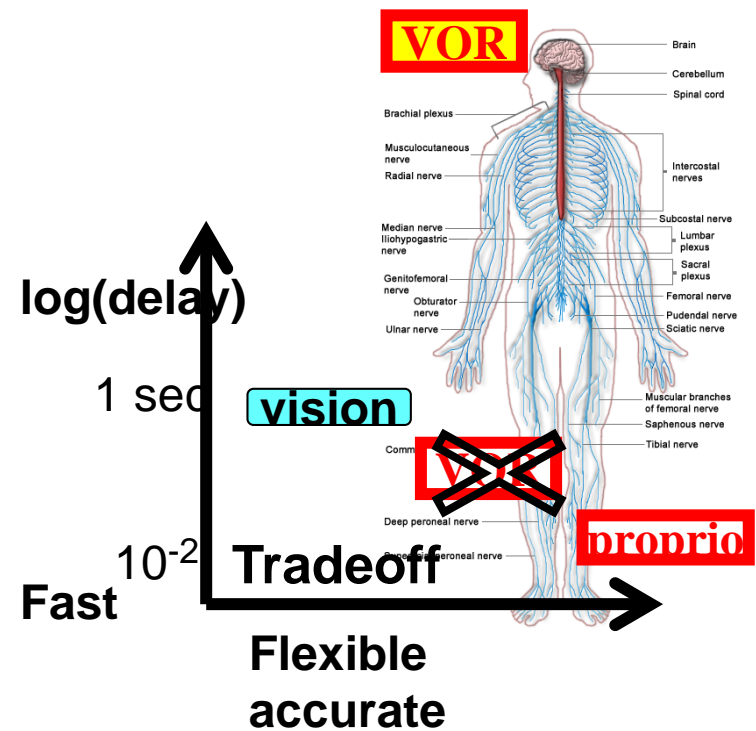
harder

What is *sensed* matters.





Need sensor that is fast and high. Why?



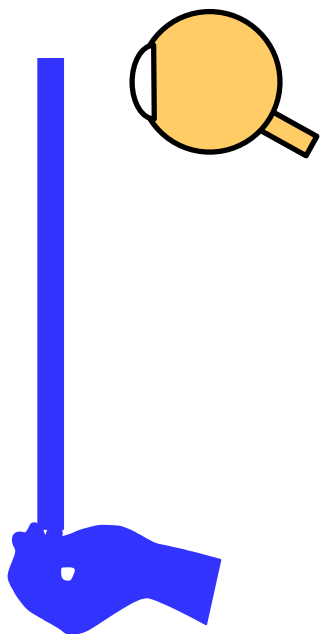
Waterbed

$$\left. \begin{matrix} \exp\left(\int \ln|T|\right) \\ \|T\|_{\infty} \end{matrix} \right\} \geq \exp(p\tau) \left| \frac{z+p}{z-p} \right|$$

$$\tau = .3s$$

$$\left. \frac{\exp\left(\int \ln|T|\right)}{\|T\|_\infty} \right\} \geq \exp(p\tau) \left| \frac{z+p}{z-p} \right| \geq \exp(p\tau)$$

Theory



100

$$\exp(p\tau) \left| \frac{z+p}{z-p} \right|$$

hard

hardest!

10

$$\exp(p\tau)$$

$$p \propto \sqrt{\frac{1}{l}}$$

2

.1

.2

.5

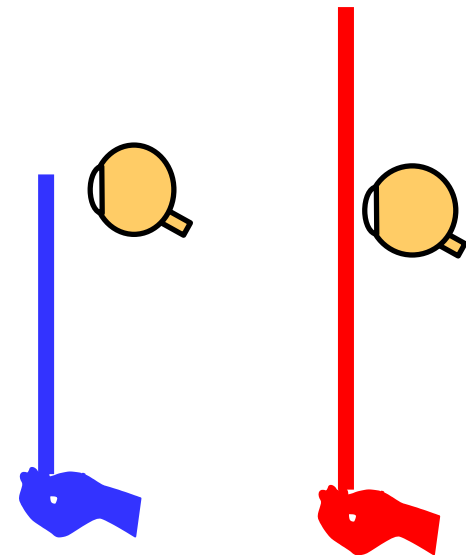
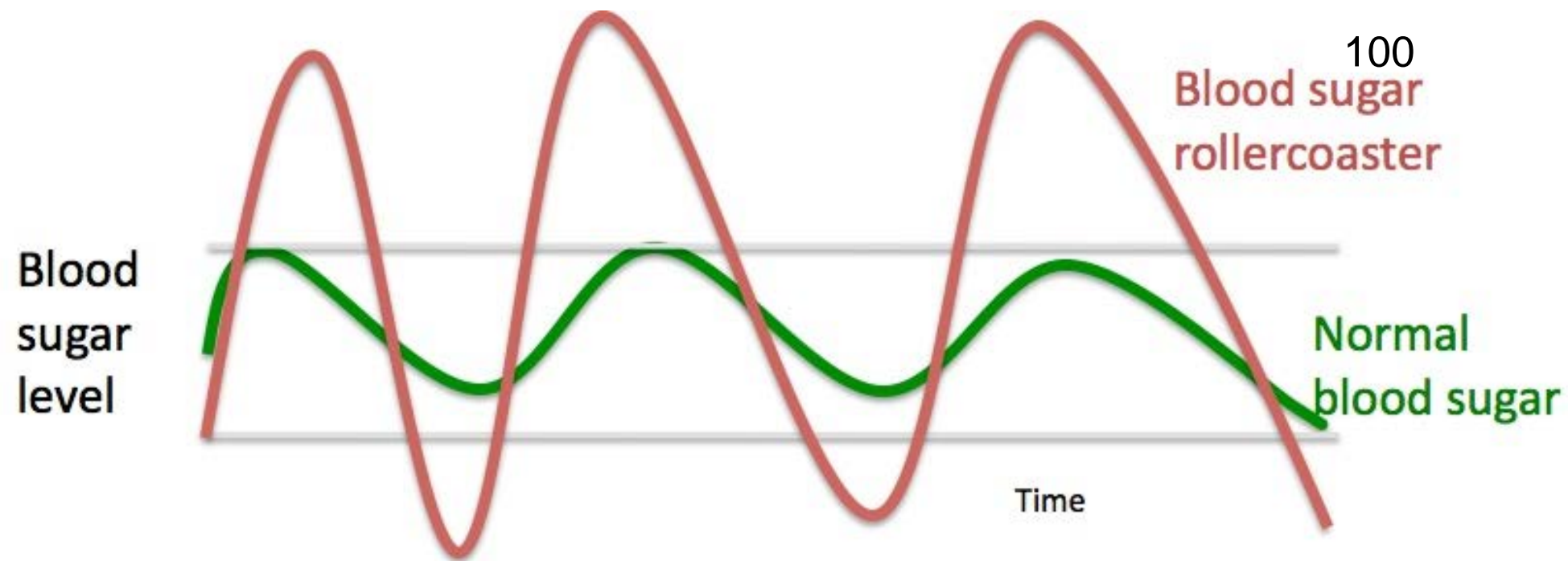
1

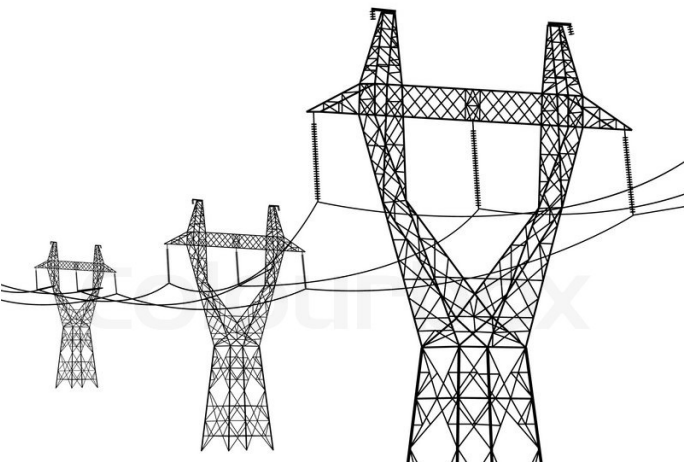
Length, m



$$\left. \exp\left(\int \ln |T| \right) \right\|_{\infty} \geq \exp(p\tau) \left| \frac{z+p}{z-p} \right|$$

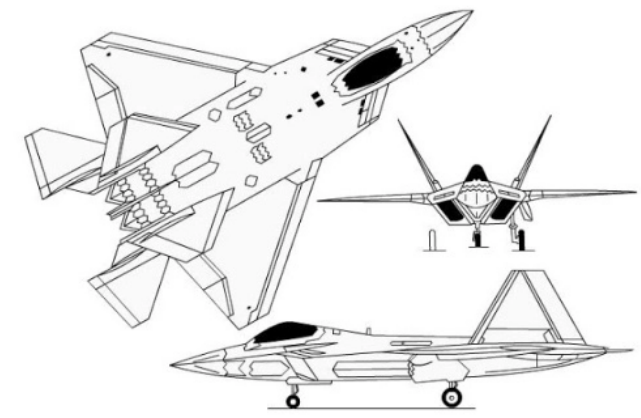
How **controlled** systems crash.





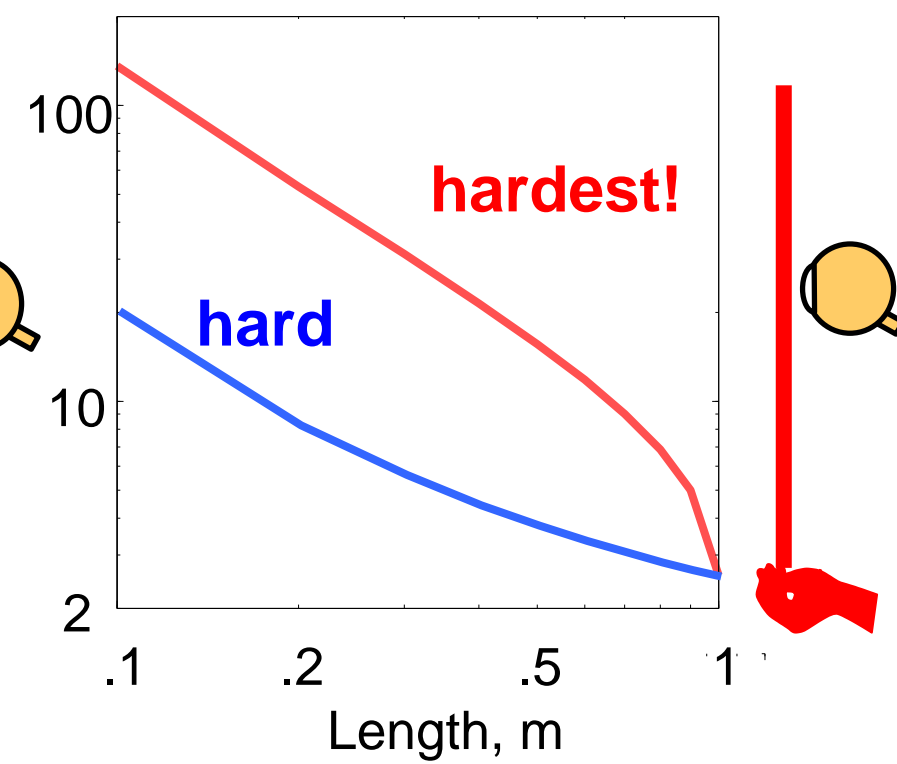
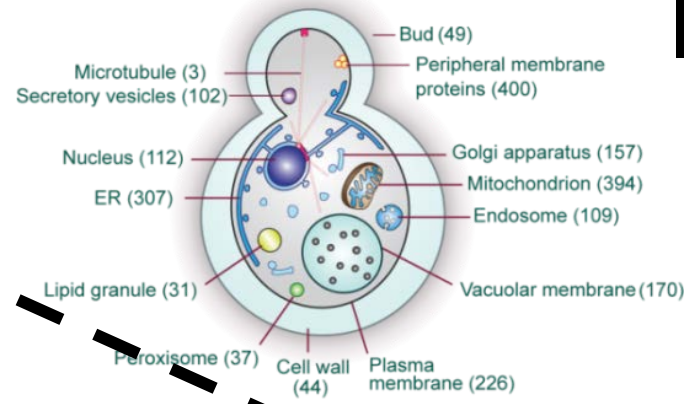
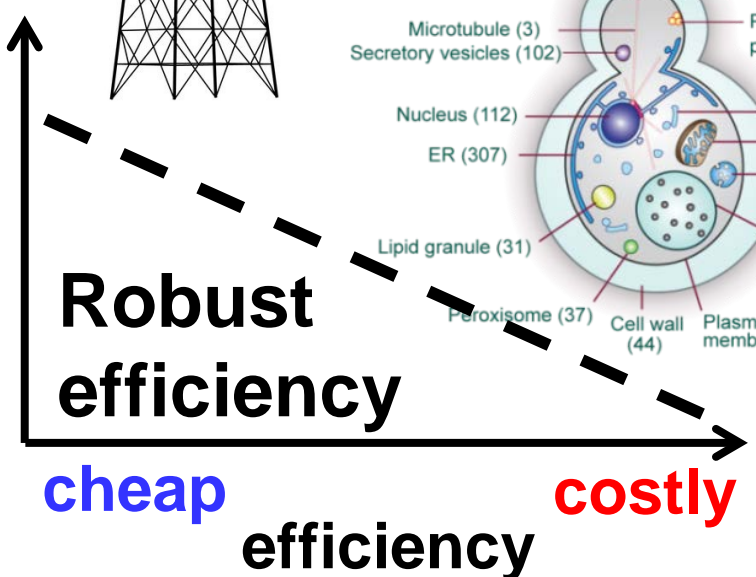
$$\left. \begin{matrix} \exp\left(\int \ln|T|\right) \\ \|T\|_\infty \end{matrix} \right\} \geq \exp(p\tau) \frac{z+p}{z-p}$$

Universal laws



Fragile

Robust

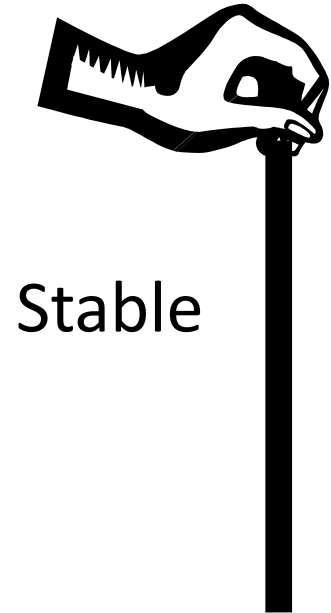


Glycolytic Oscillations and Limits on Robust Efficiency

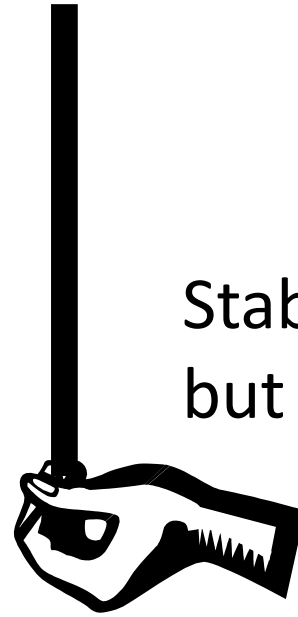
Fiona A. Chandra,^{1*} Gentian Buzi,² John C. Doyle²



... which is consumed in a final reaction modeling...
 ... in glycolysis, two ATP...
 ... upstream and four are...
 ... which normalizes to $q = 1$...
 ... (two downstream) with...
 ... To highlight essential...
 ... st possible analysis, we...
 ... the concentration such that the...

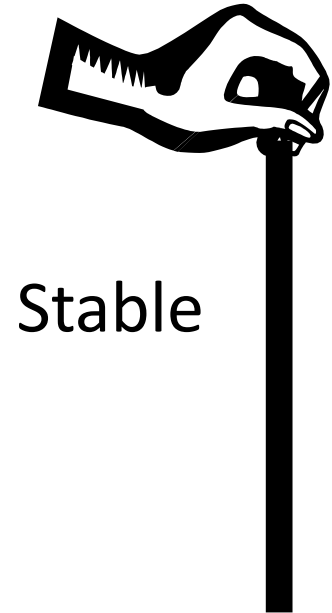


Stable



Stabilizable
but fragile

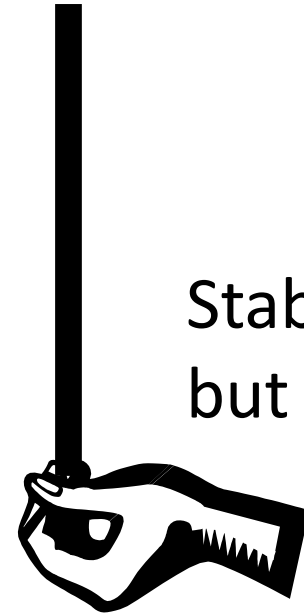
Other examples



Stable

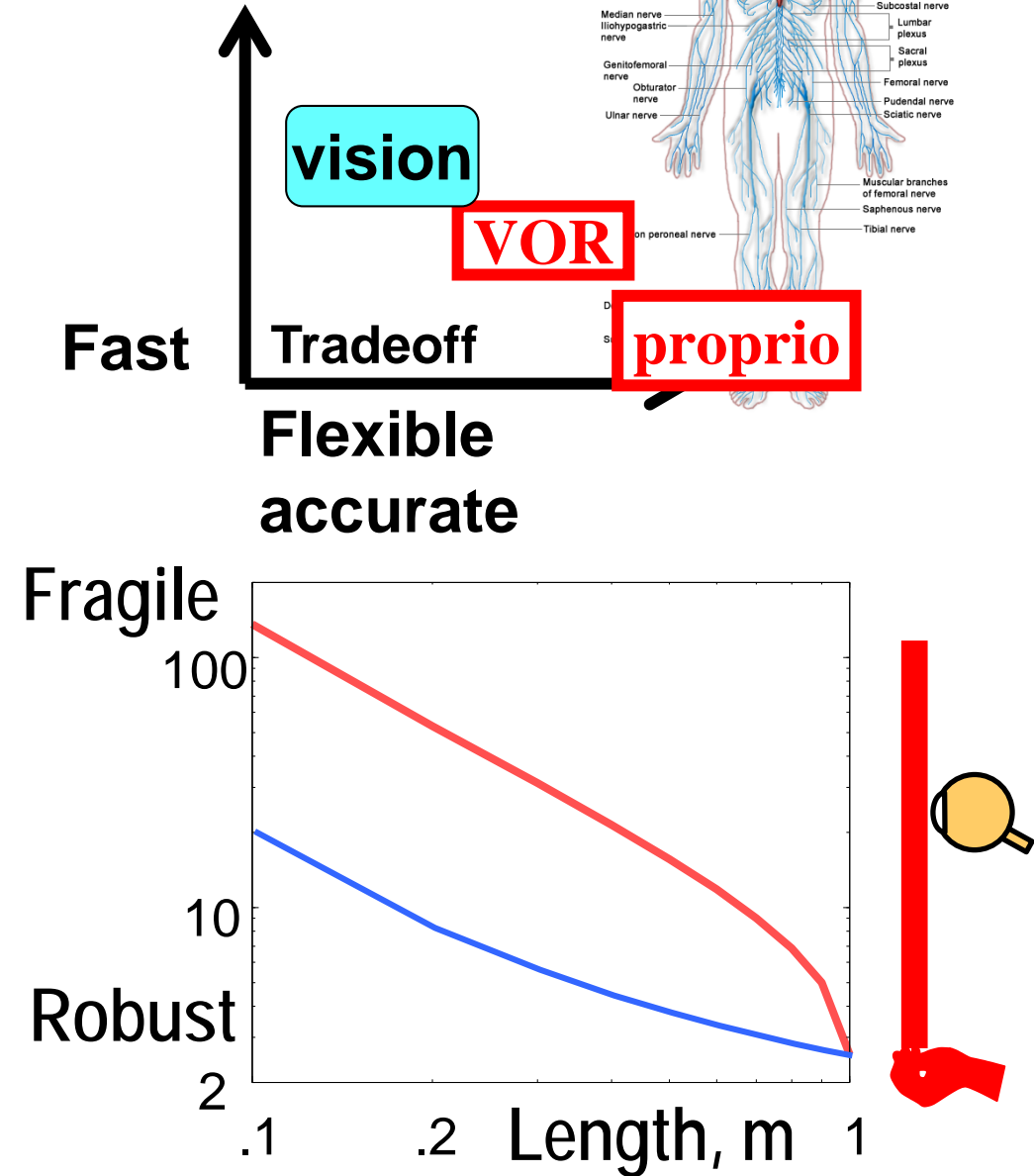
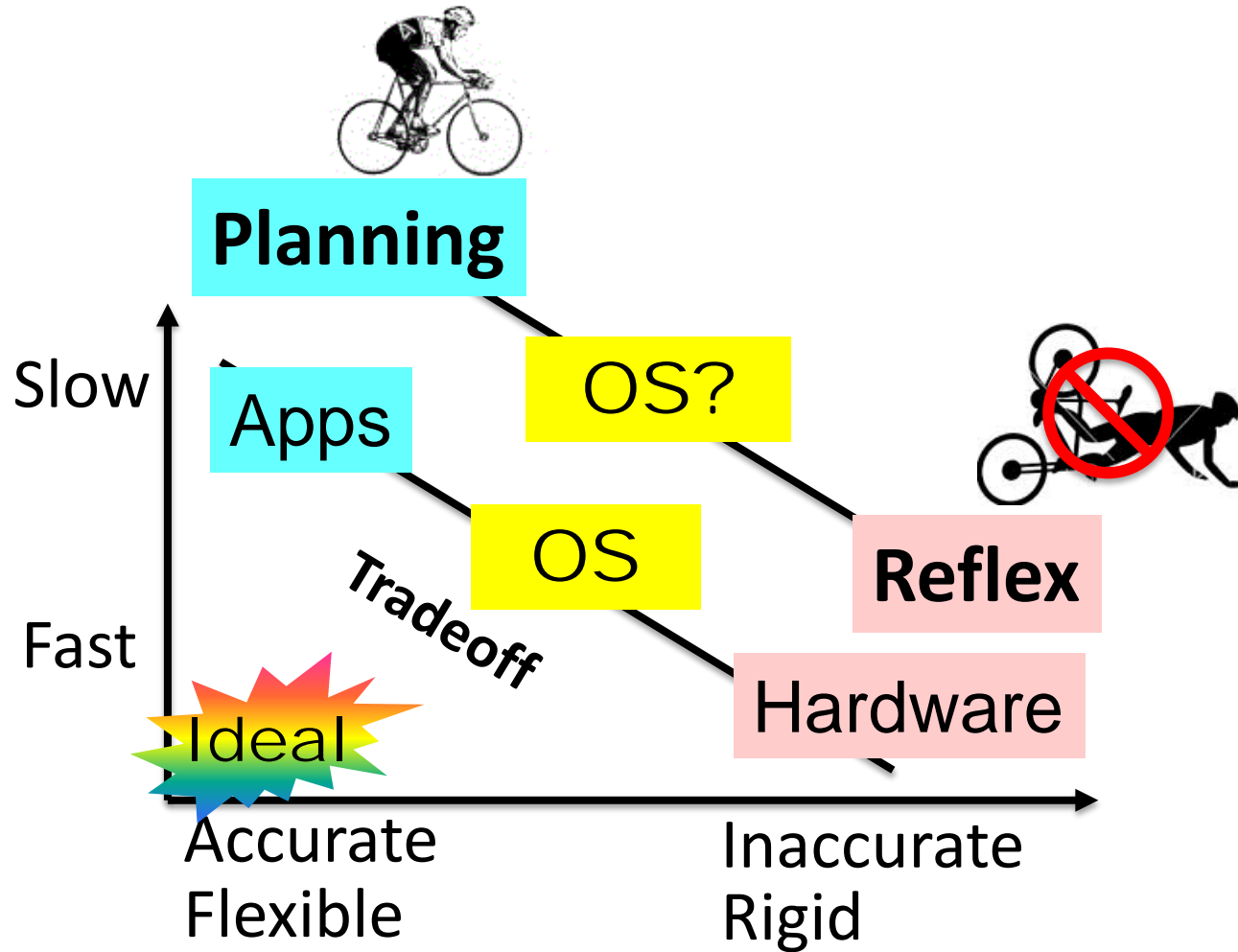
Death

Life



Stabilizable
but fragile

Universal laws and architectures



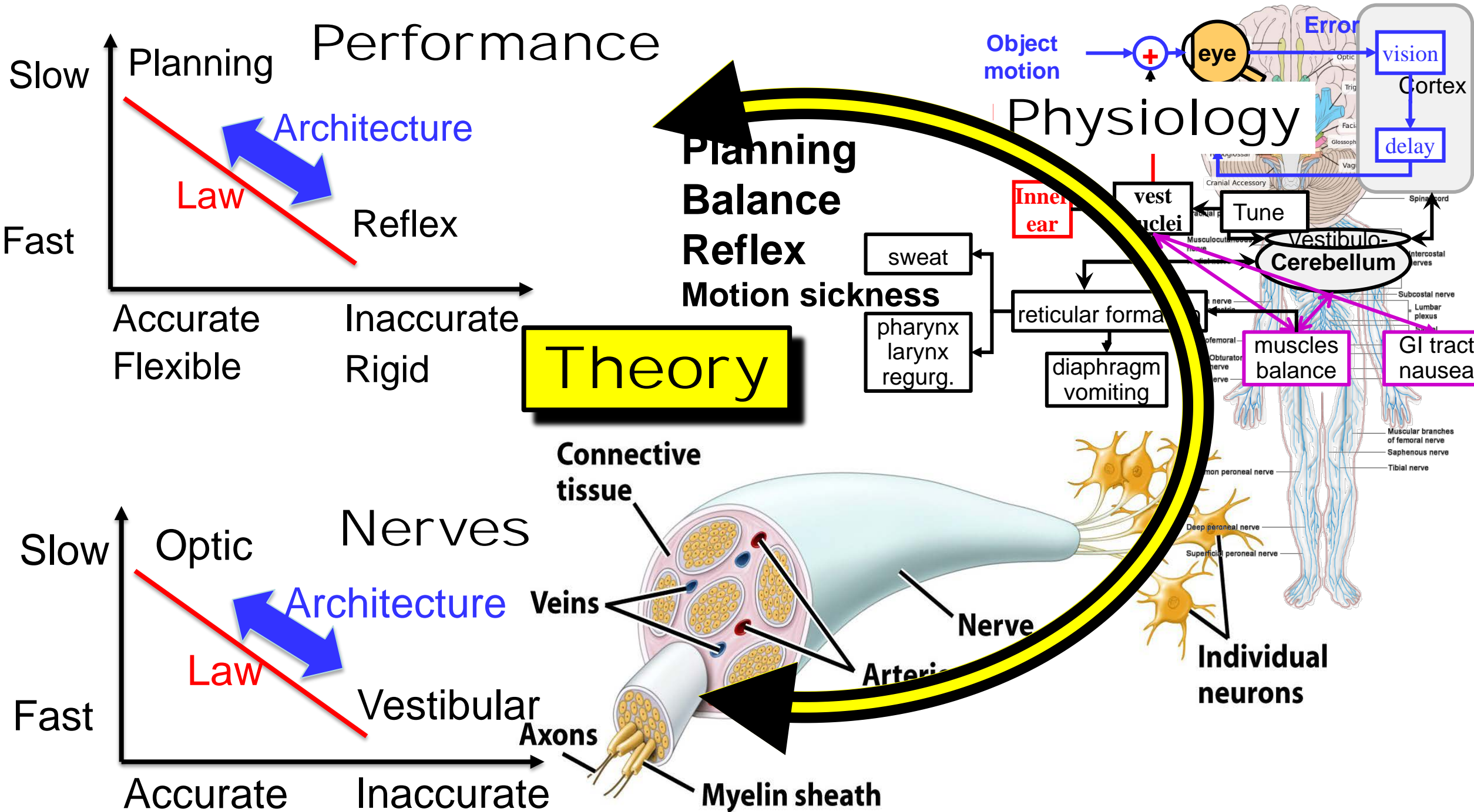
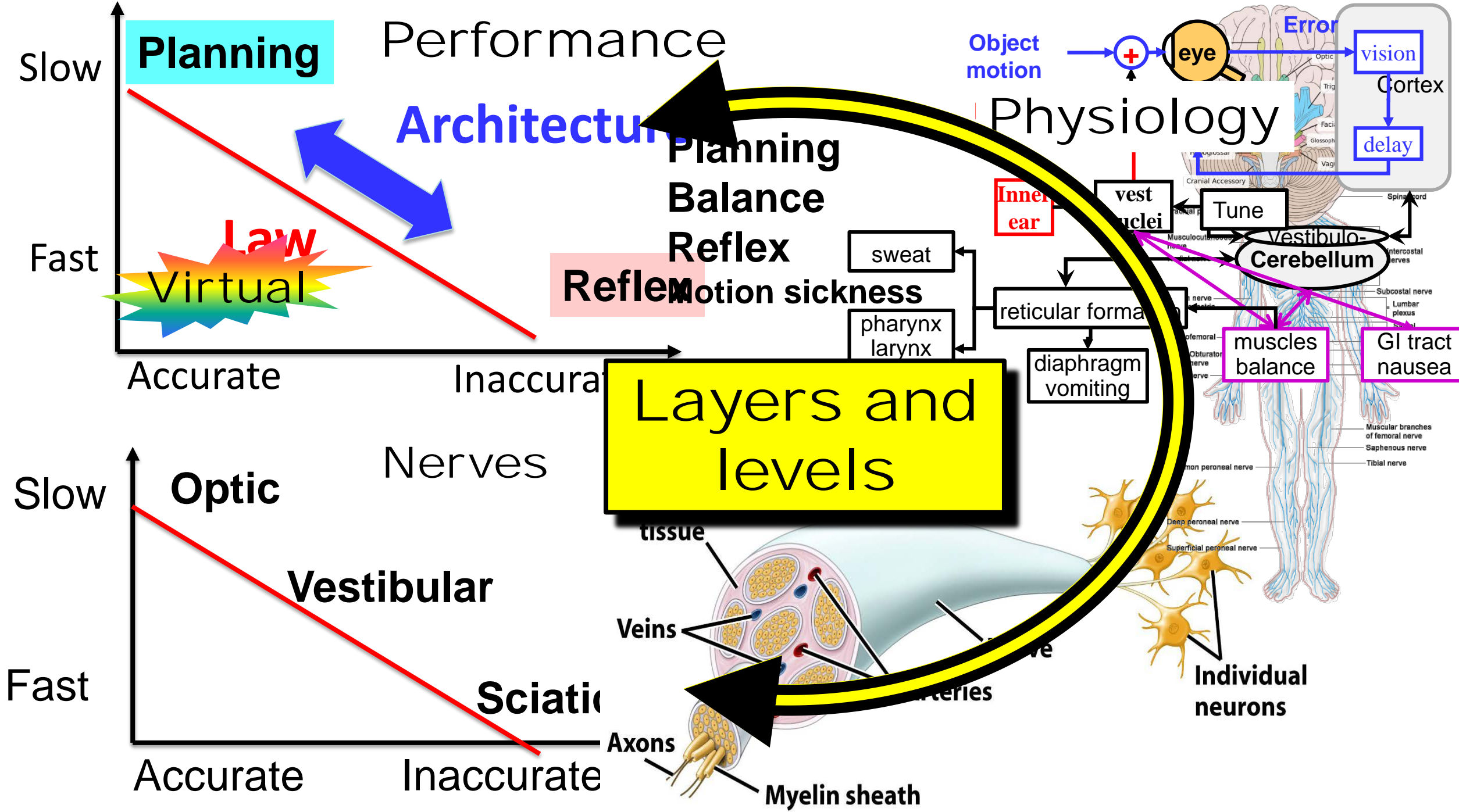


Figure 25-1b Discover Biology 3/e



Physiology

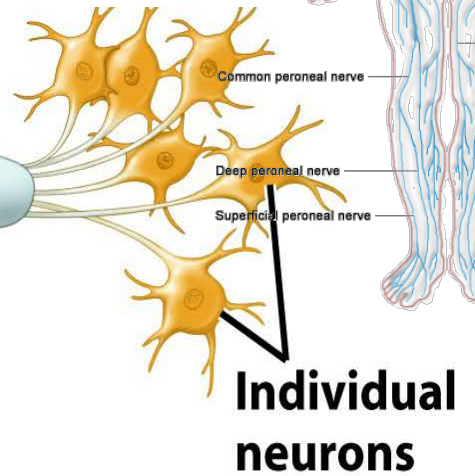
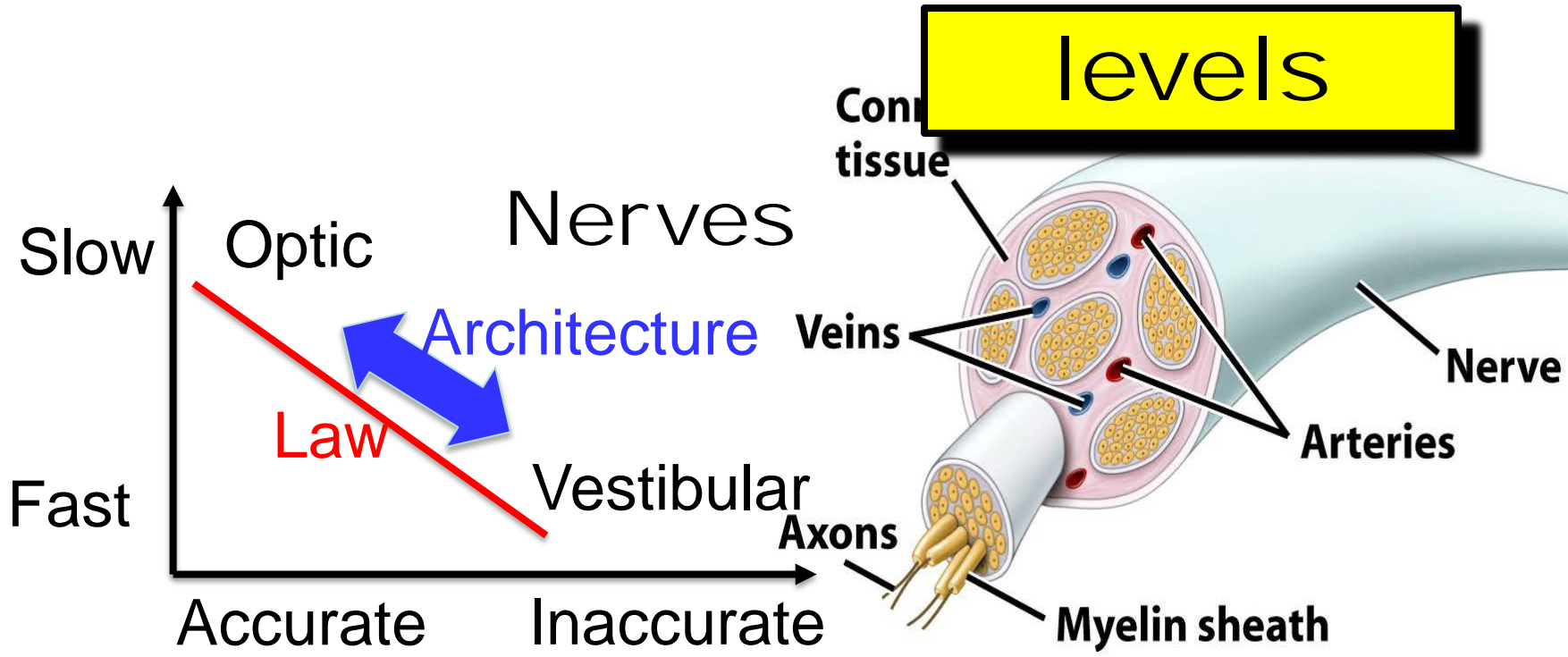
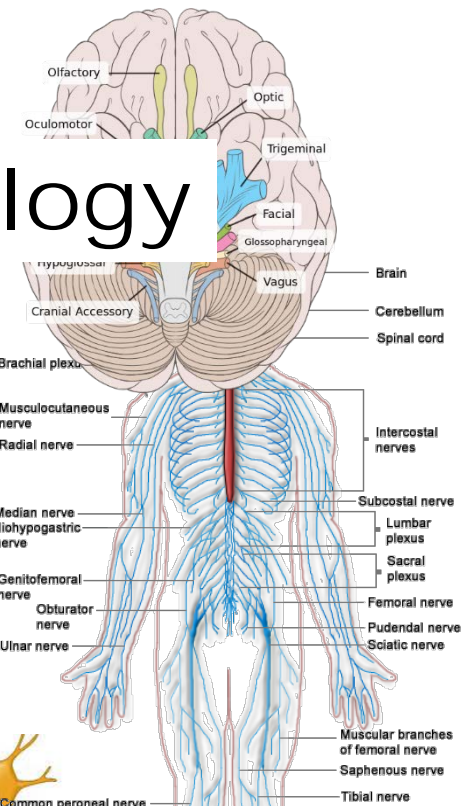


Figure 25-1b Discover Biology 3/e

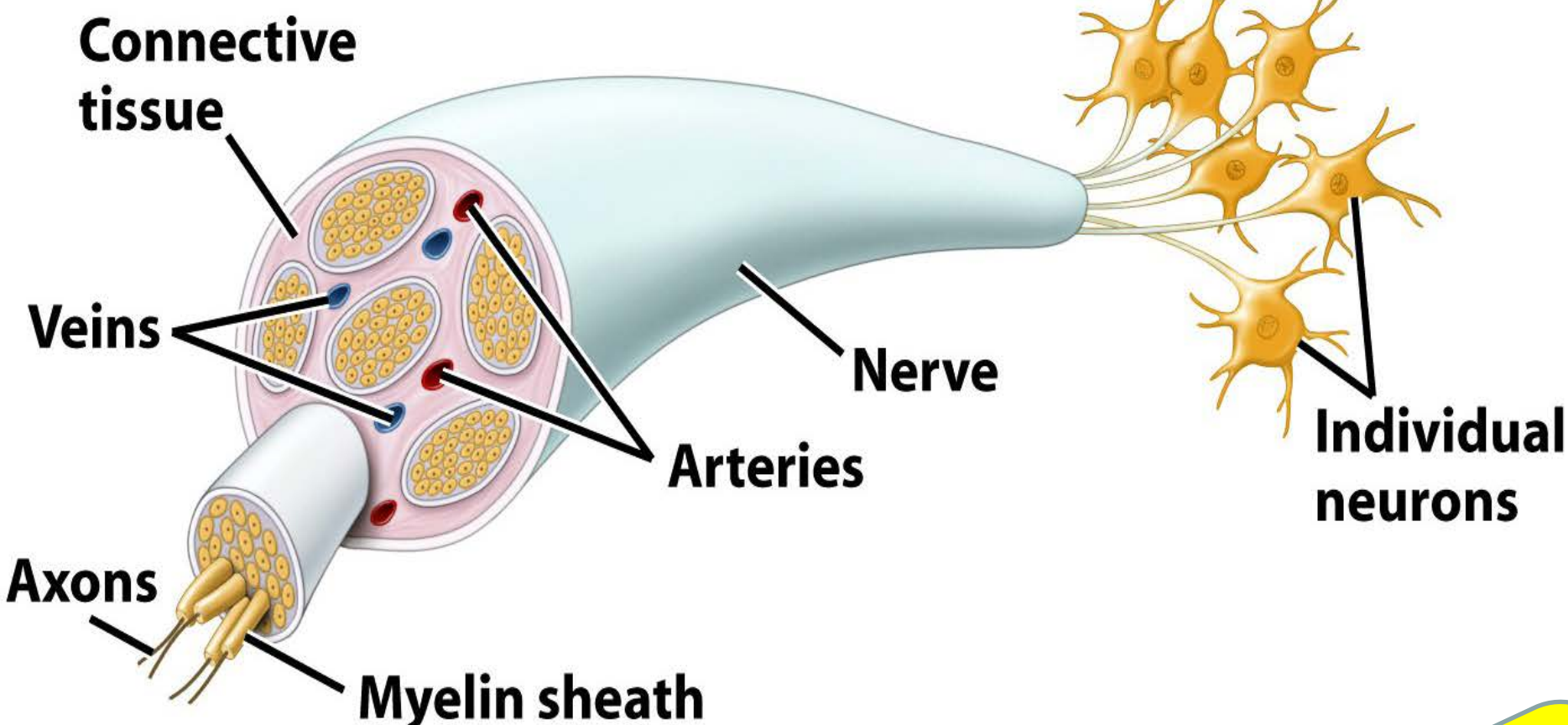
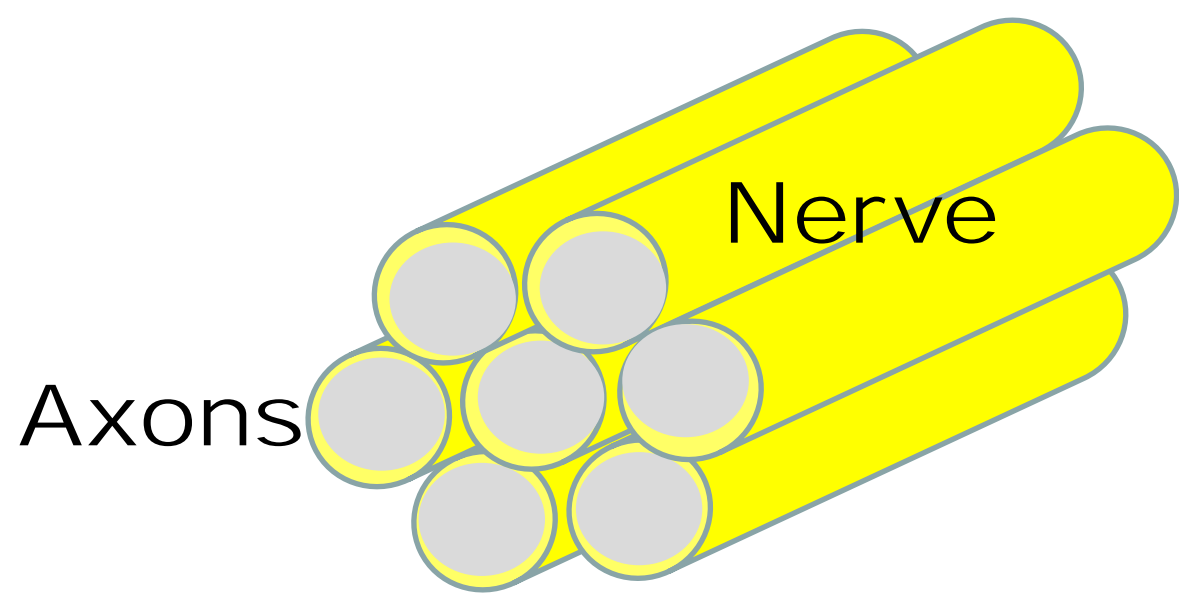


Figure 25-1b Discover Biology 3/e
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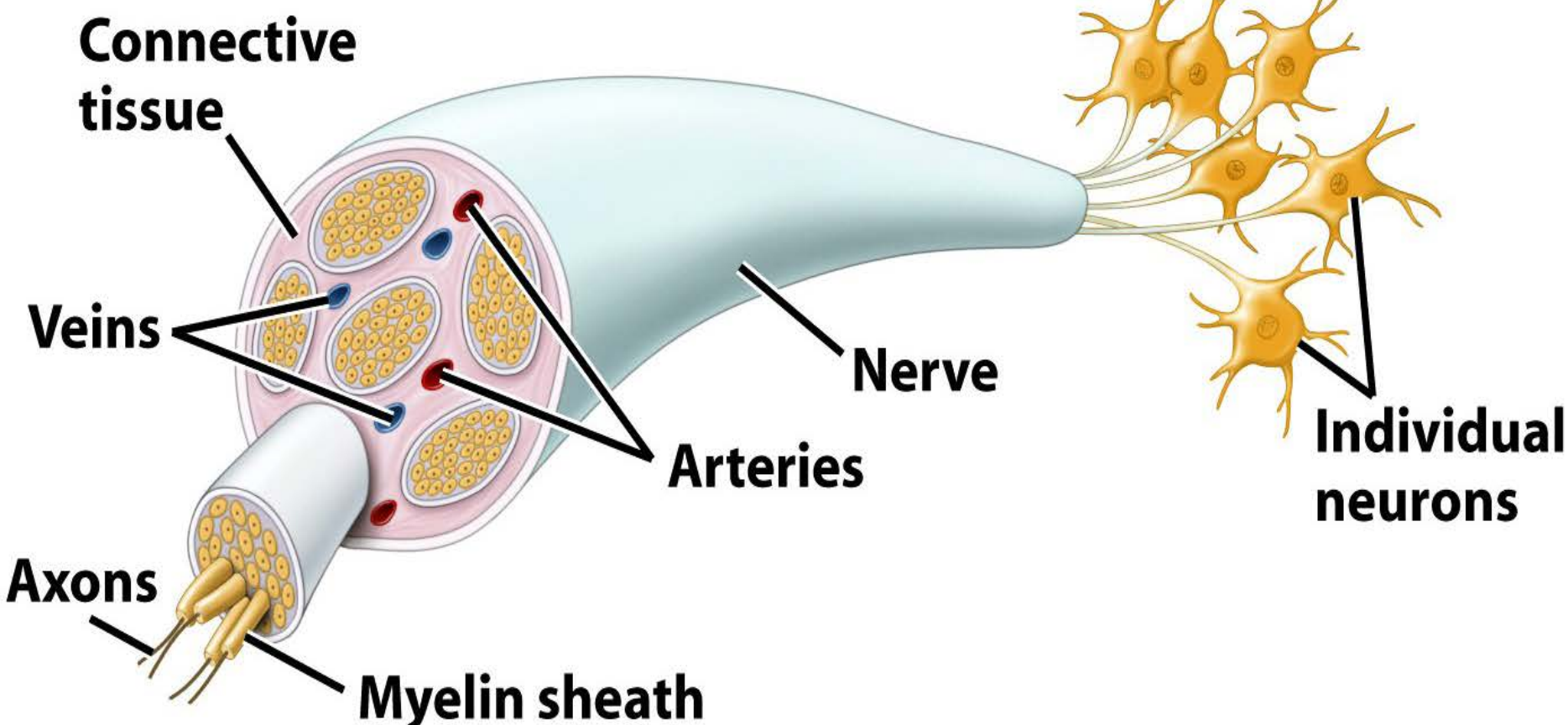
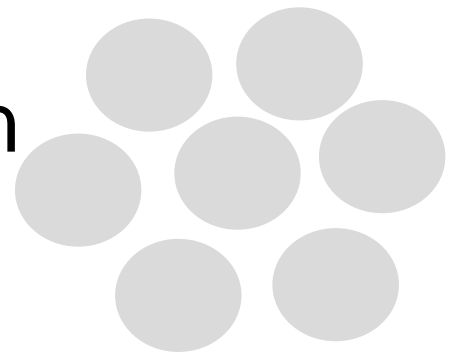
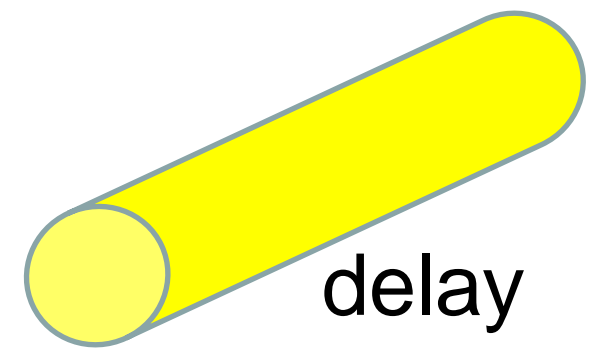


Figure 25-1b Discover Biology 3/e
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quantization



Axons



delay

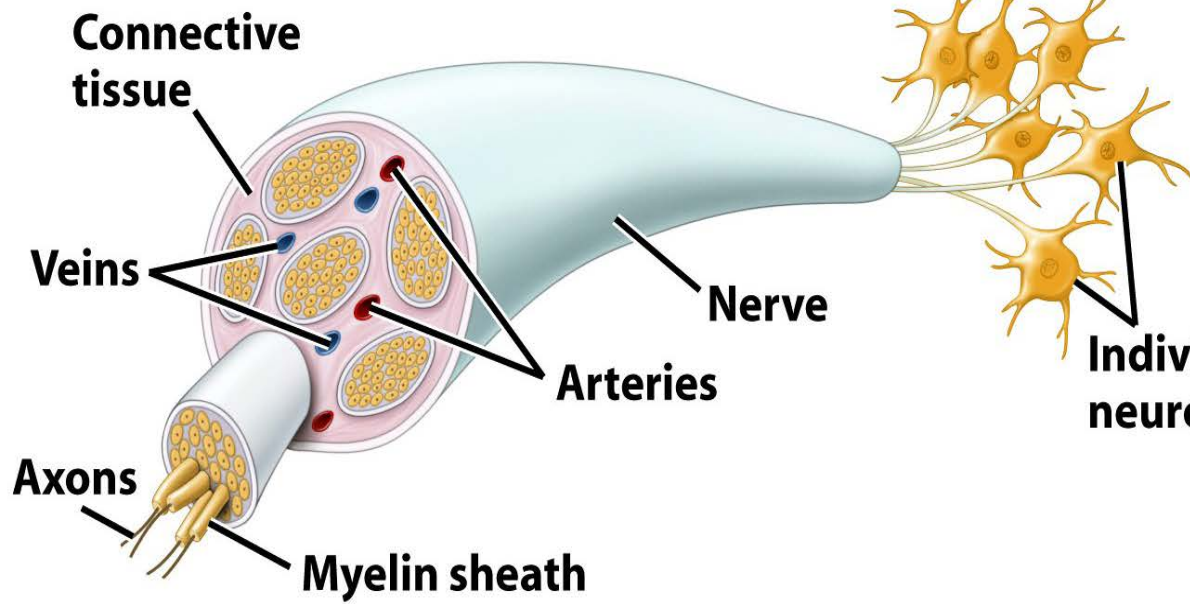
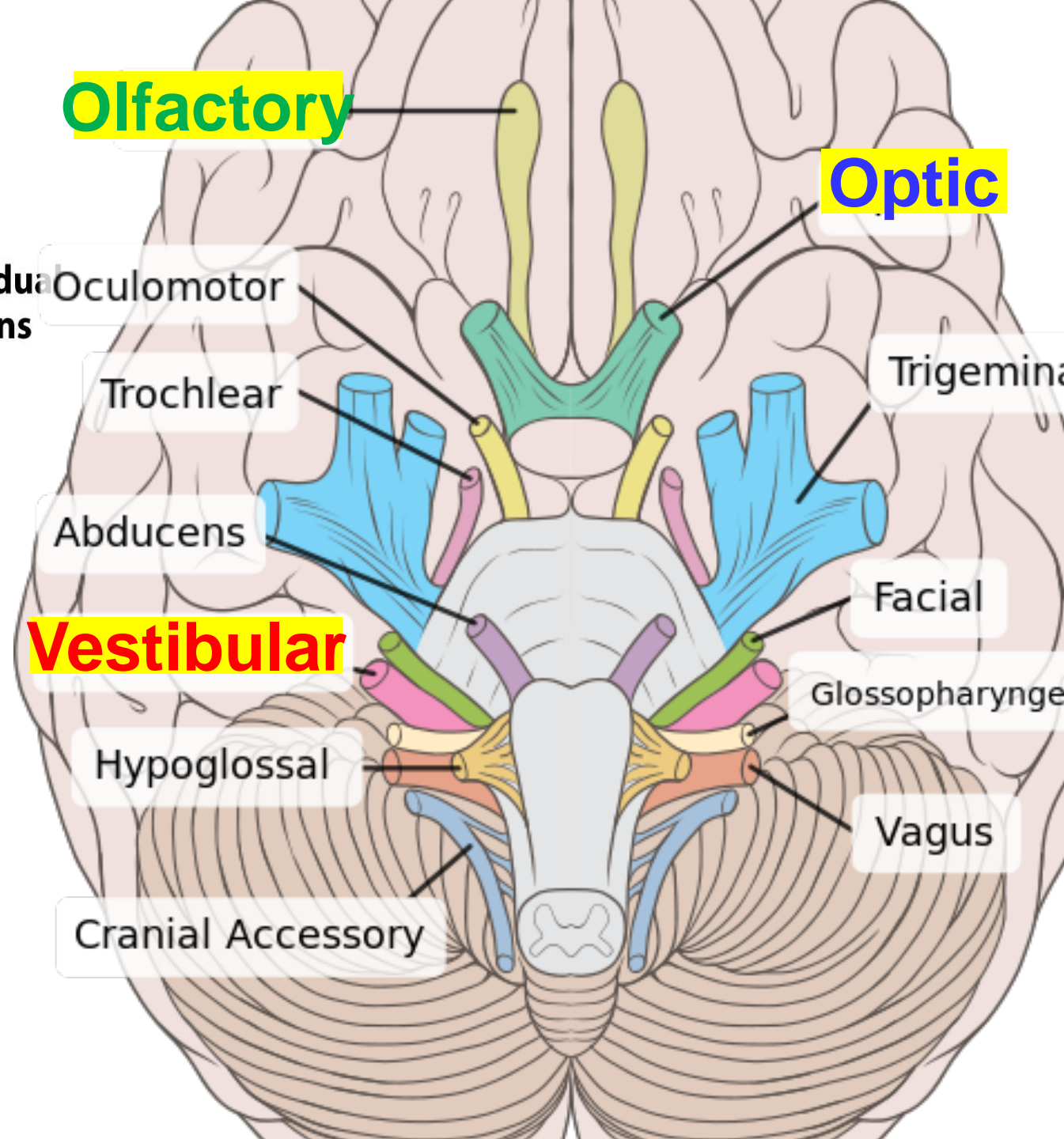


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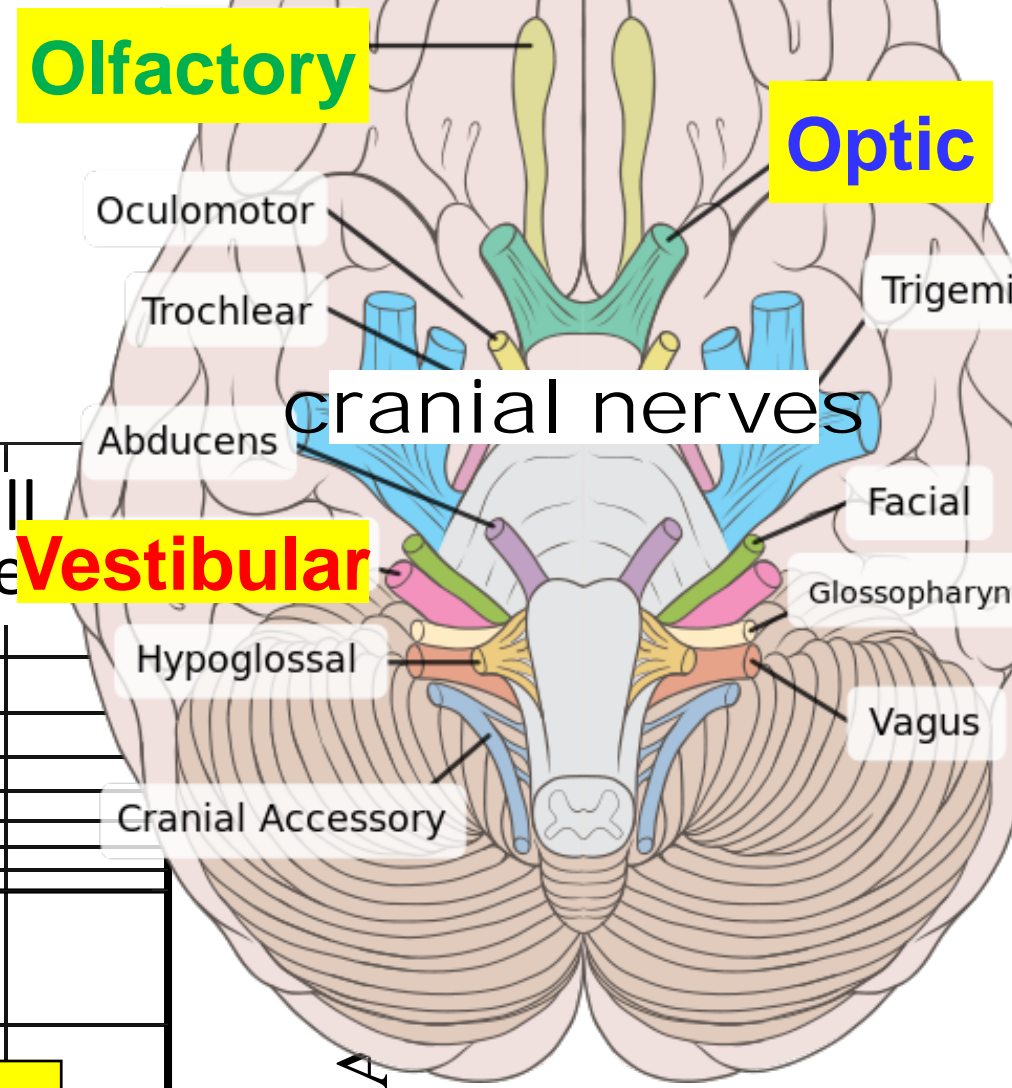
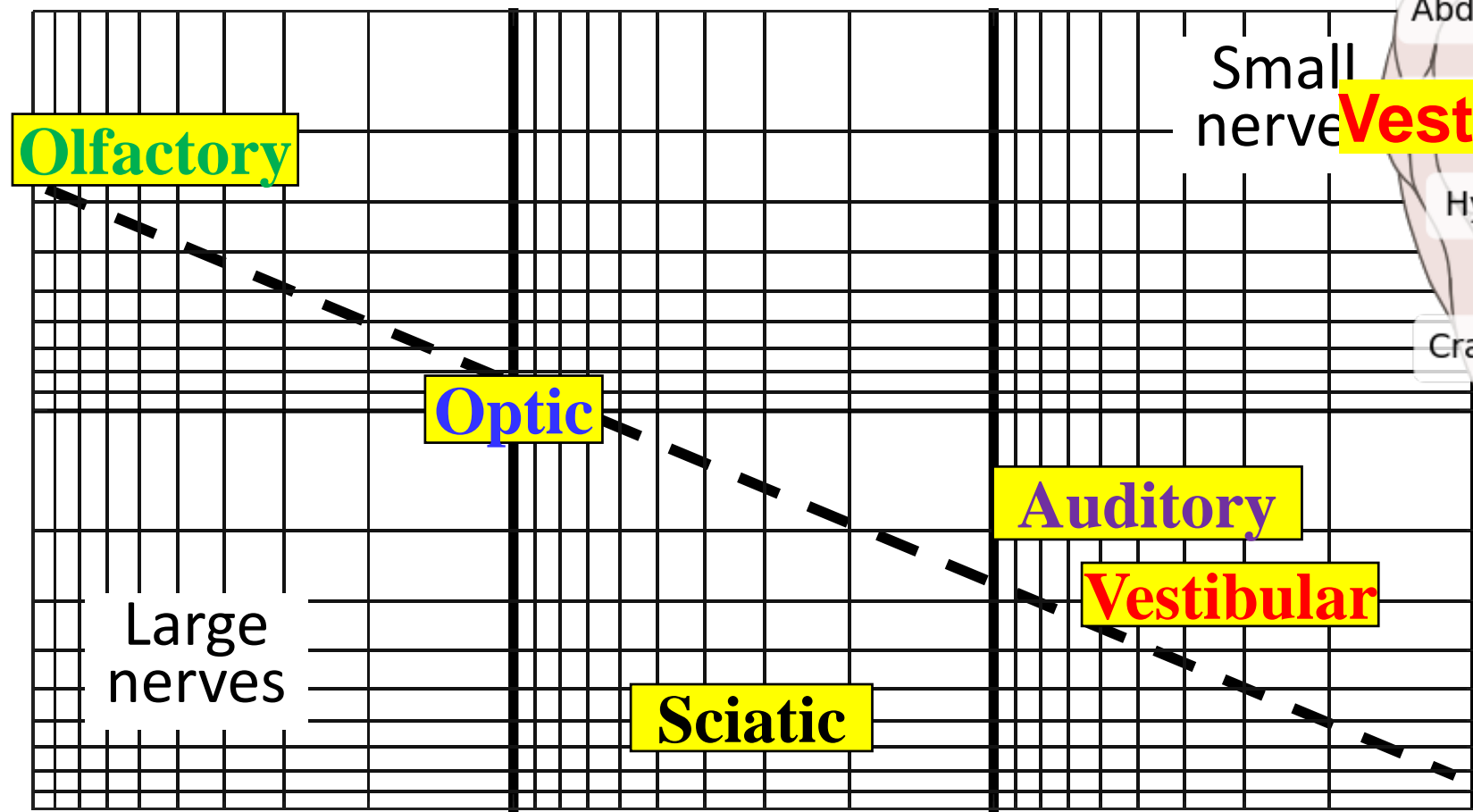


cranial nerves

- similar diameters
- diverse lengths
- diverse composition
- bottlenecks?

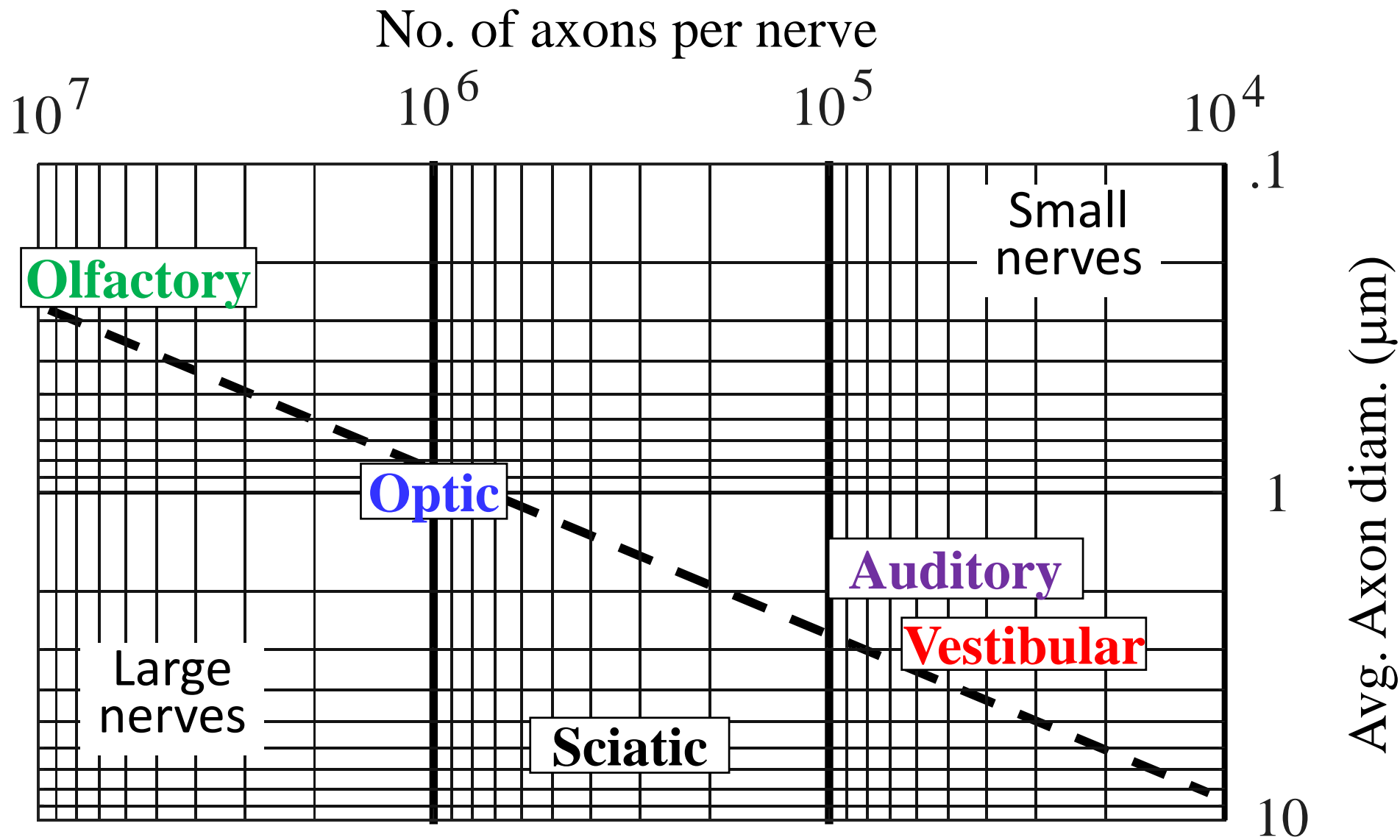
No. of axons per nerve

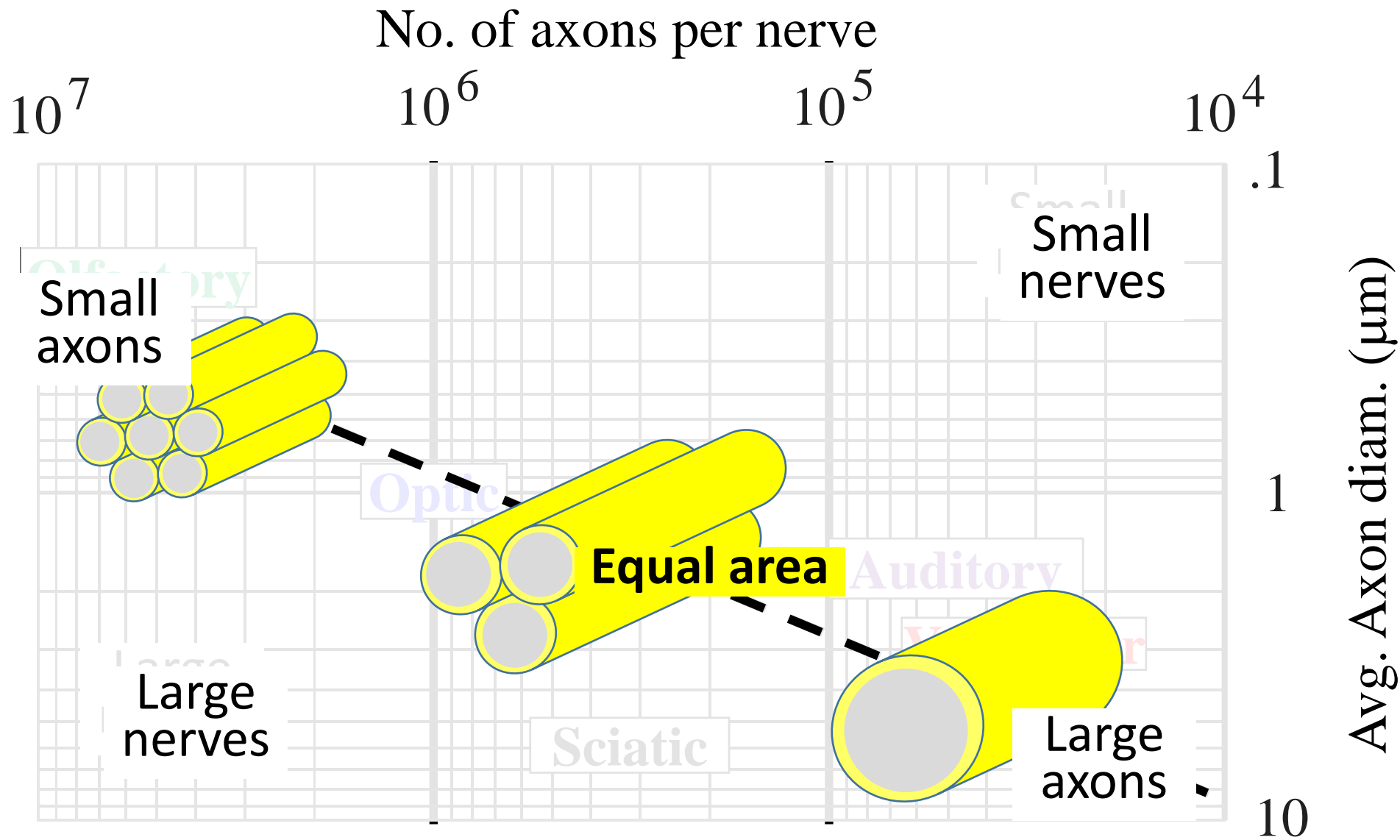
10^7 10^6 10^5

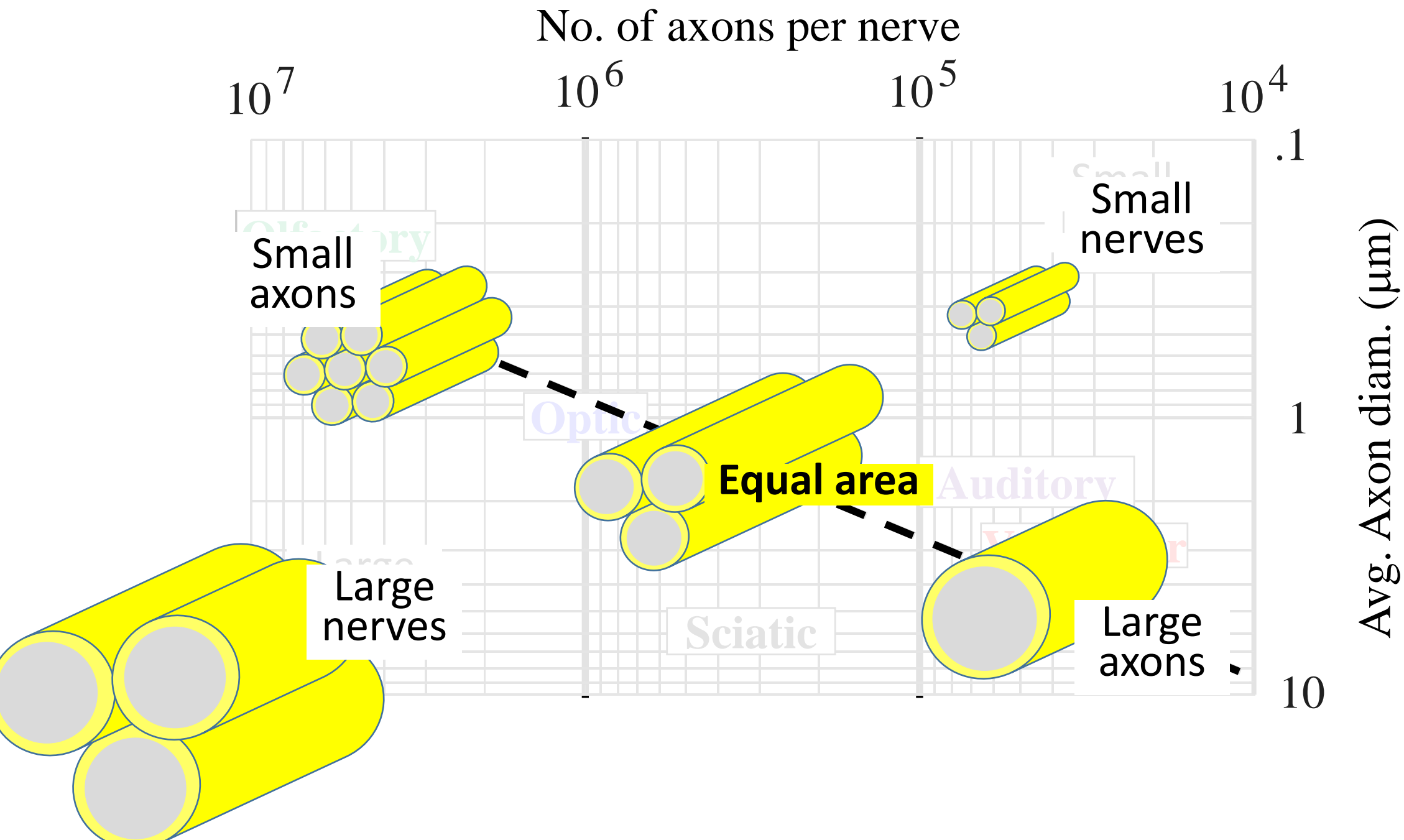


Avg. A

10







No. of axons per nerve

10^7

10^6

10^5

10^4

Small axons

Olfactory

Small nerves

Optic

Equal area

Auditory

Vestibular

Large nerves

Sciatic

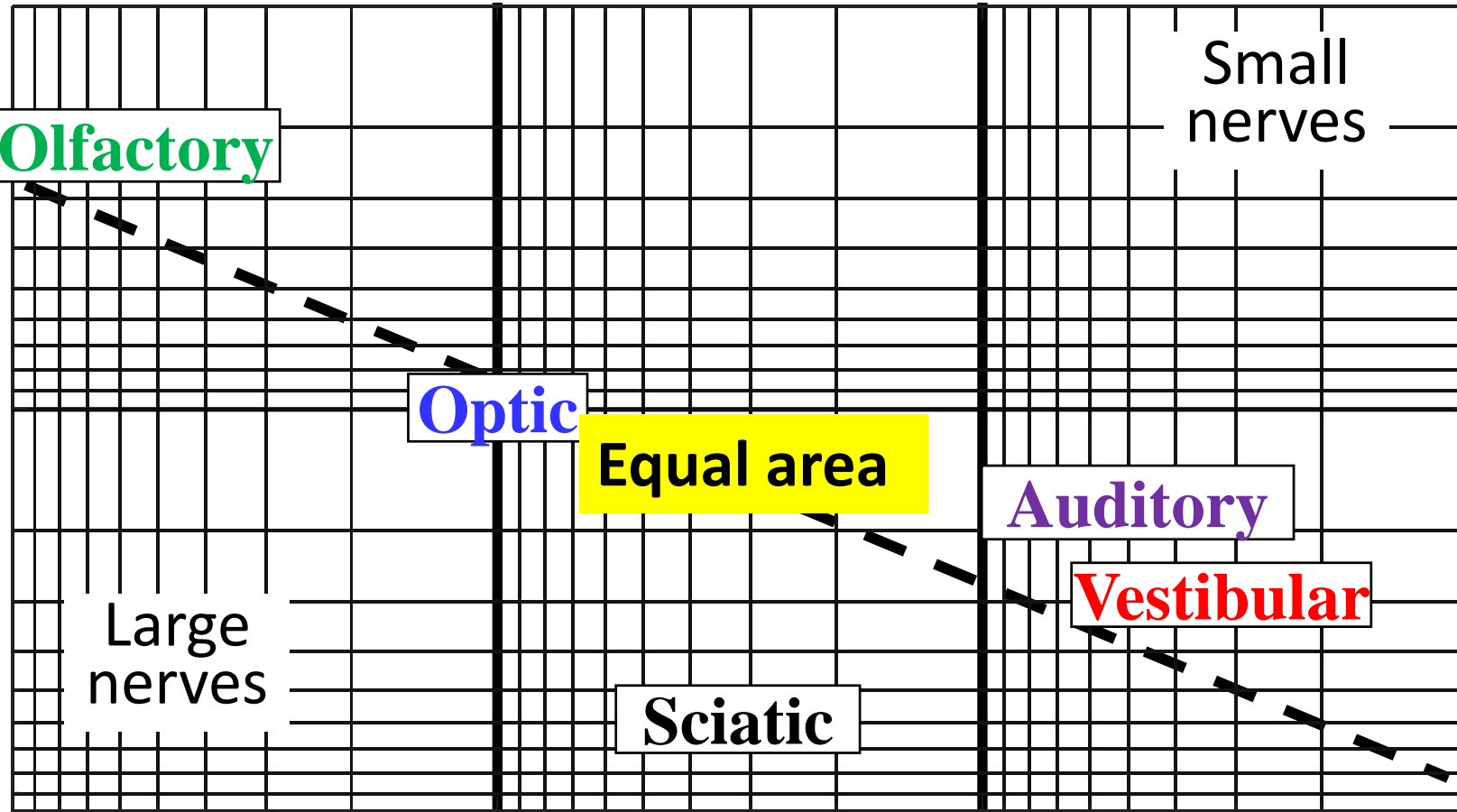
.1

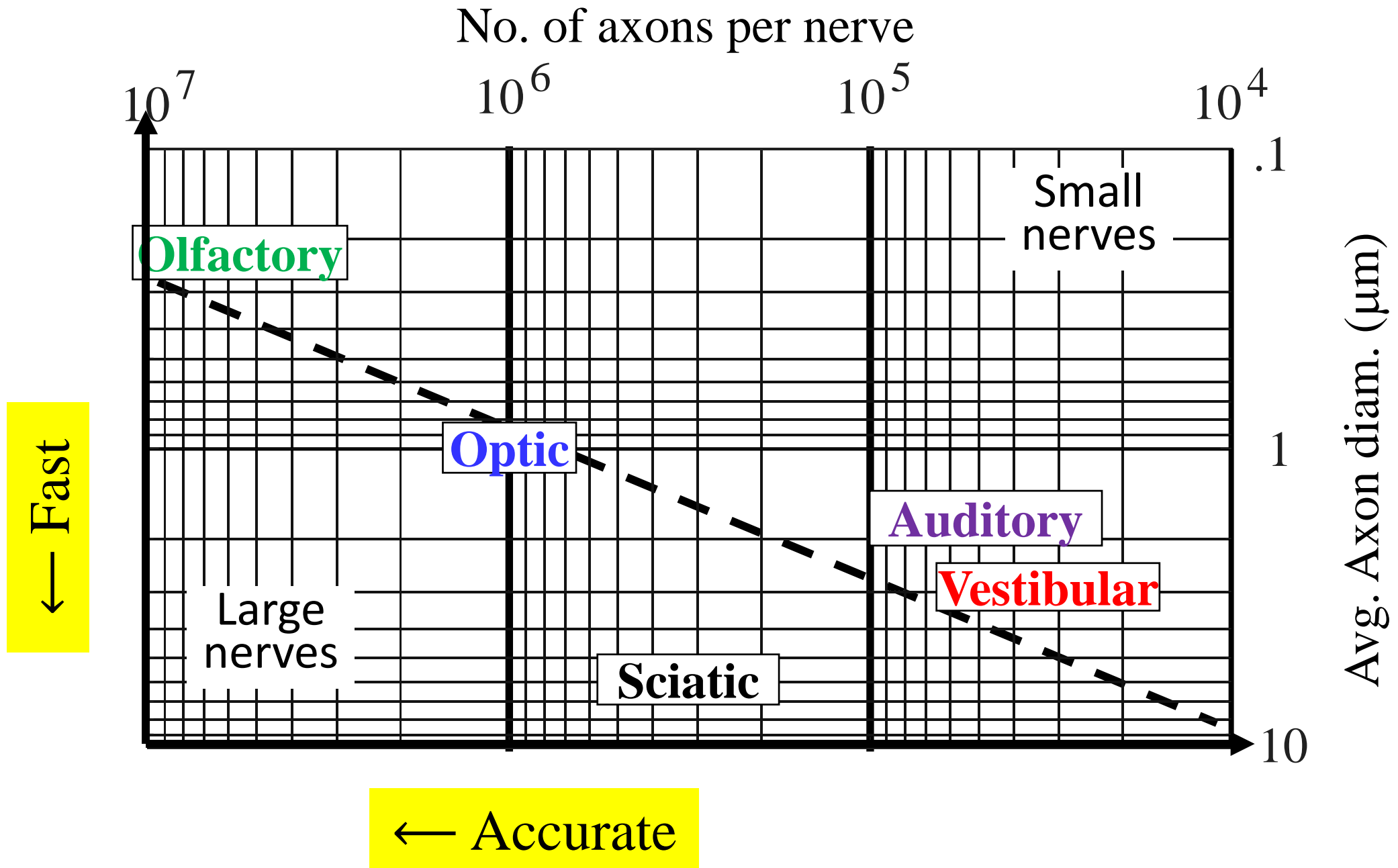
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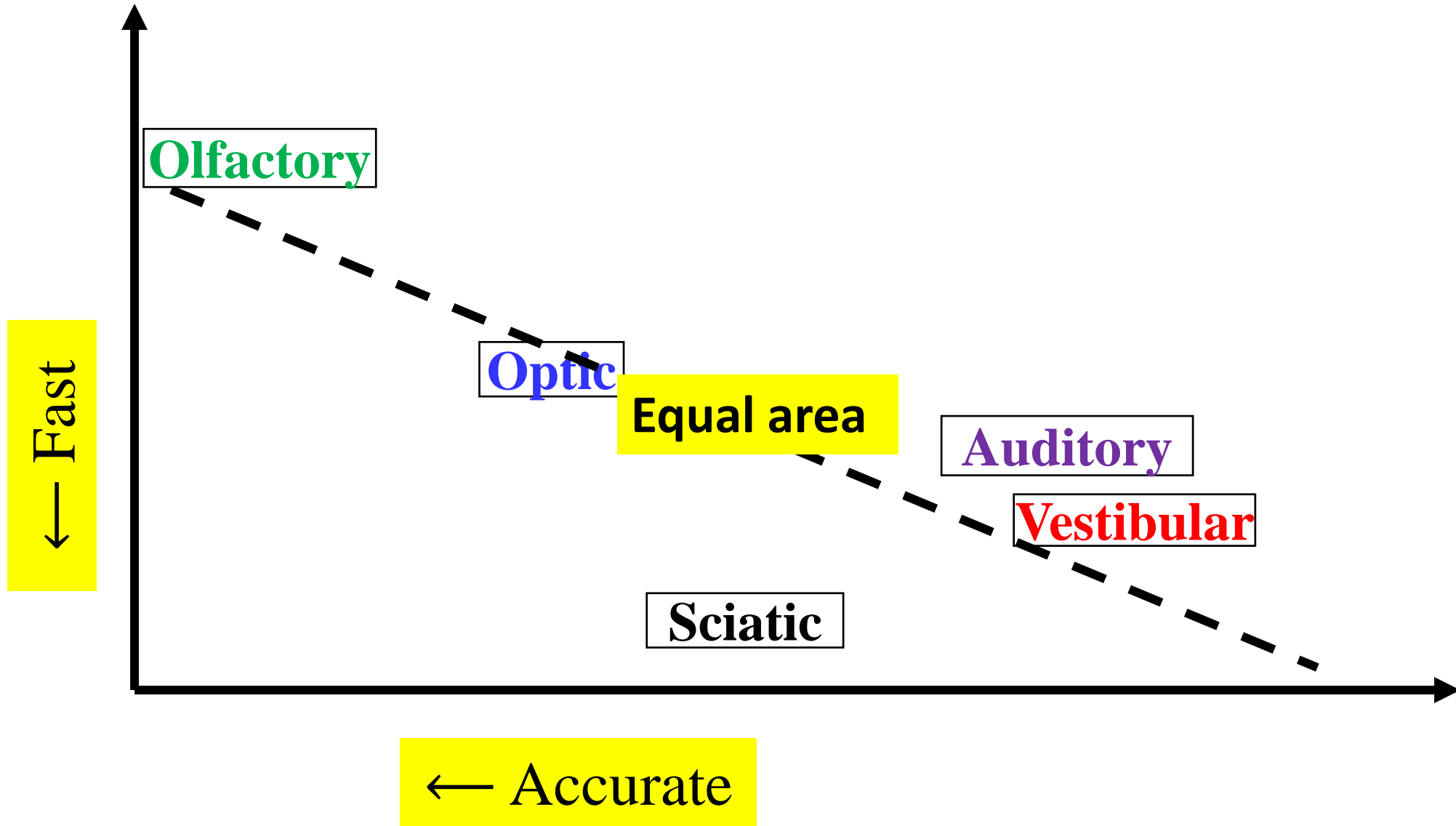
10

Avg. Axon diam. (μm)

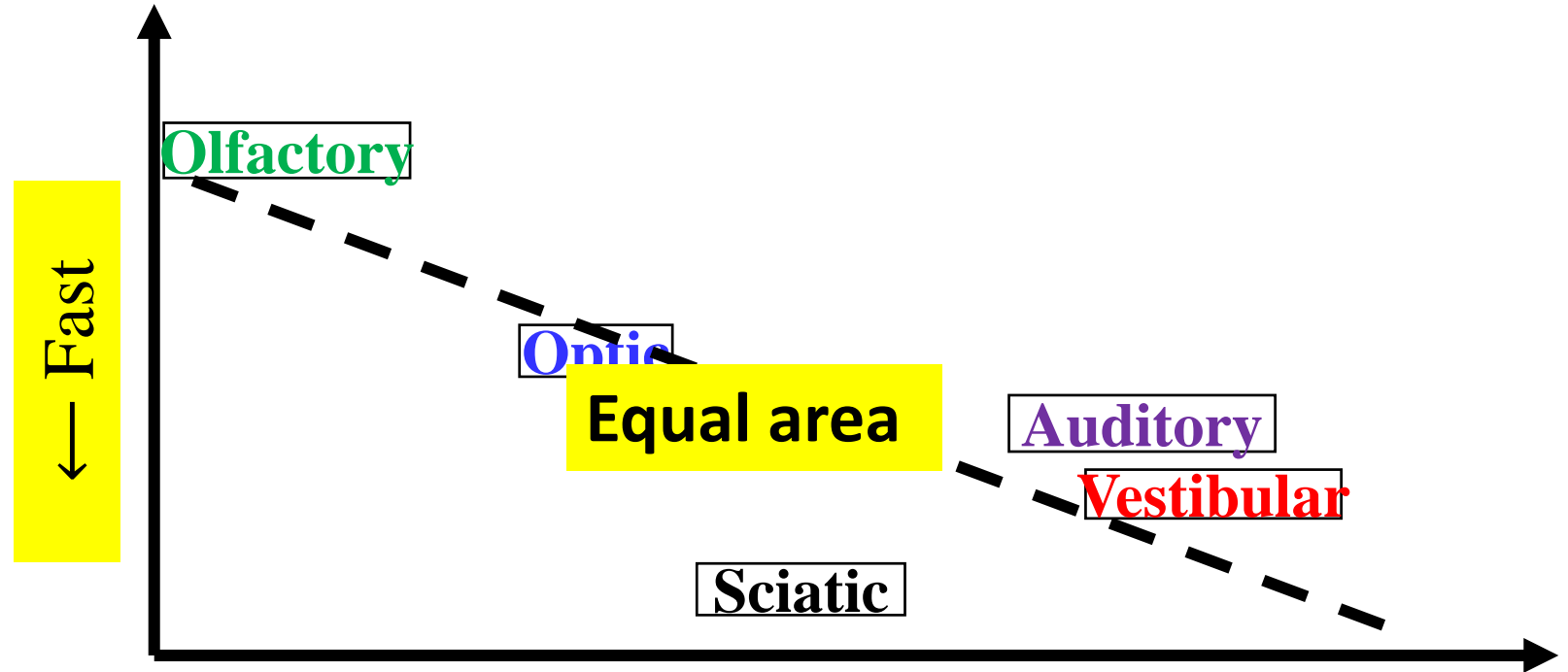
Large axons







log(delay)

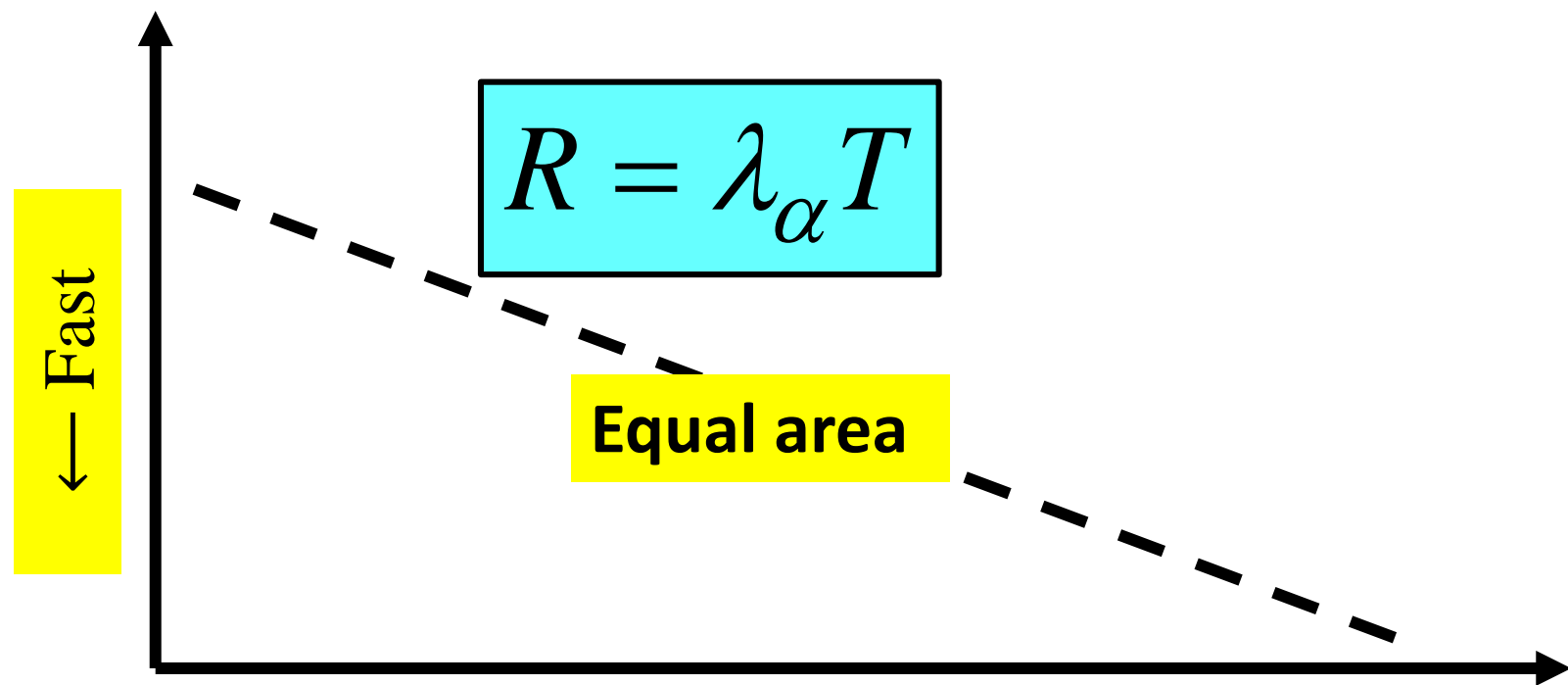


← Fast

← Accurate

$-\log(\text{bandwidth})$

$\log(T)$
 $\log(\text{delay})$



$$R = \lambda_{\alpha} T$$

Equal area

← Fast

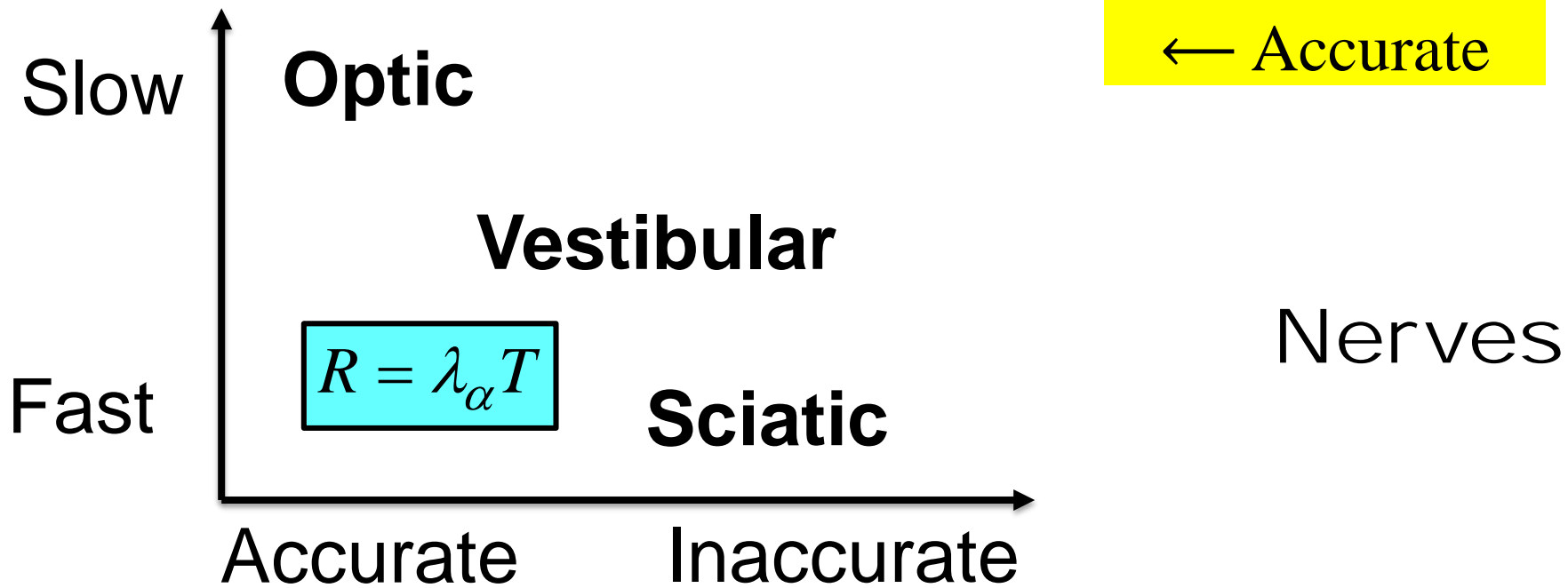
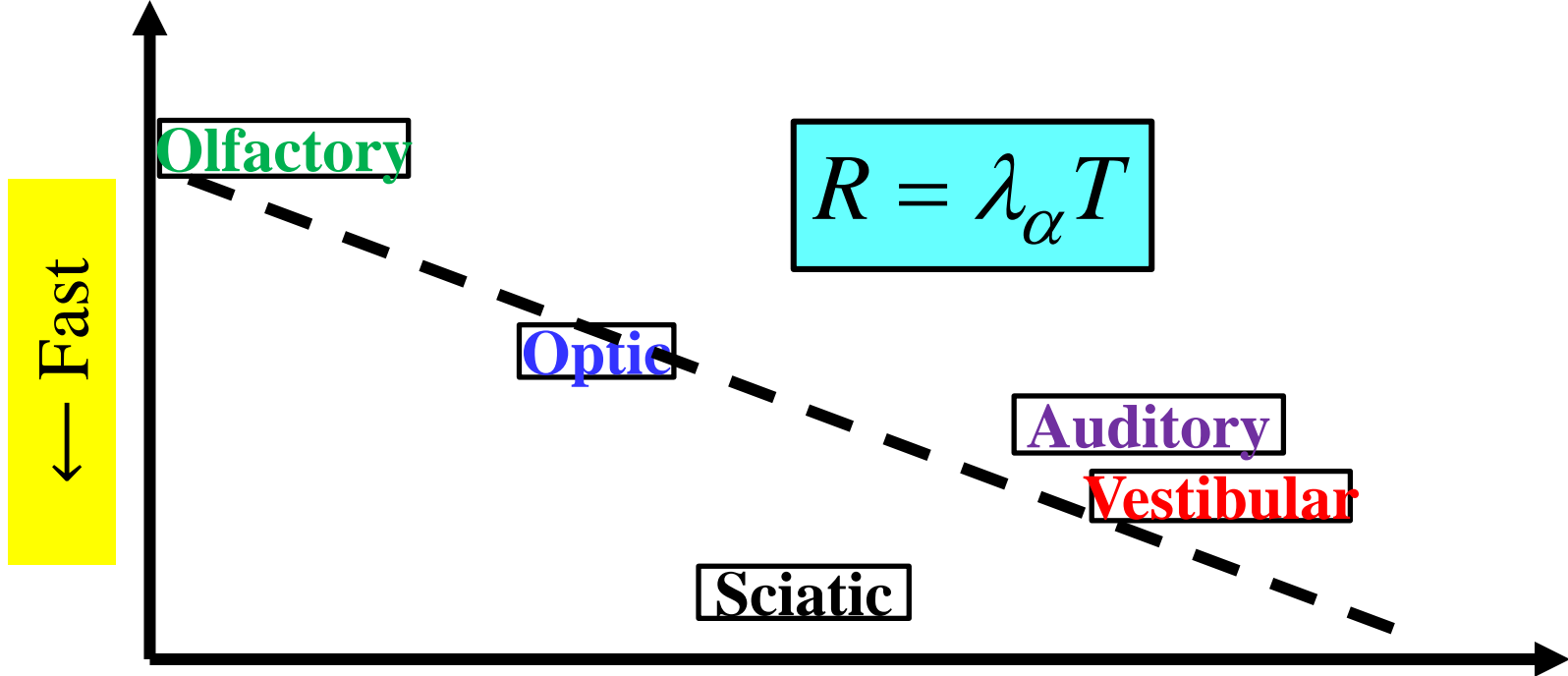
← Accurate

$$\lambda_{\alpha} \propto \text{area}$$

$-\log(R)$
 $-\log(\text{bandwidth})$

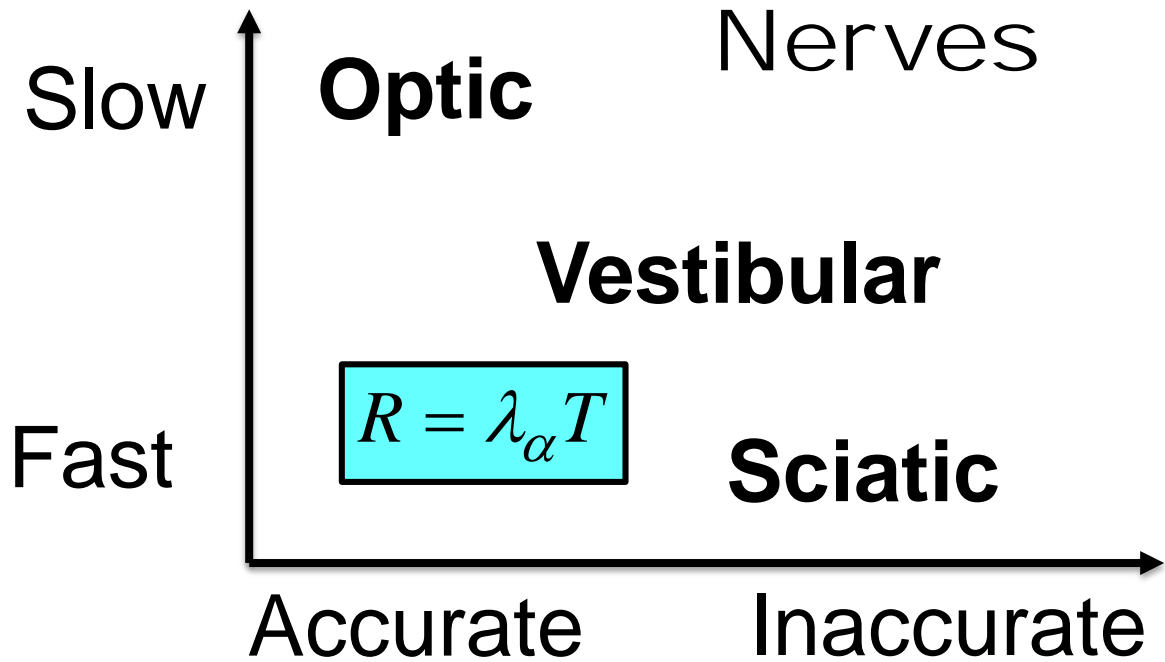
Simon Laughlin
Terry Sejnowski

Speed vs Accuracy



Why?

Extremely Diverse



Physiology

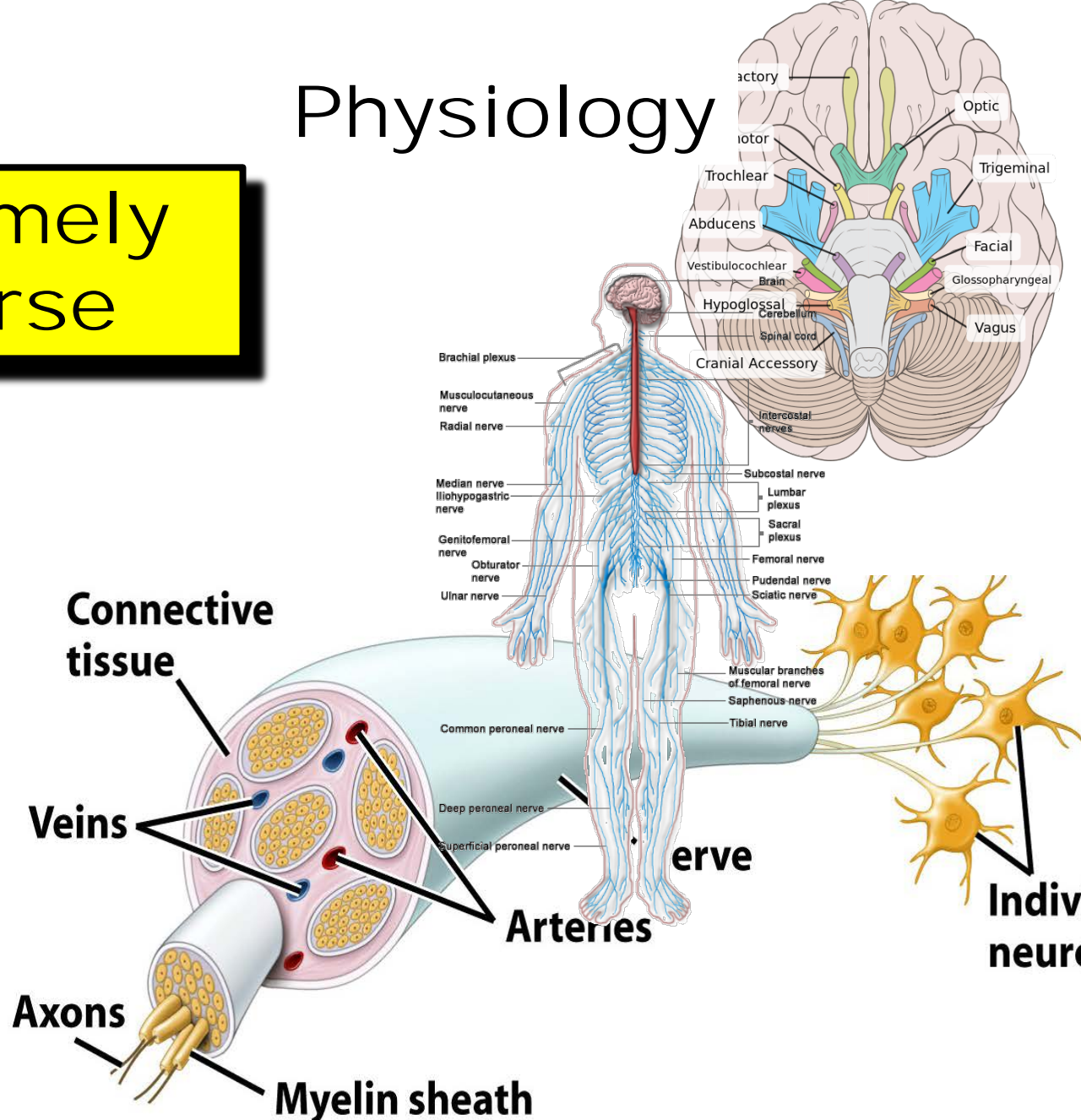


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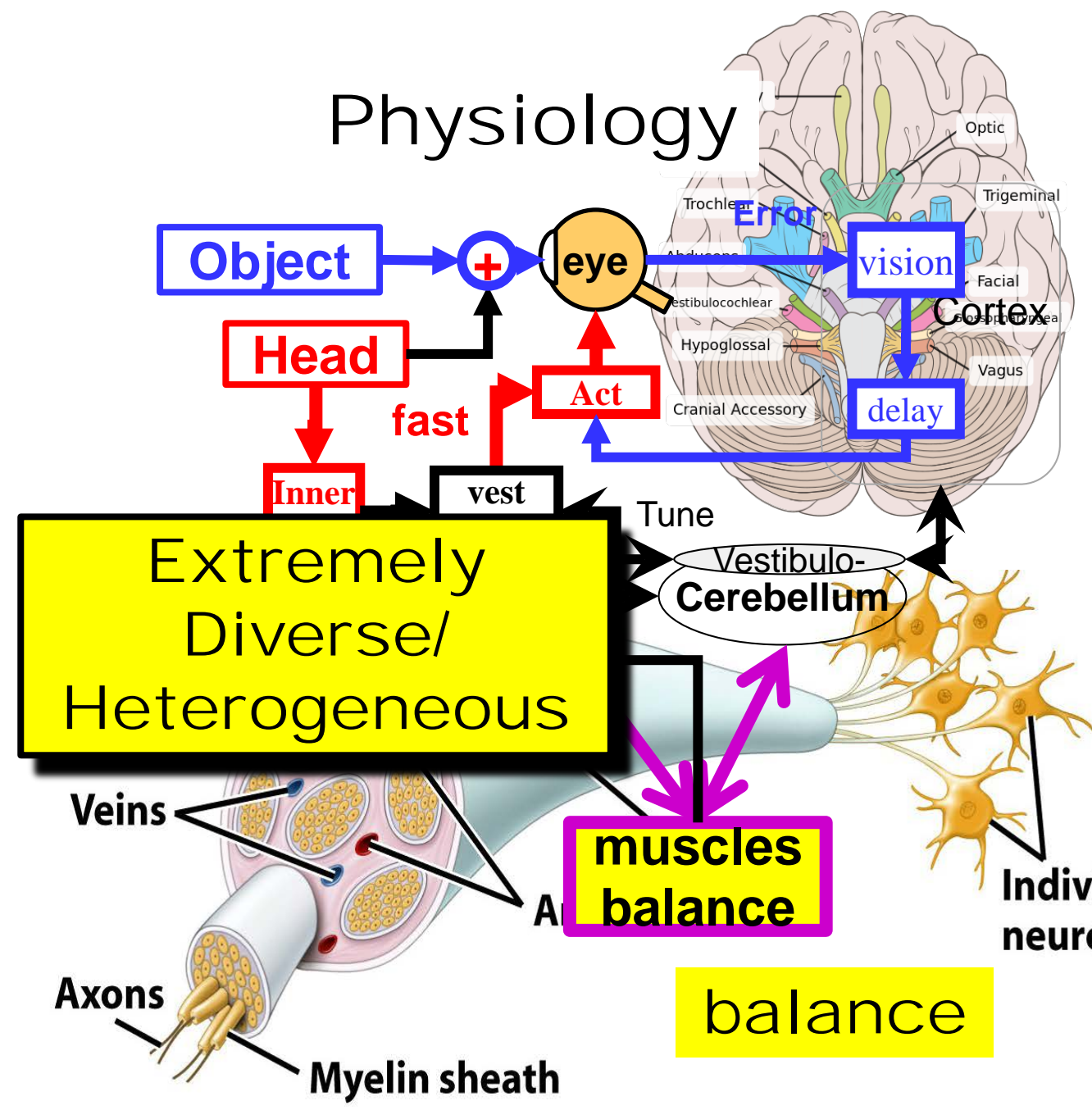
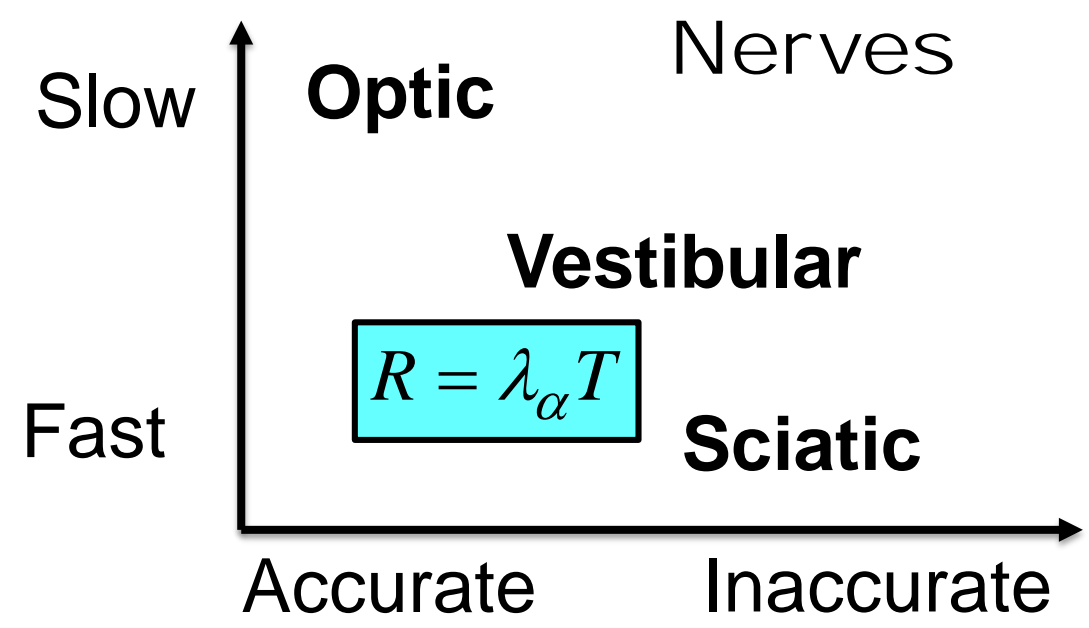
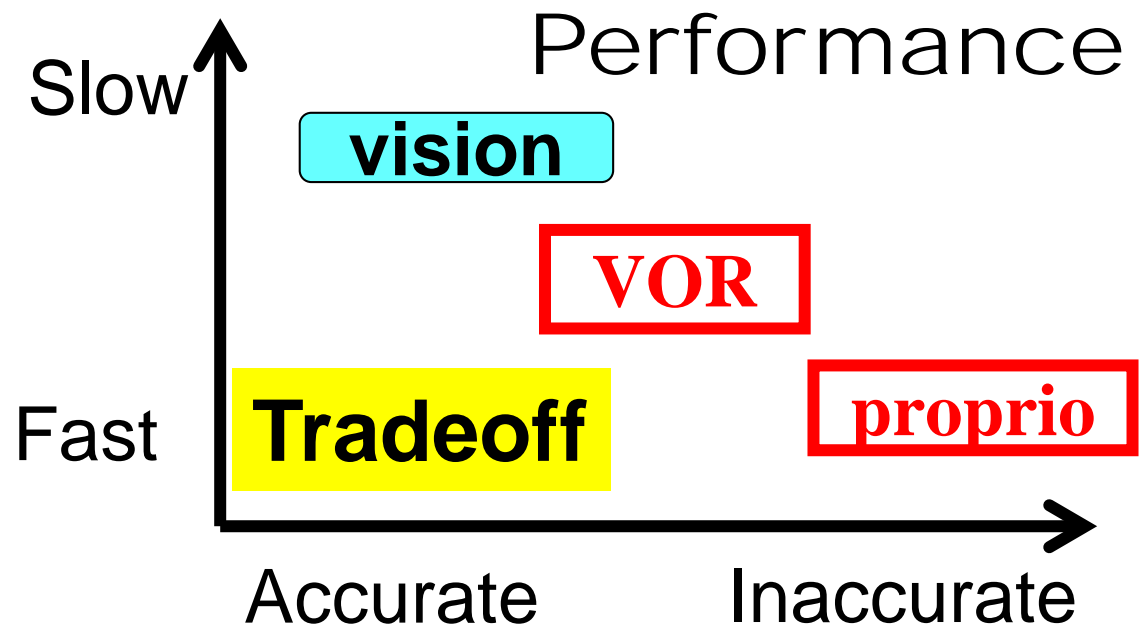


Figure 25-1b Discover Biology 3/e
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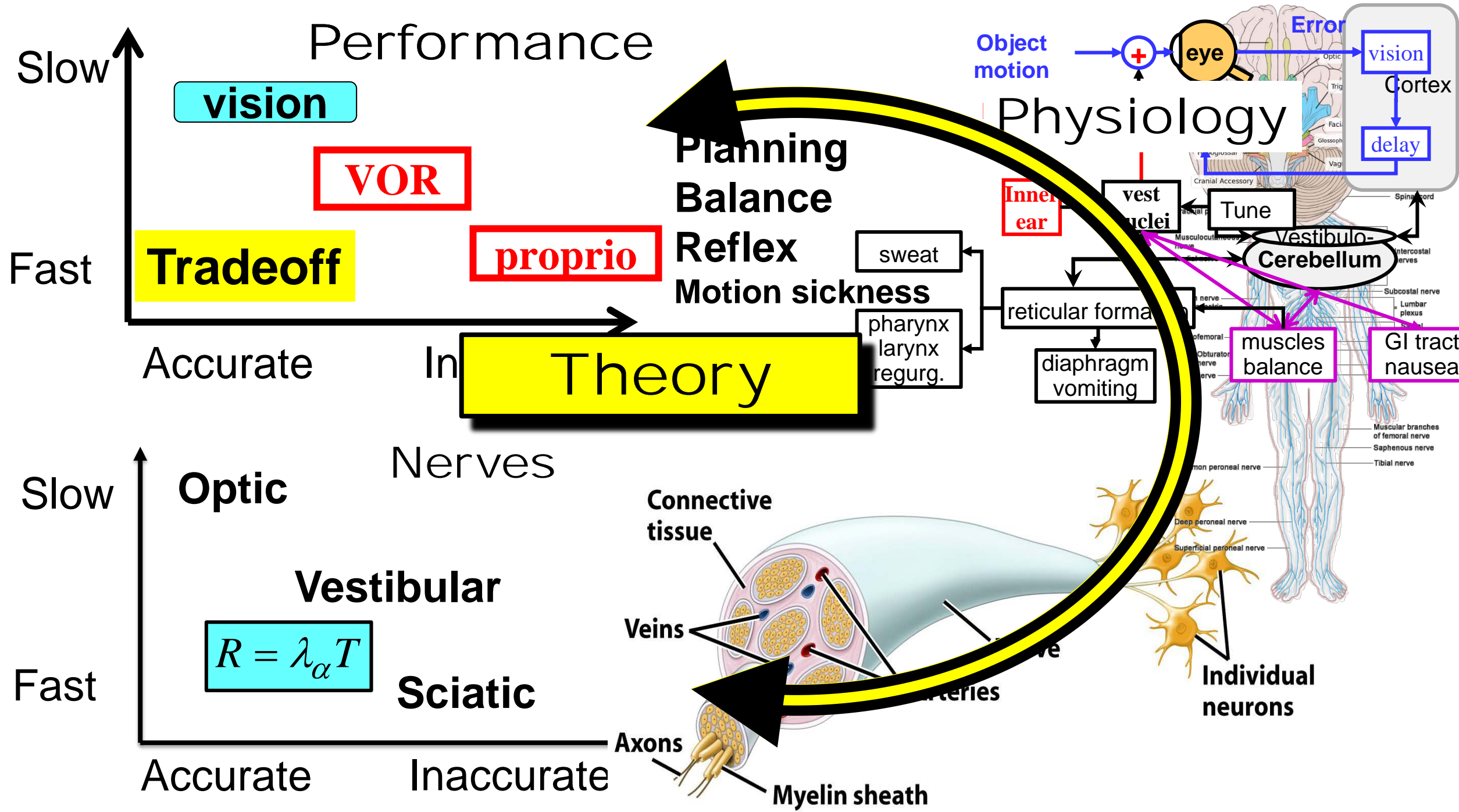
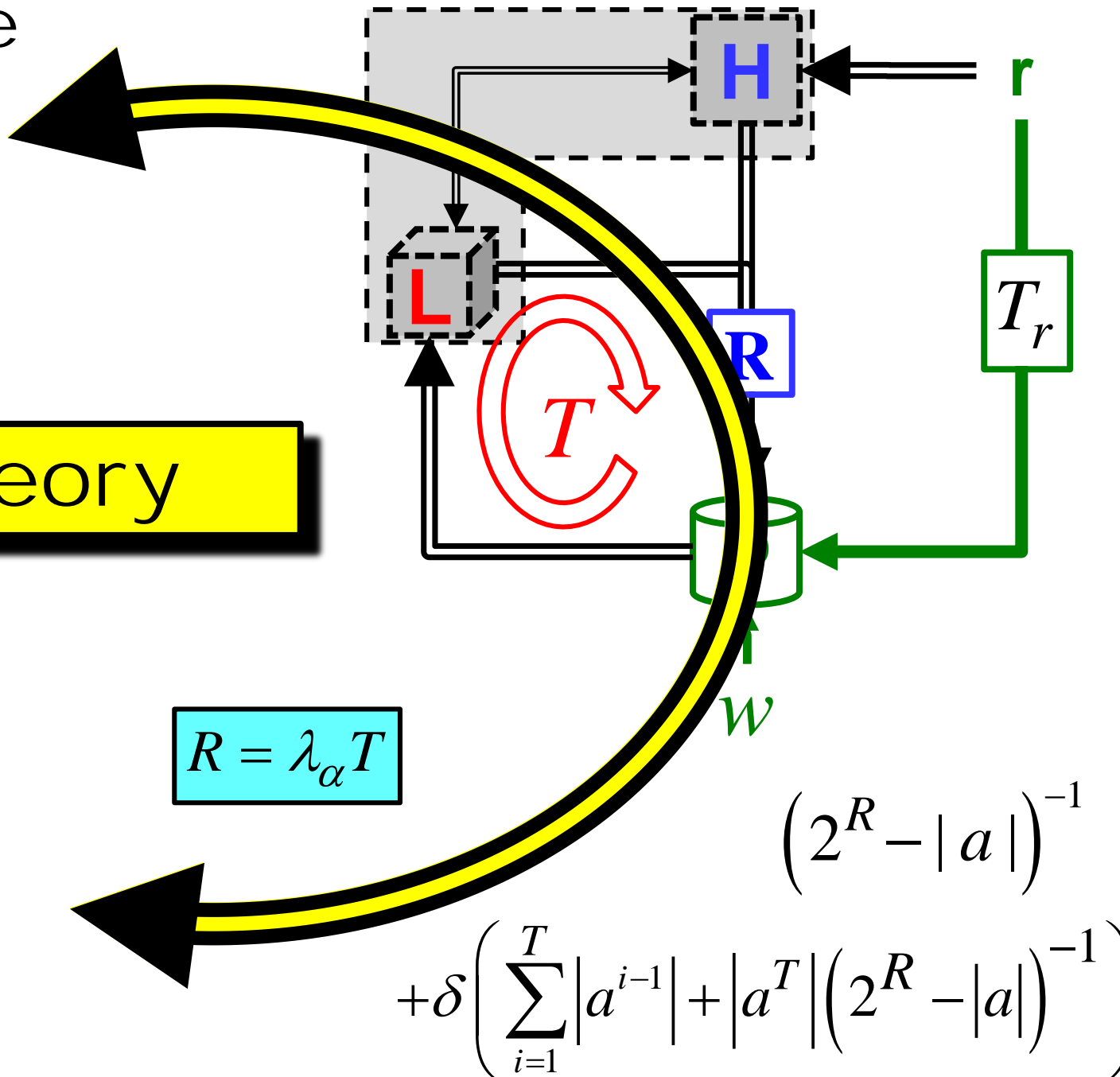
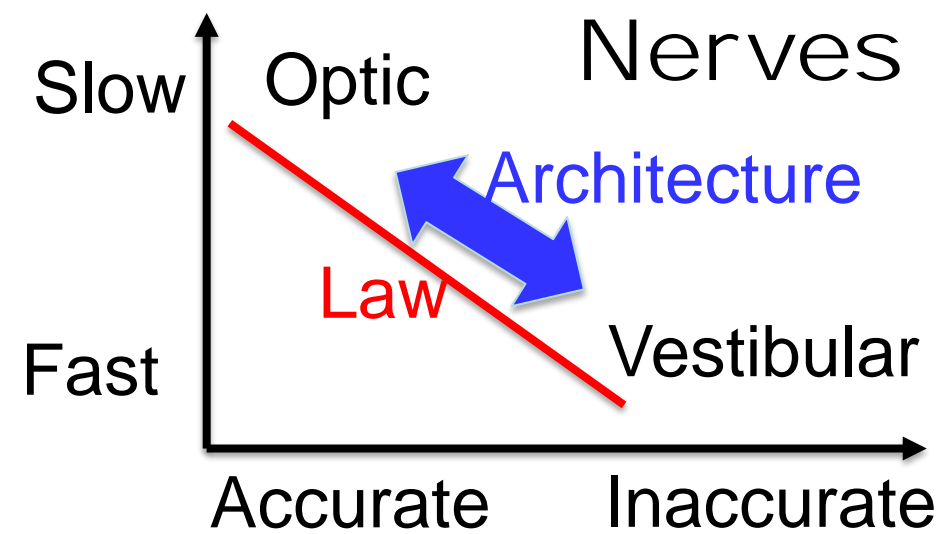
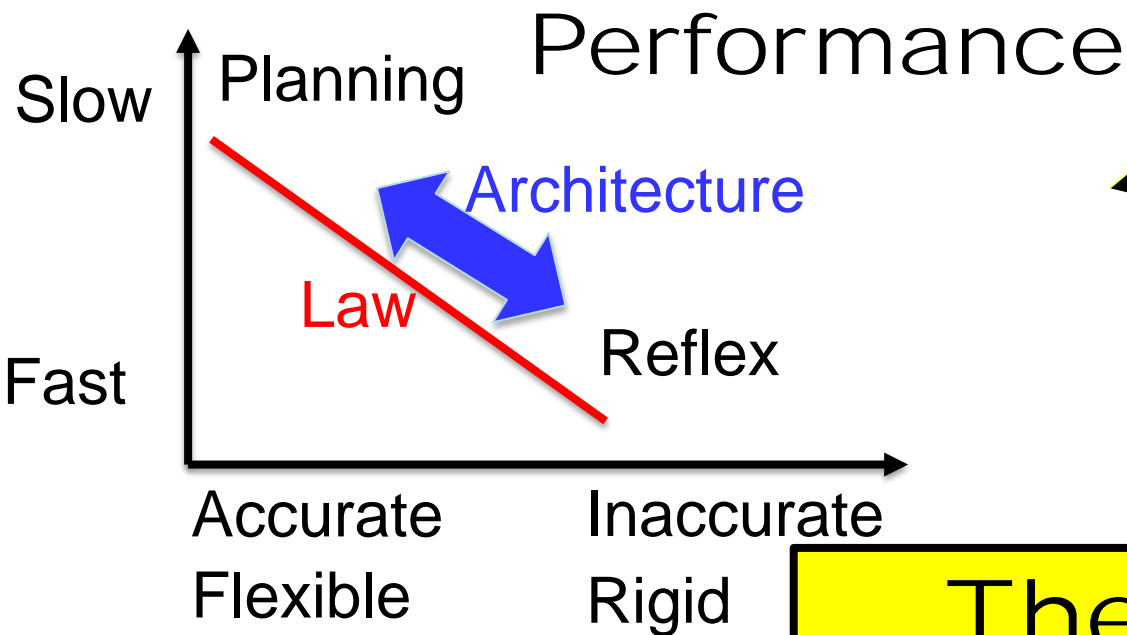
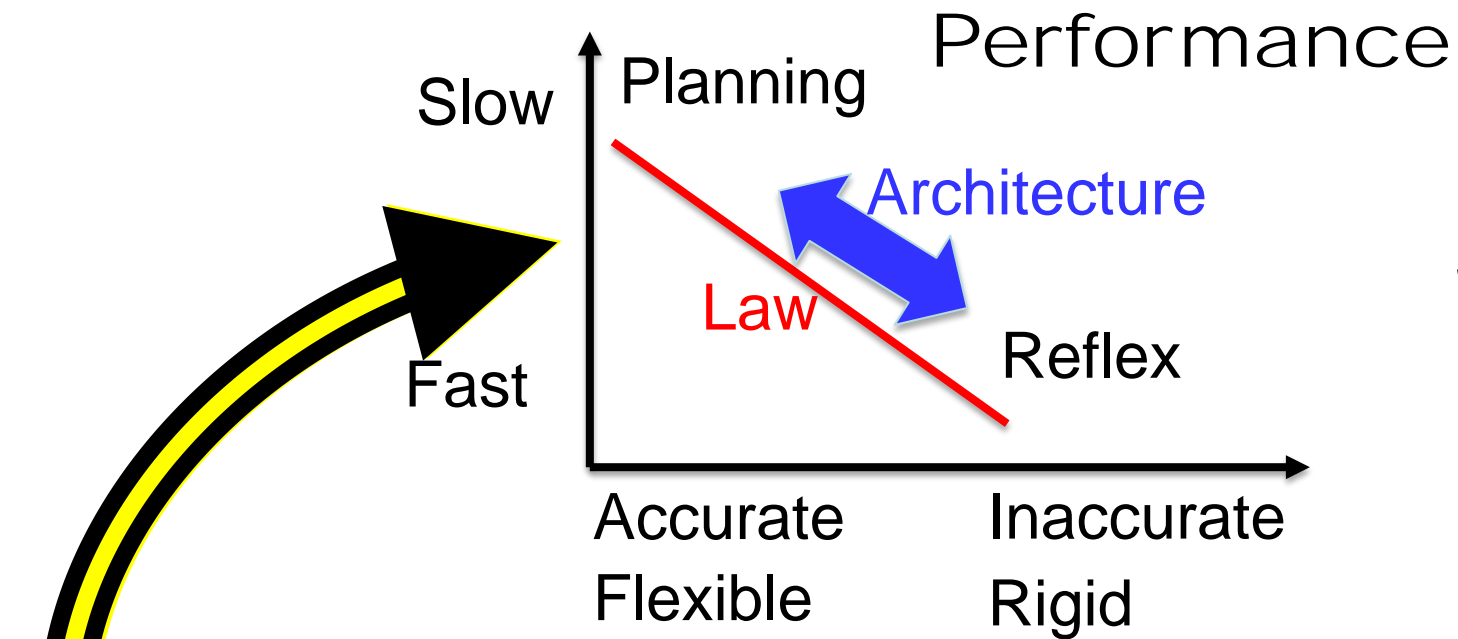


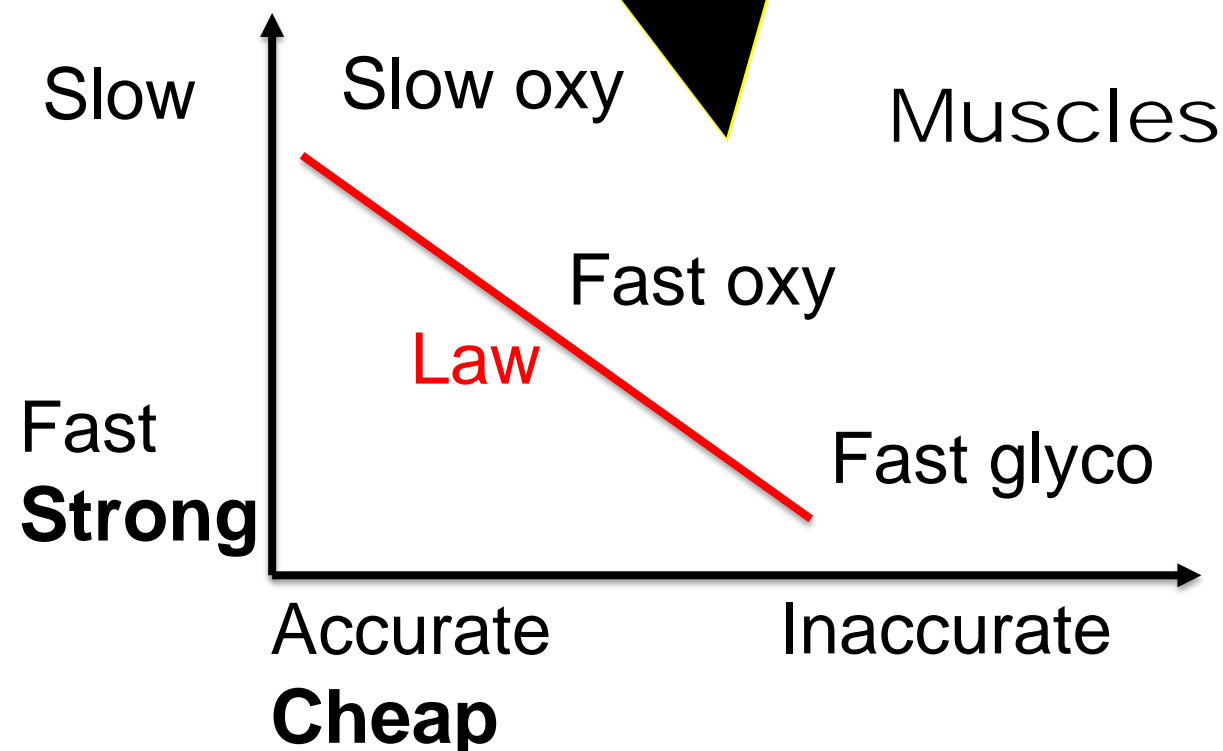
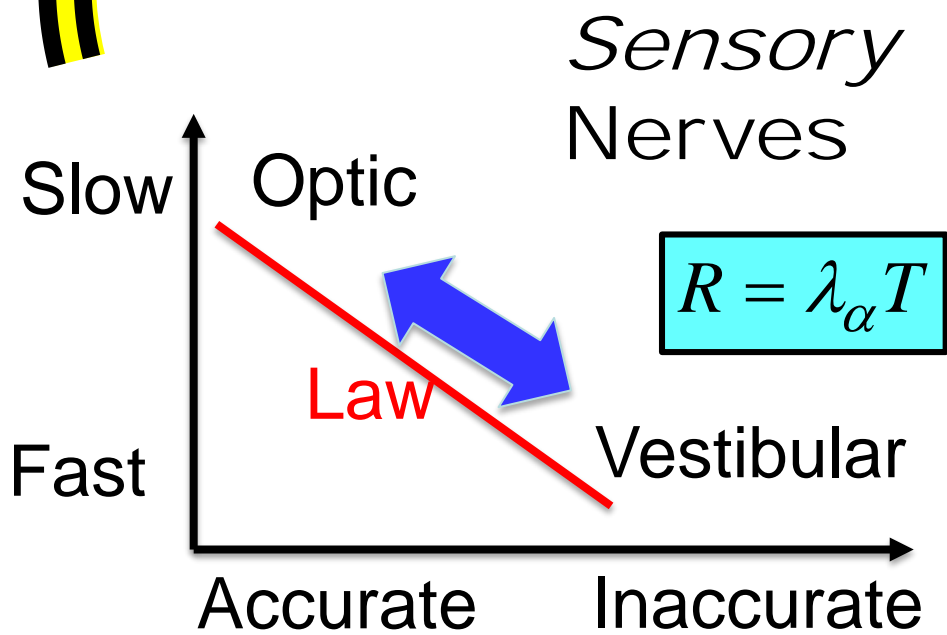
Figure 20.14. Diagram illustrating the relationship between performance, physiology, and theory in a biological system.





$$+ \delta \left(\sum_{i=1}^T |a^{i-1}| + |a^T| \left(2^R - |a| \right)^{-1} \right)$$

$$\left(2^R - |a| \right)^{-1}$$



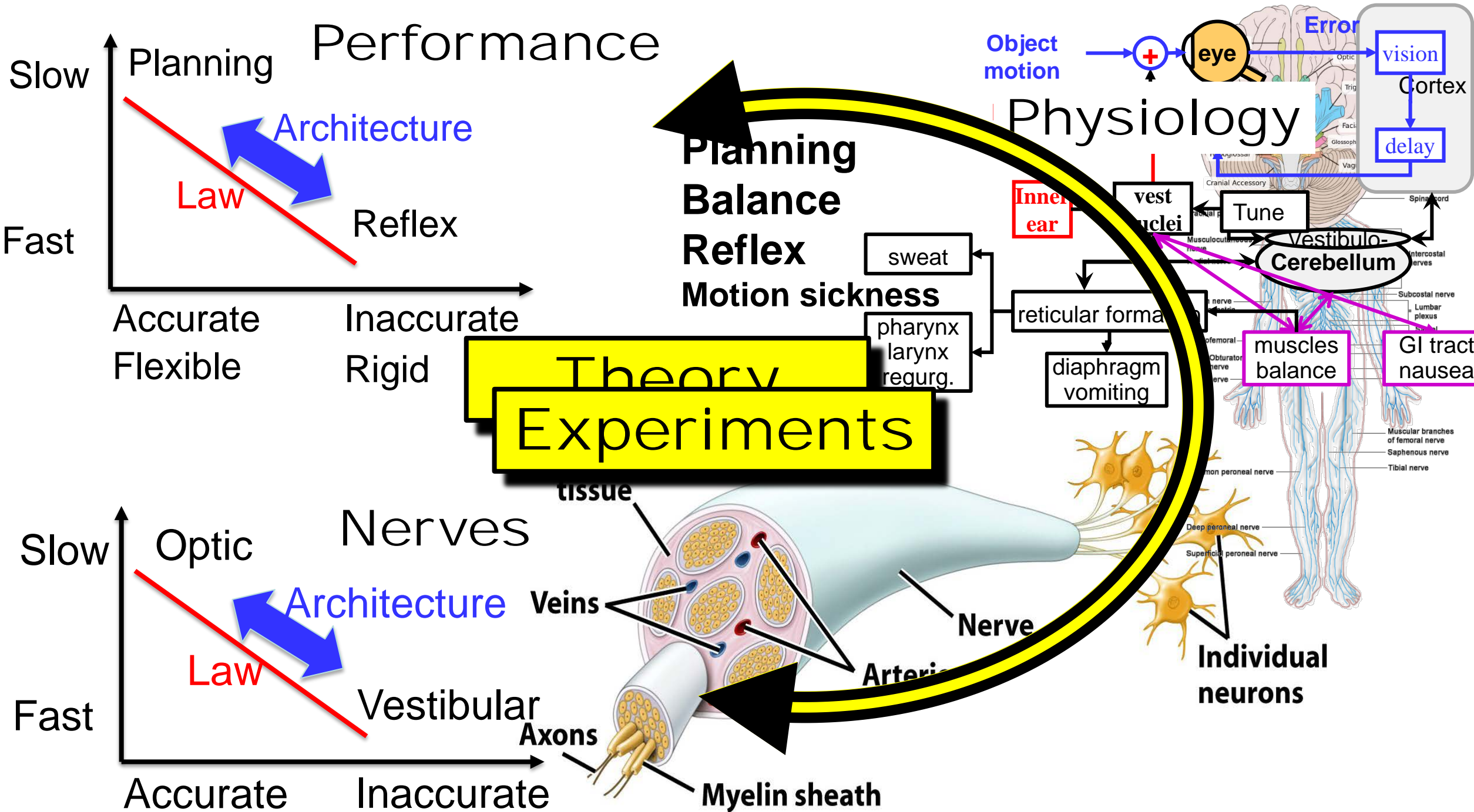
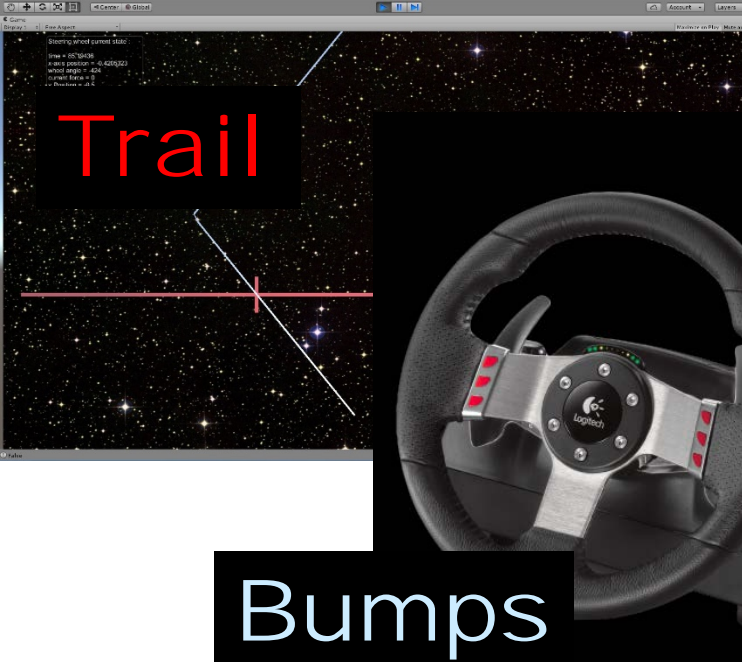
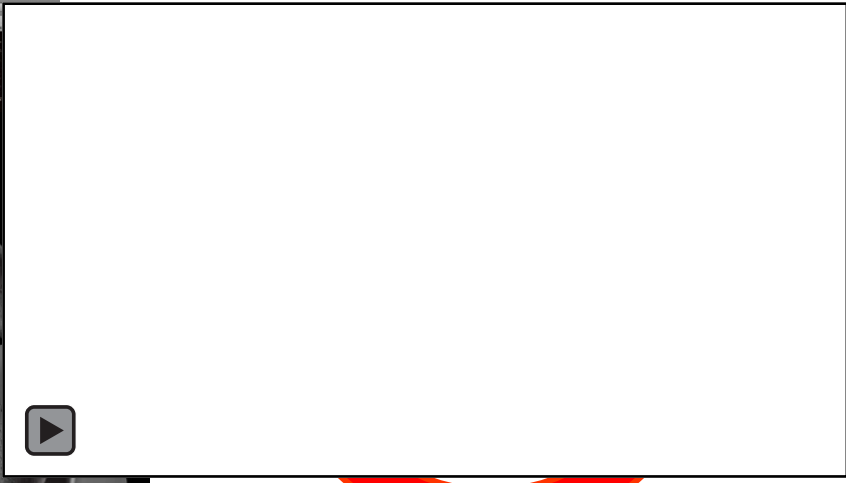


Figure 25-1b Discover Biology 3/e



Trail

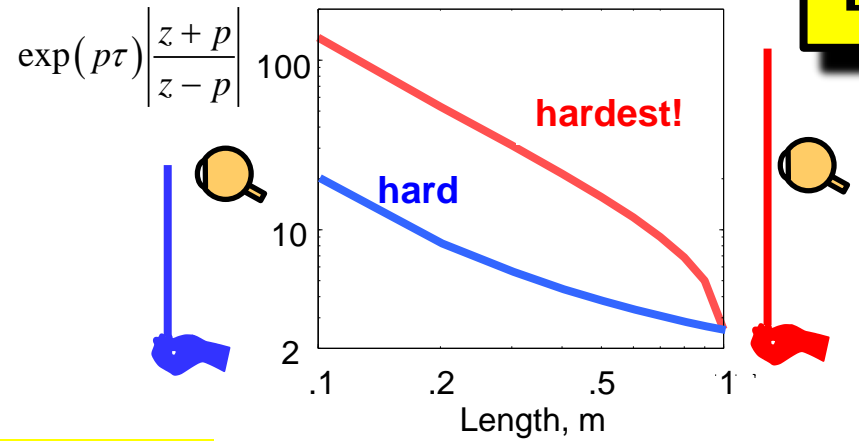
Bumps



Experiments

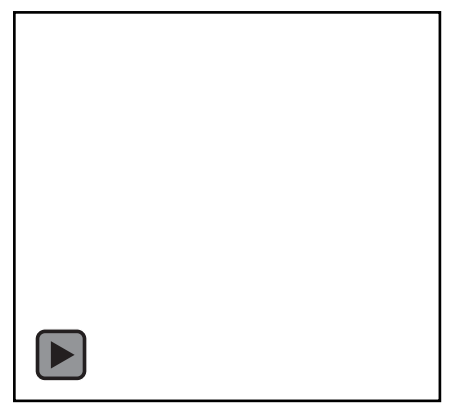
Object motion

Slow



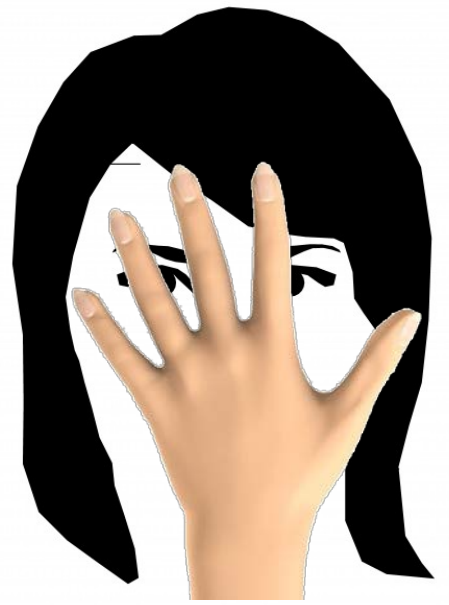
Waterbed

$$\left. \exp\left(\int \ln |T|\right) \right\|T\|_{\infty} \geq \exp(p\tau) \frac{z+p}{z-p}$$



Head motion

Fast



Trail

Theory

Experiments

Object motion

Slow



- Video biking game with trails and bumps
- **Balancing stick (inverted pendulum)**
- Vision and VOR with object and head motion
- Balancing body with vision, vestibular, and proprioception

$\exp(p\tau)$

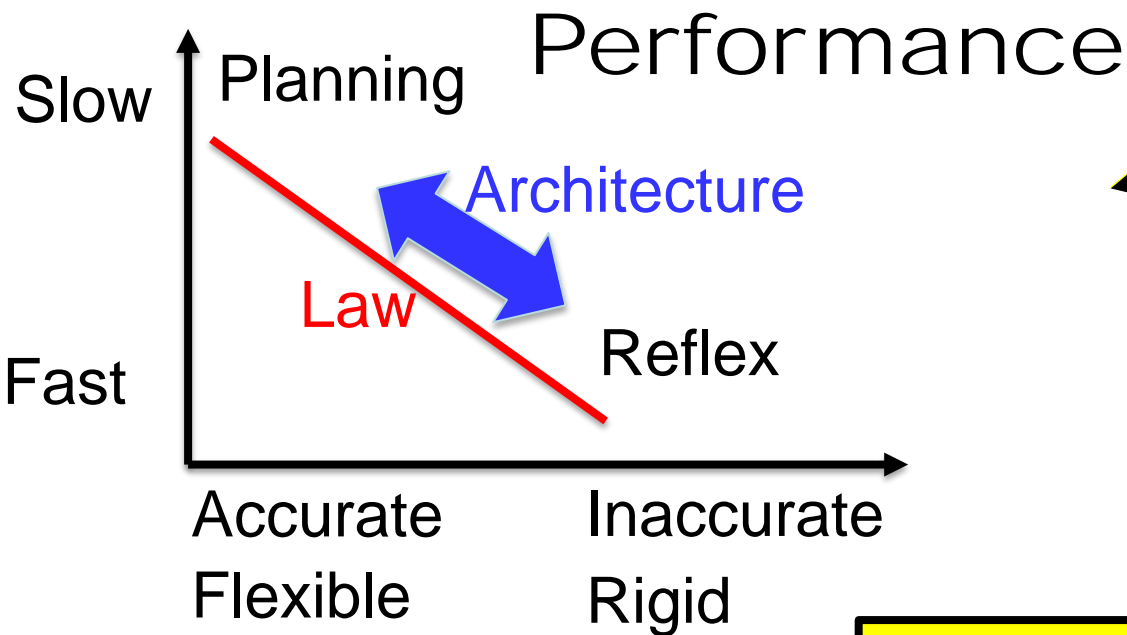
2
.1

- Quantitative match with theory (but equipment)
- Qualitative (but easy to do live demos)
- **Both**

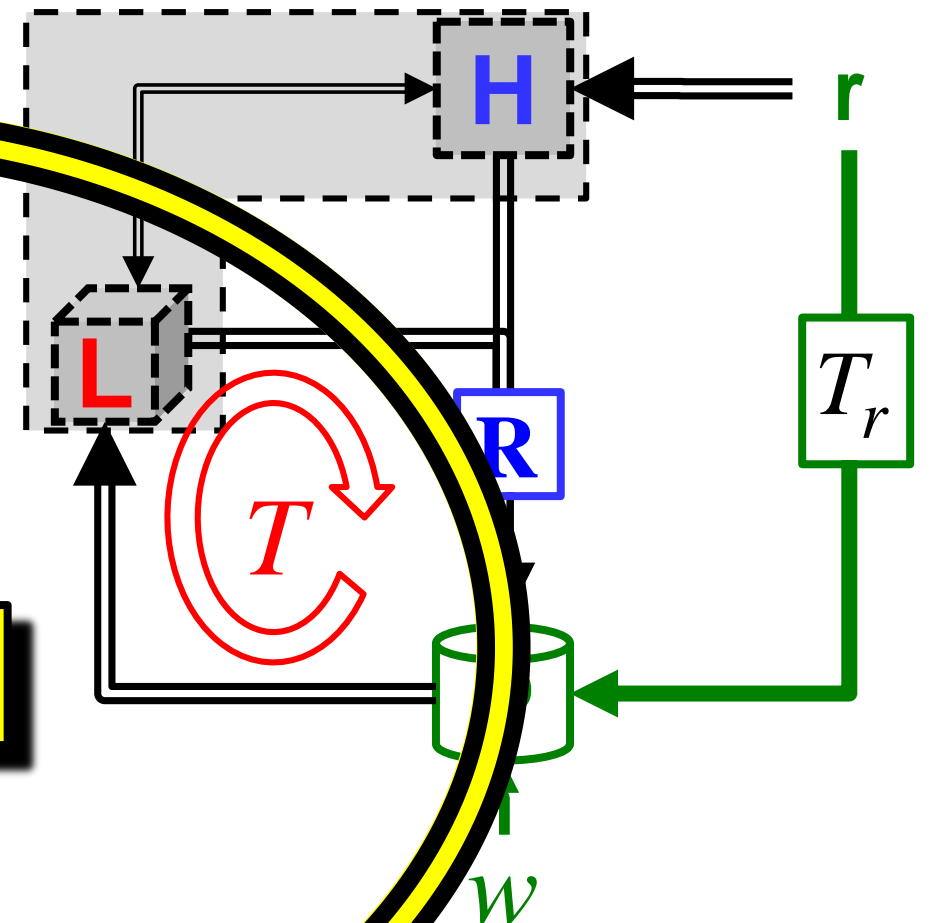
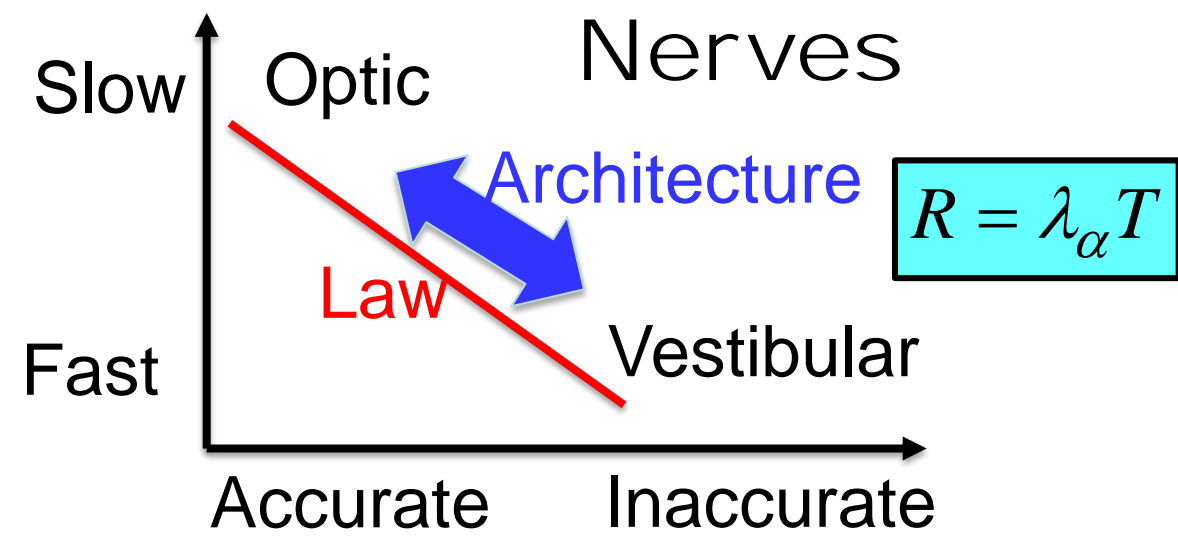
$\exp(\int$

$\|T\|_\infty$

Waterbed



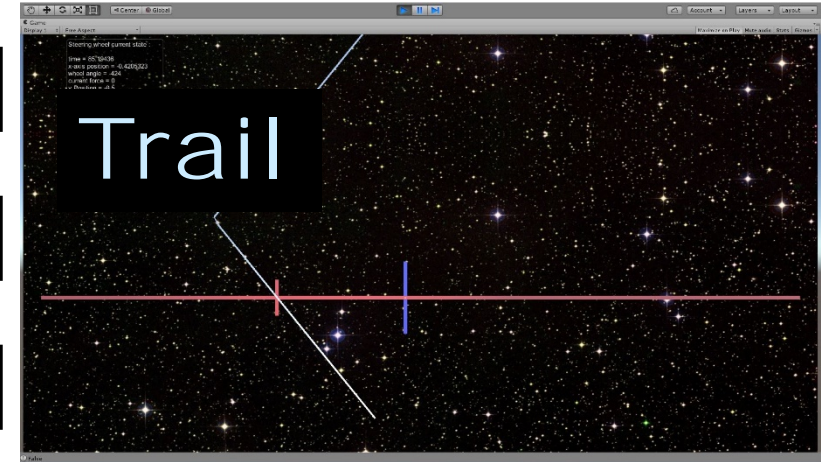
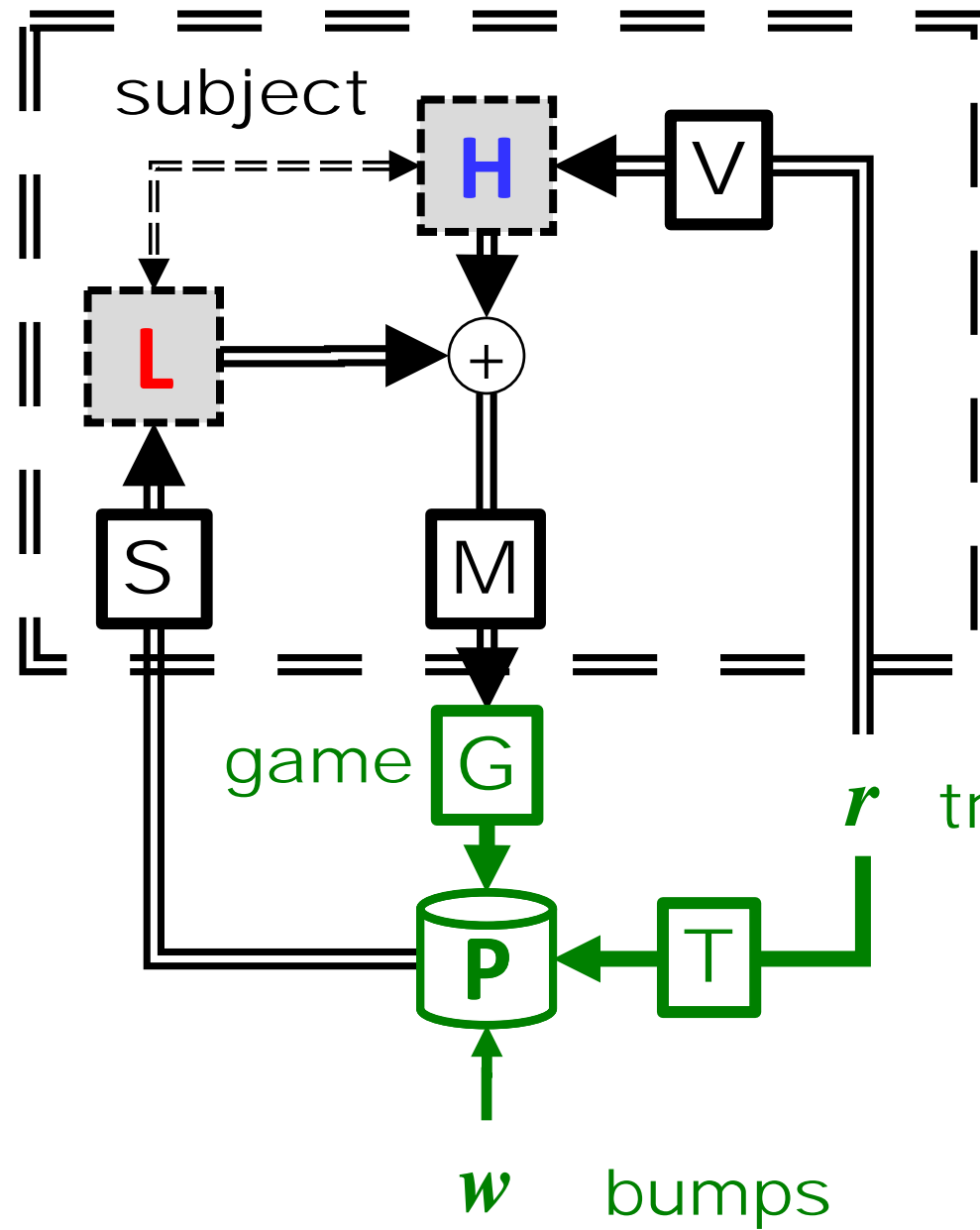
Examples



$$\left(2^R - |a|\right)^{-1} + \delta \left(\sum_{i=1}^T |a^{i-1}| + |a^T| \left(2^R - |a|\right)^{-1} \right)$$

In subject
 V=Vision
 S=Spindle
 M=Muscle
 H=High layer
 L=Low layer

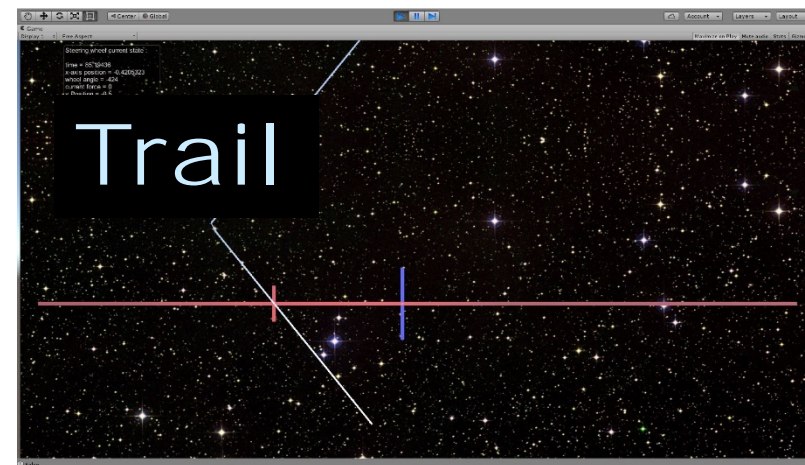
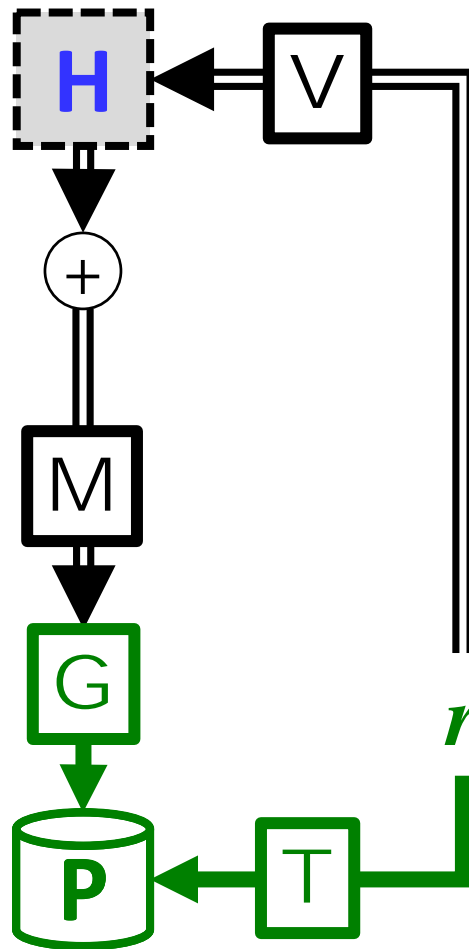
In game:
 G=Game motor
 T=Advance



In subject
V=Vision

M=Muscle
H=High layer

In game:
G=Game motor
T=Advance



r trail

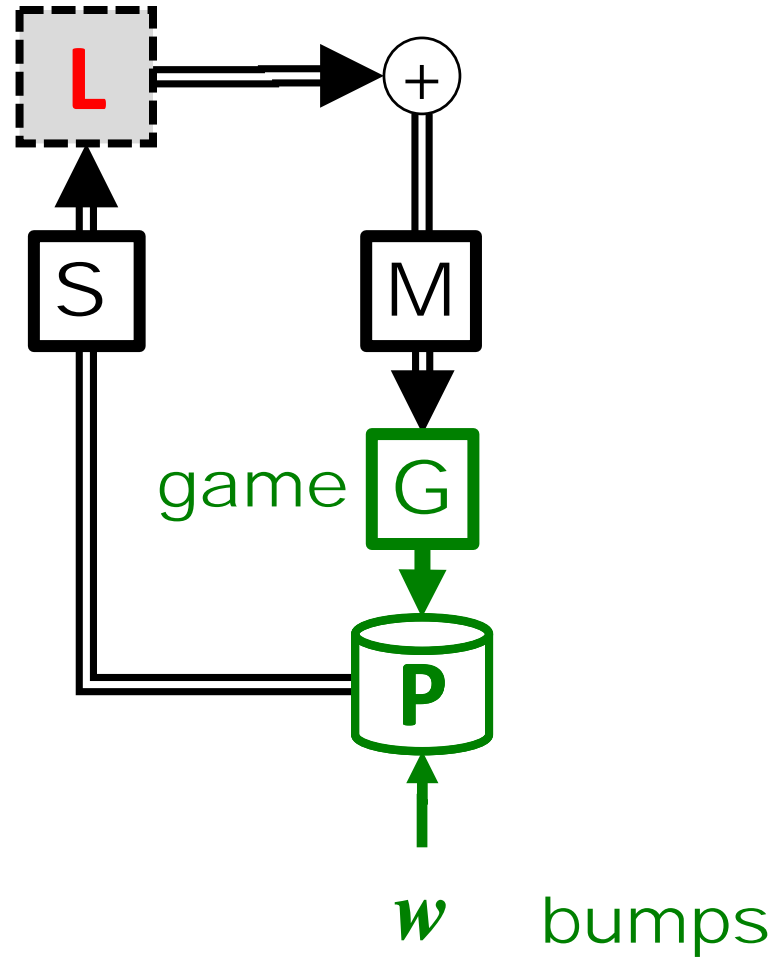


In subject

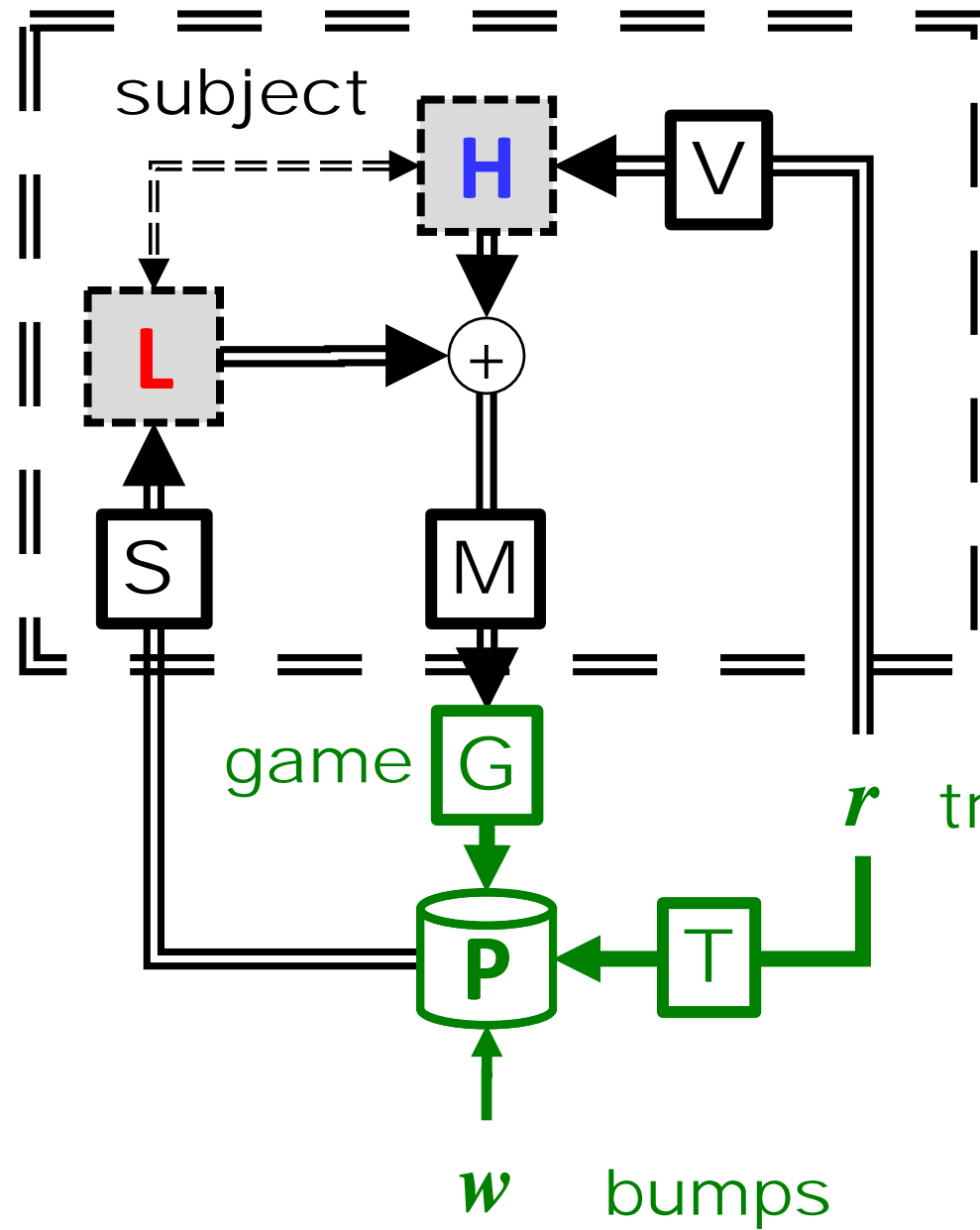
S=Spindle
M=Muscle

L=Low layer

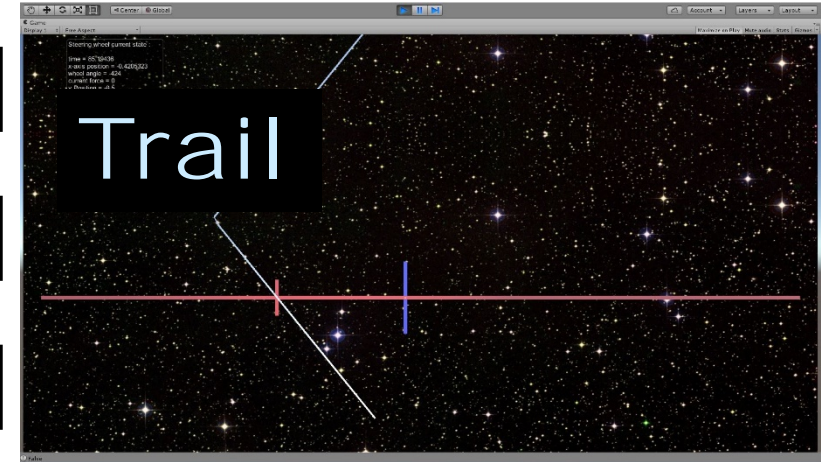
In game:
G=Game motor



In subject
 V=Vision
 S=Spindle
 M=Muscle
 H=High layer
 L=Low layer

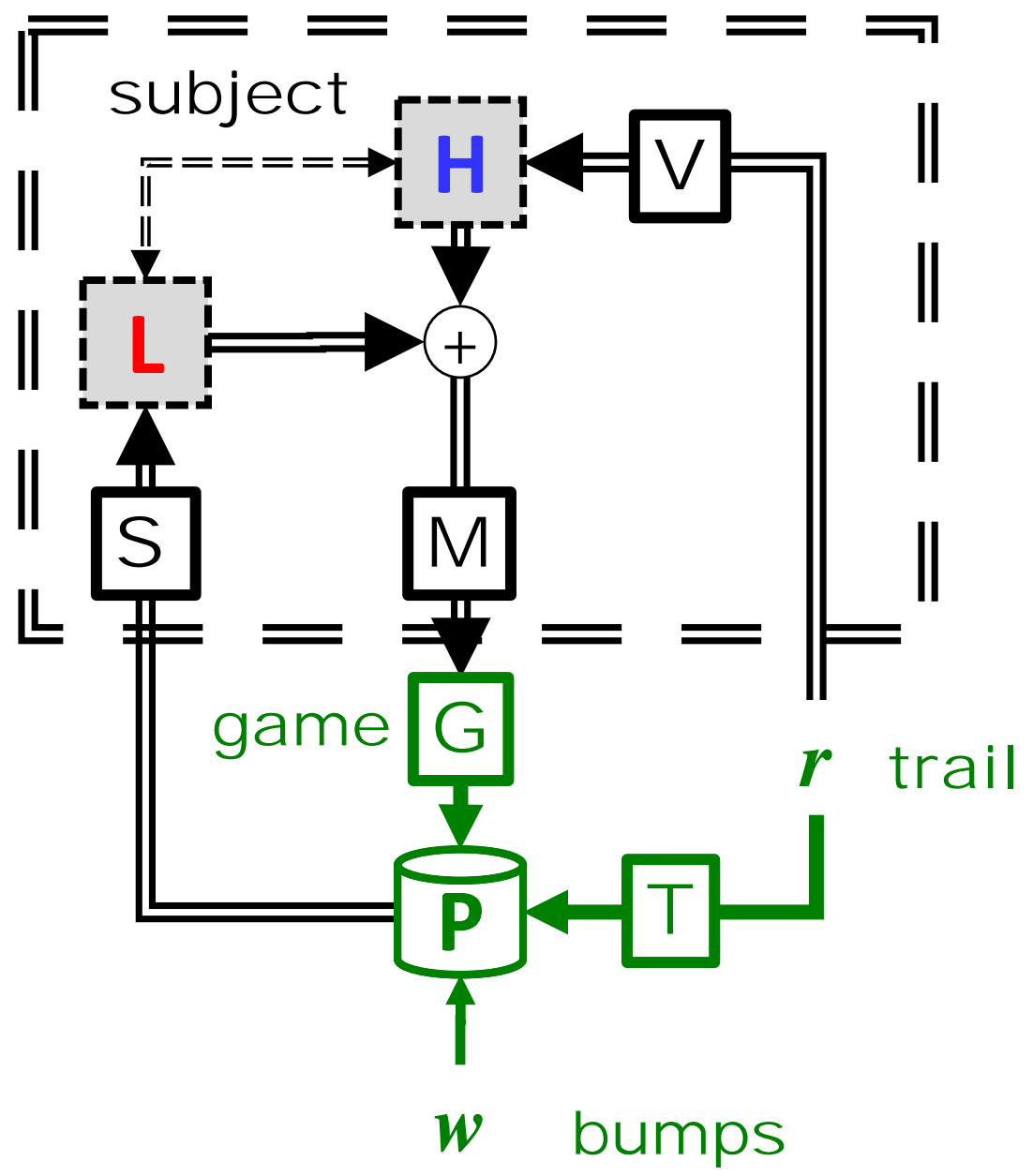


In game:
 G=Game motor
 T=Advance



In subject
V=Vision
S=Spindle
M=Muscle
H=High layer
L=Low layer

In game:
G=Game motor
T=Advance



Quantization
and delay
everywhere

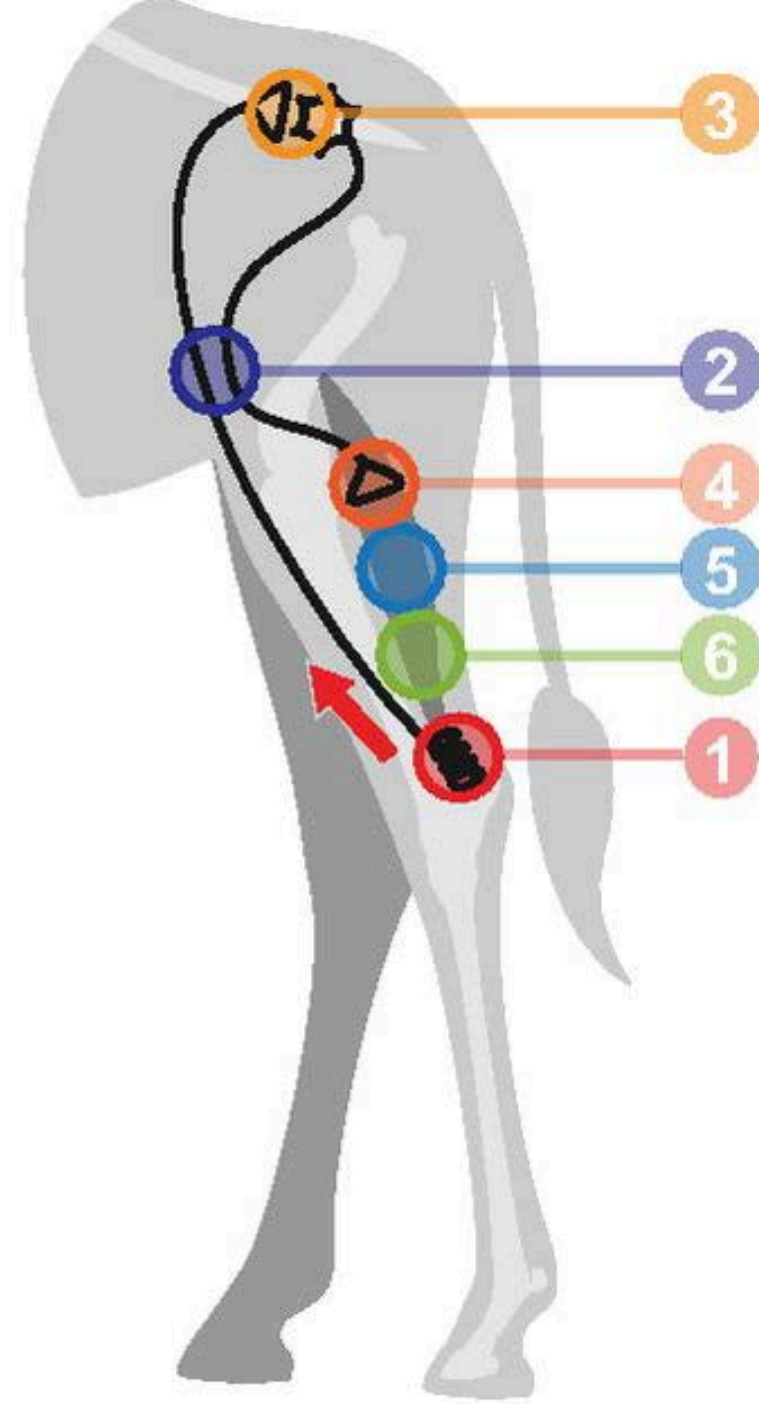
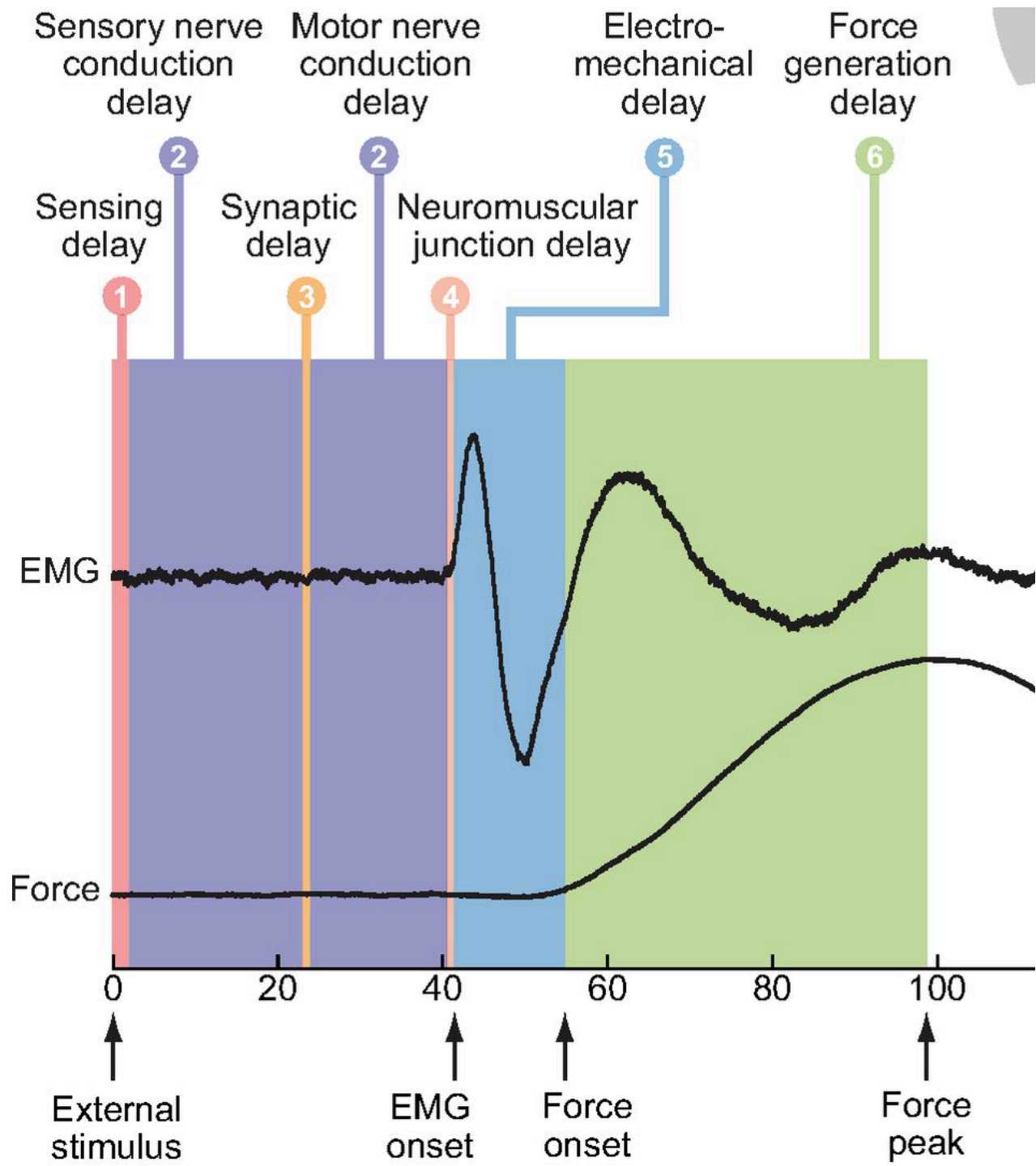
RESEARCH ARTICLE

Sensorimotor responsiveness and resolution in the giraffe

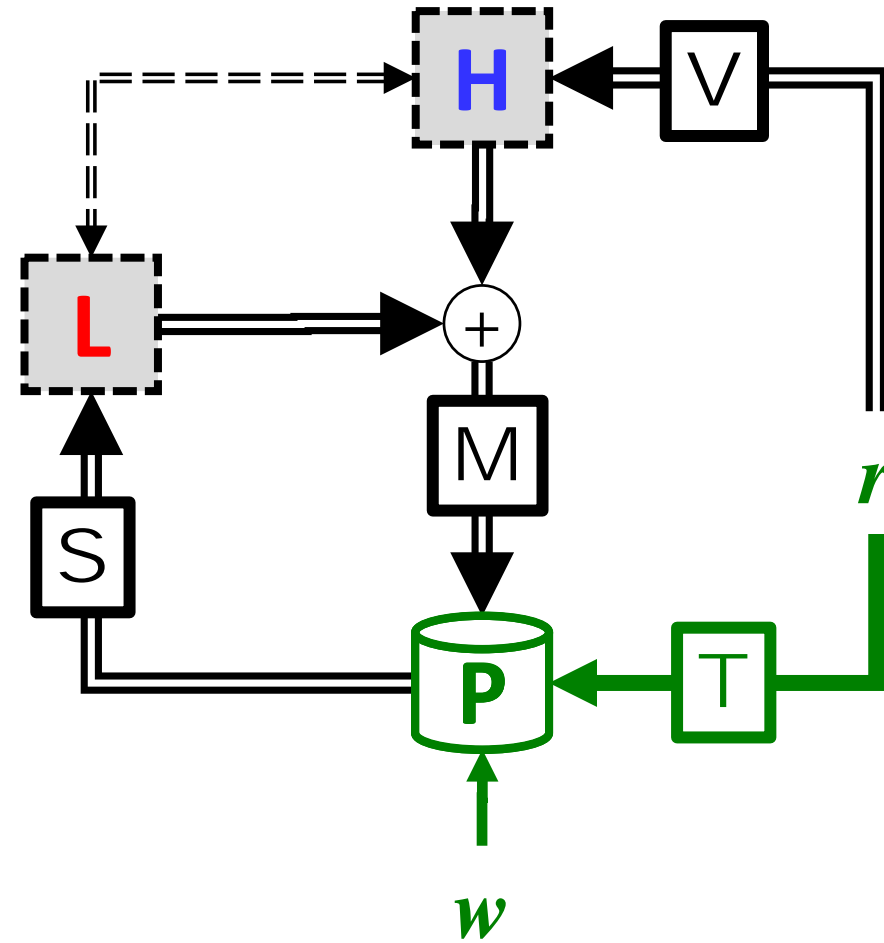
Heather L. More^{1,*†}, Shawn M. O'Connor^{1,*}, Emil Brøndum², Tobias Wang³, Mads F. Bertelsen⁴,
Carsten Grøndahl⁴, Karin Kastberg⁵, Arne Hørlyck⁵, Jonas Funder⁶ and J. Maxwell Donelan¹

¹Department of Biomedical Physiology and Kinesiology, Simon Fraser University, Canada, ²Department of Biomedicine, Aarhus University, Denmark, ³Zoophysiology, Department of Biosciences, Aarhus University, Denmark, ⁴Center for Zoo and Wild Animal Health, Copenhagen Zoo, Frederiksberg, Denmark, ⁵Department of Diagnostic Imaging, Aarhus University Hospital, Skejby, Denmark and ⁶Department of CardioThoracic Surgery, Aarhus University Hospital, Skejby, Denmark

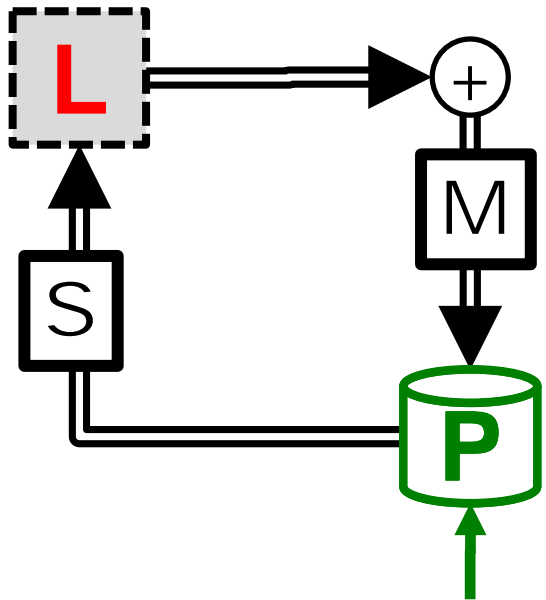
*These authors contributed equally to this work



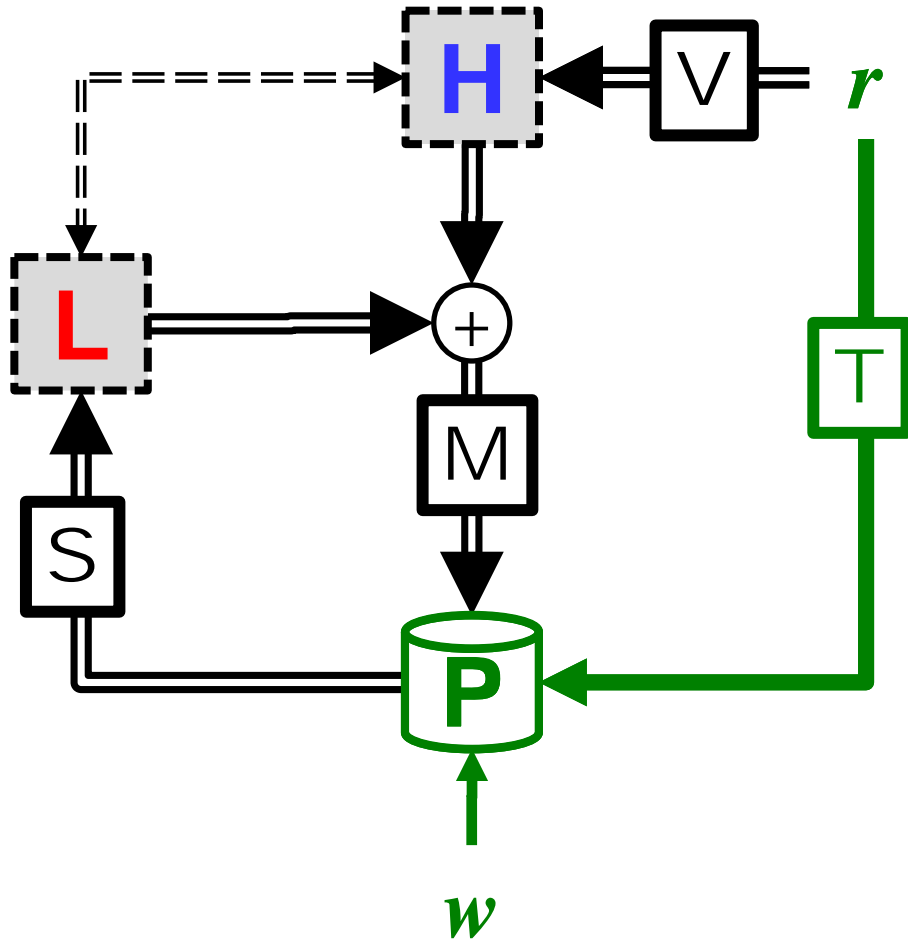
V=Vision
S=Spindle
M=Muscle
H=High layer
L=Low layer
T=Advance



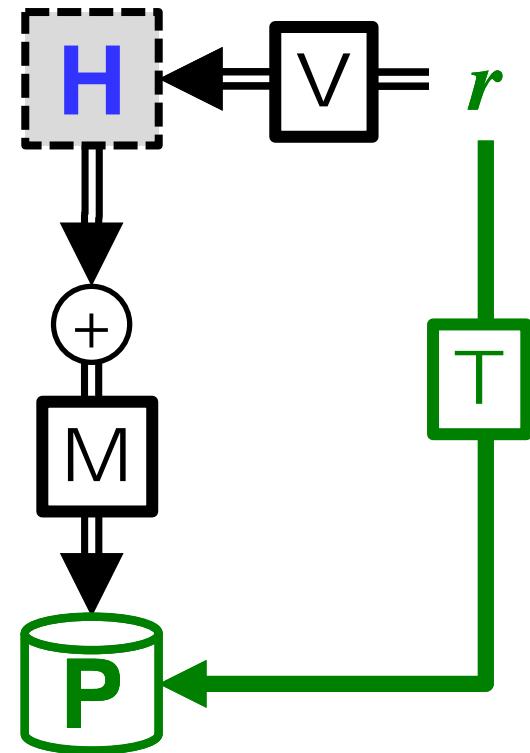
key idea



bumps



w

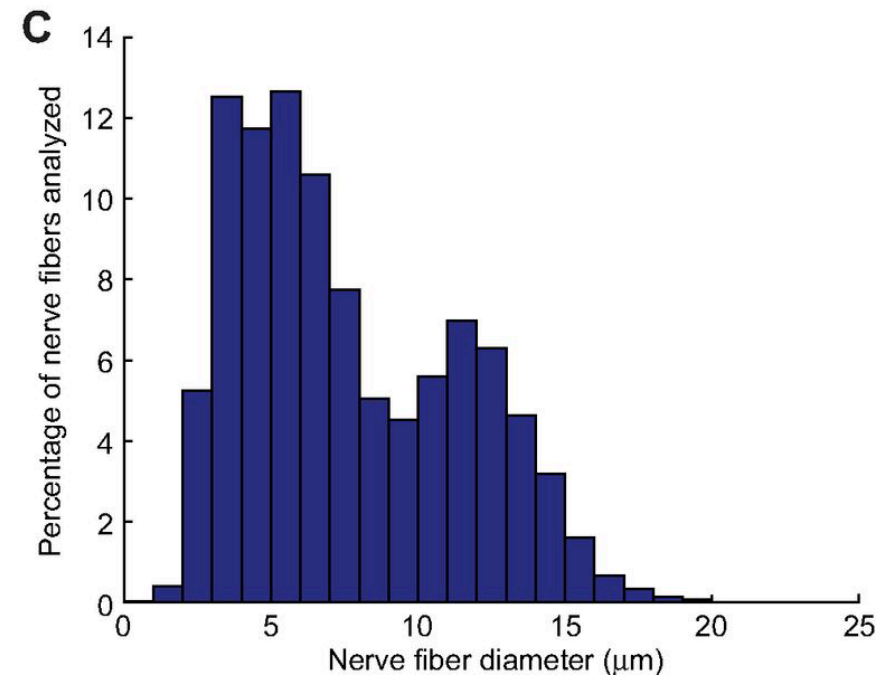
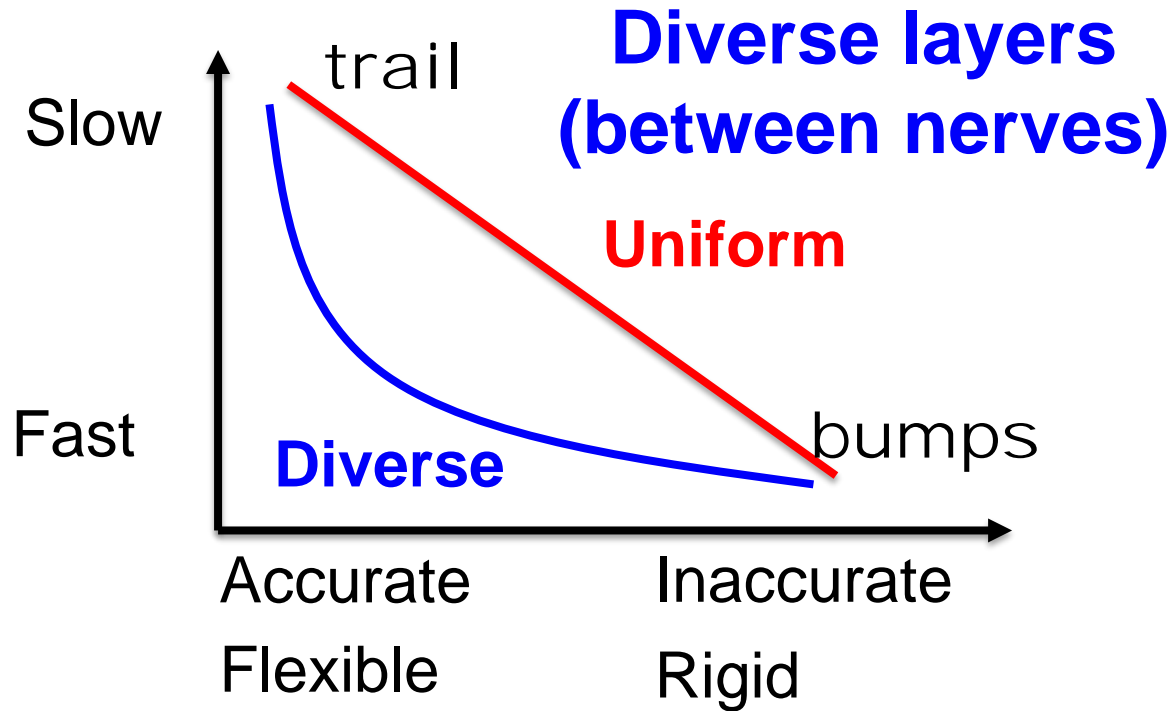


trail

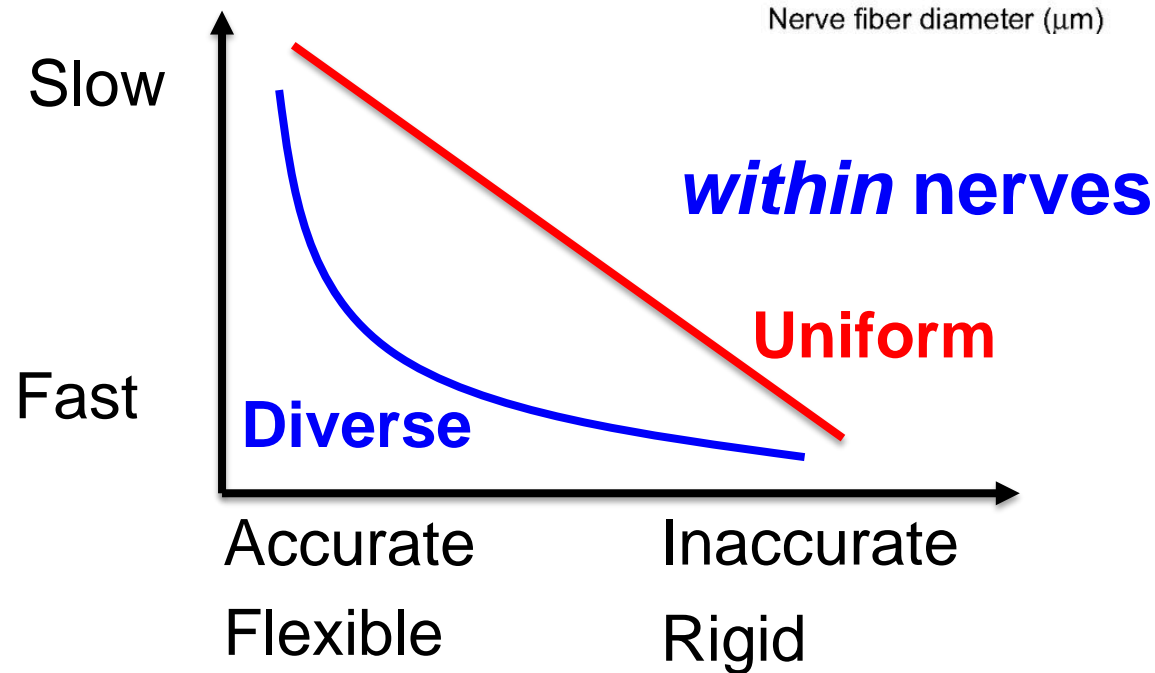
$$\delta \left(\underbrace{\sum_{i=1}^T |a^{i-1}|}_{\text{delay}} + \underbrace{|a^T| \left(2^R - |a| \right)^{-1}}_{\text{delay+quant}} \right)$$

errors add

$$+ \underbrace{\left(2^R - |a| \right)^{-1}}_{\text{quant}}$$



Diversity sweet spots

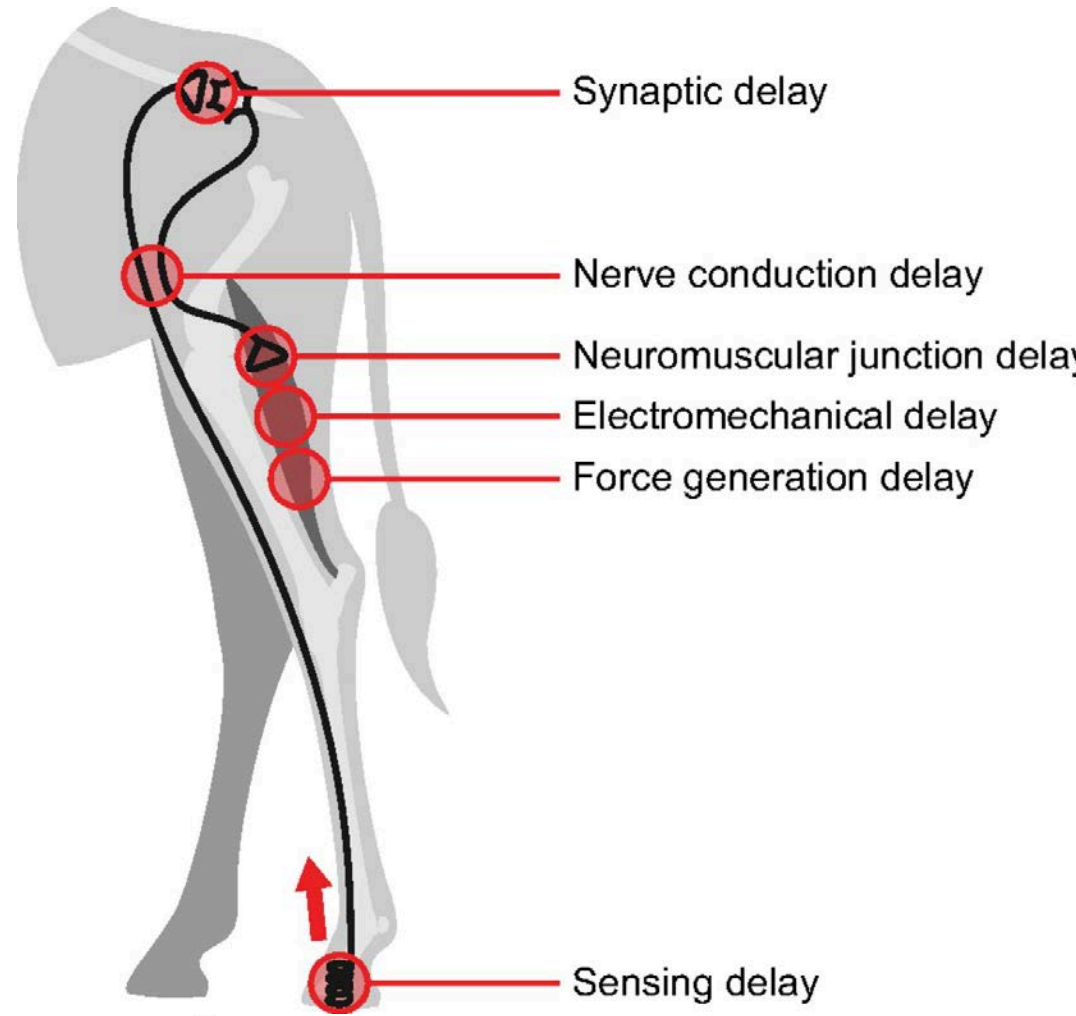
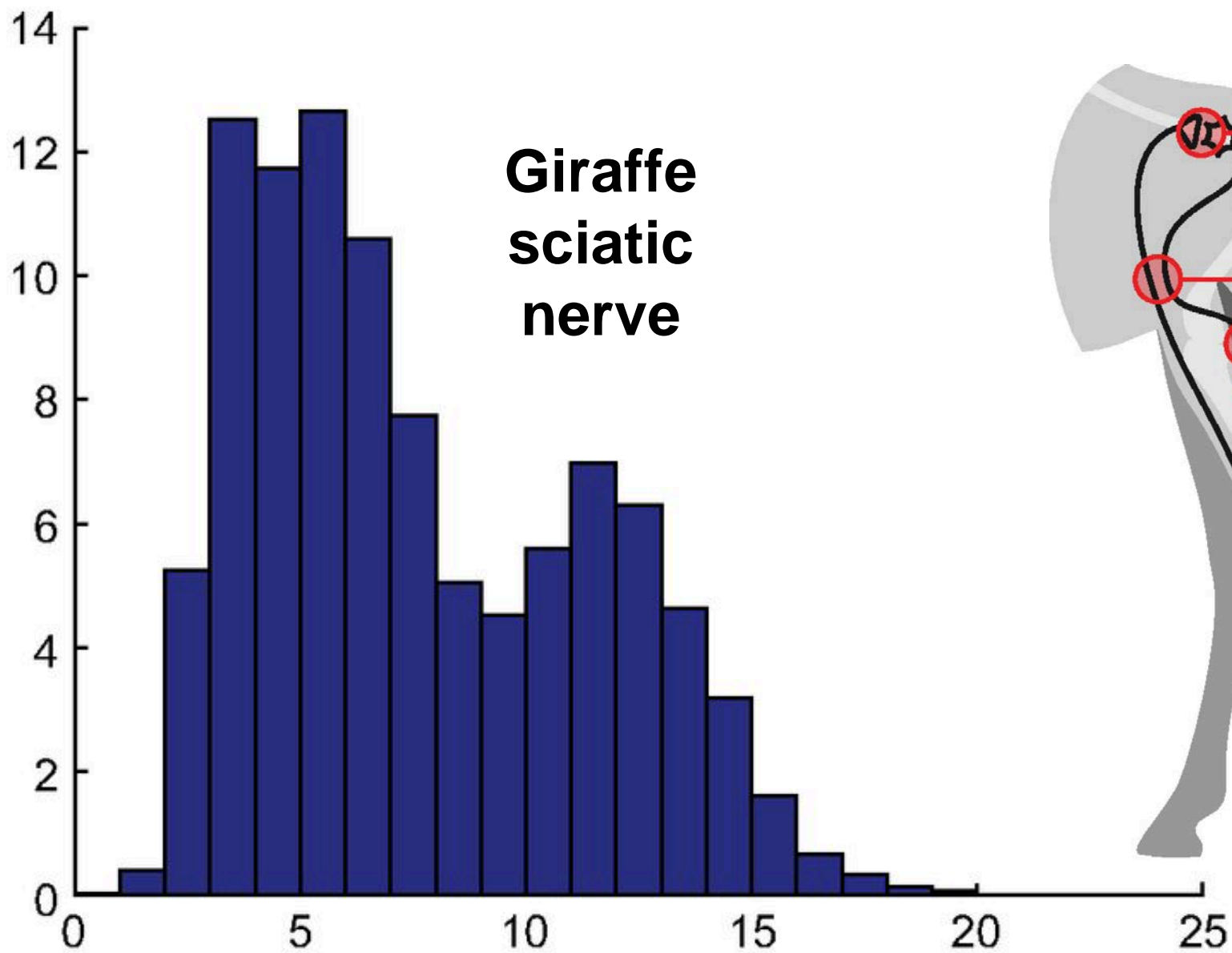


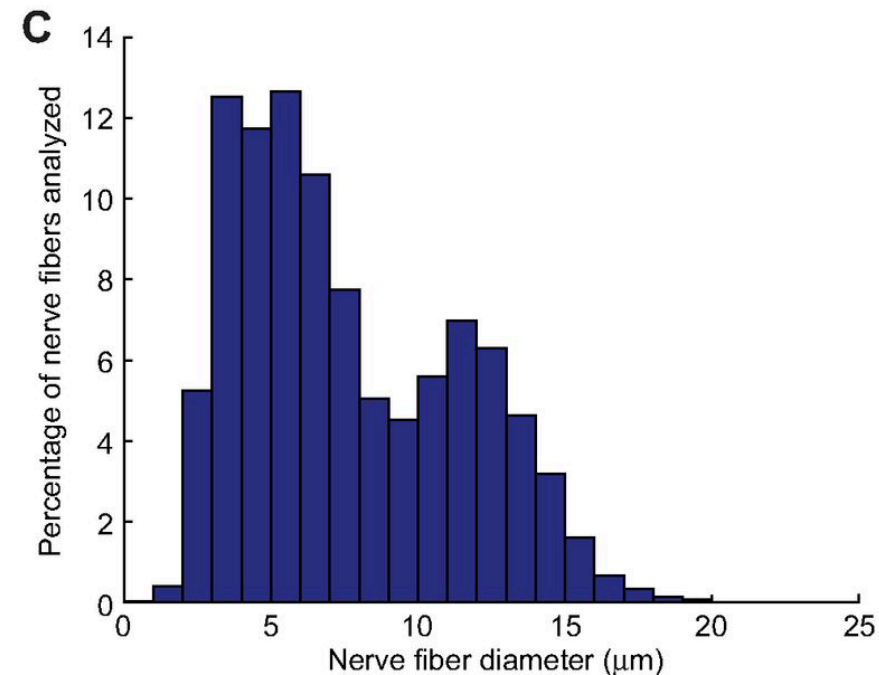
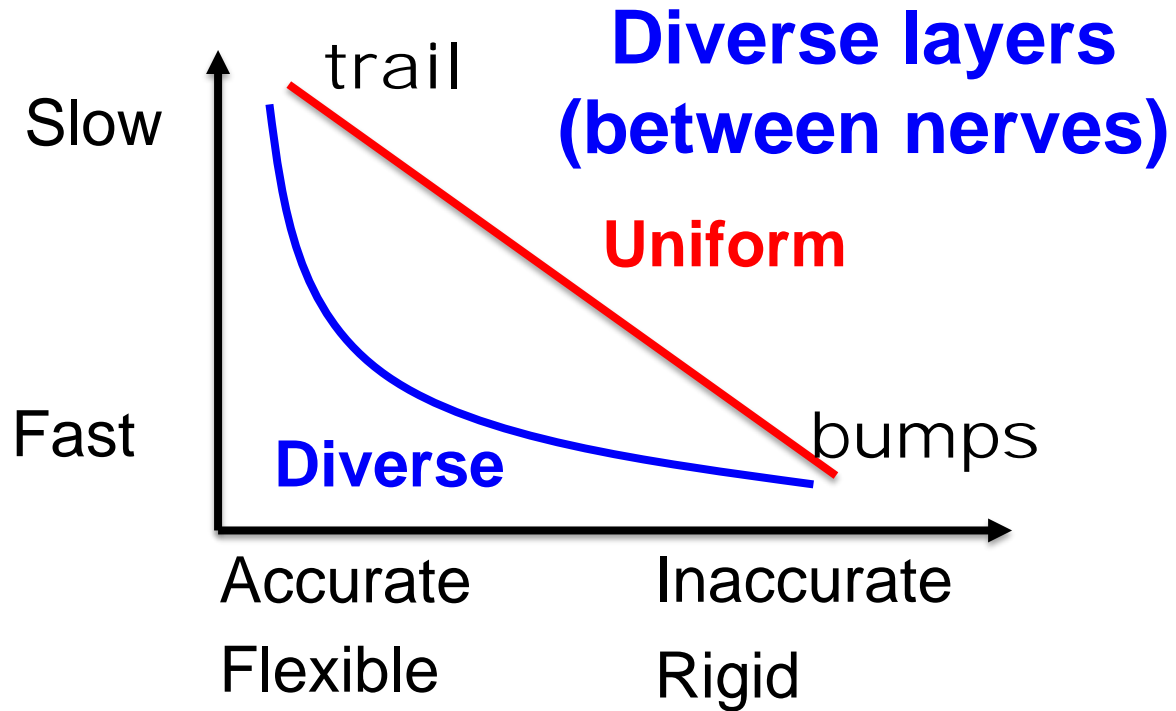
C

Percentage of nerve fibers analyzed

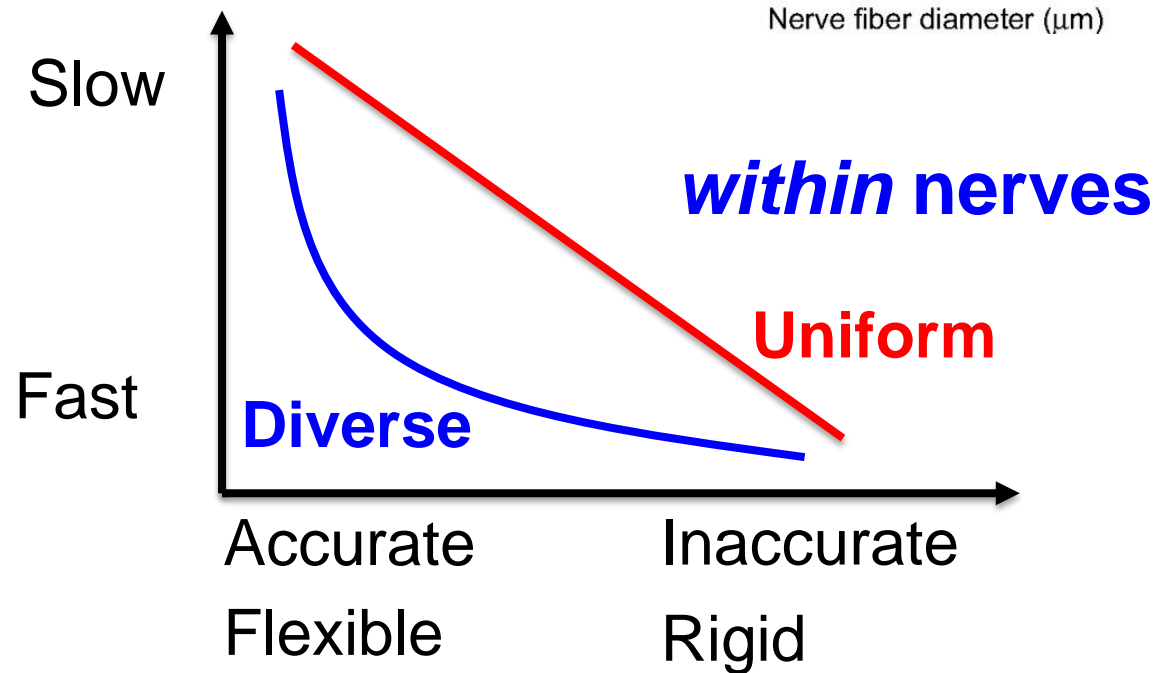
**Giraffe
sciatic
nerve**

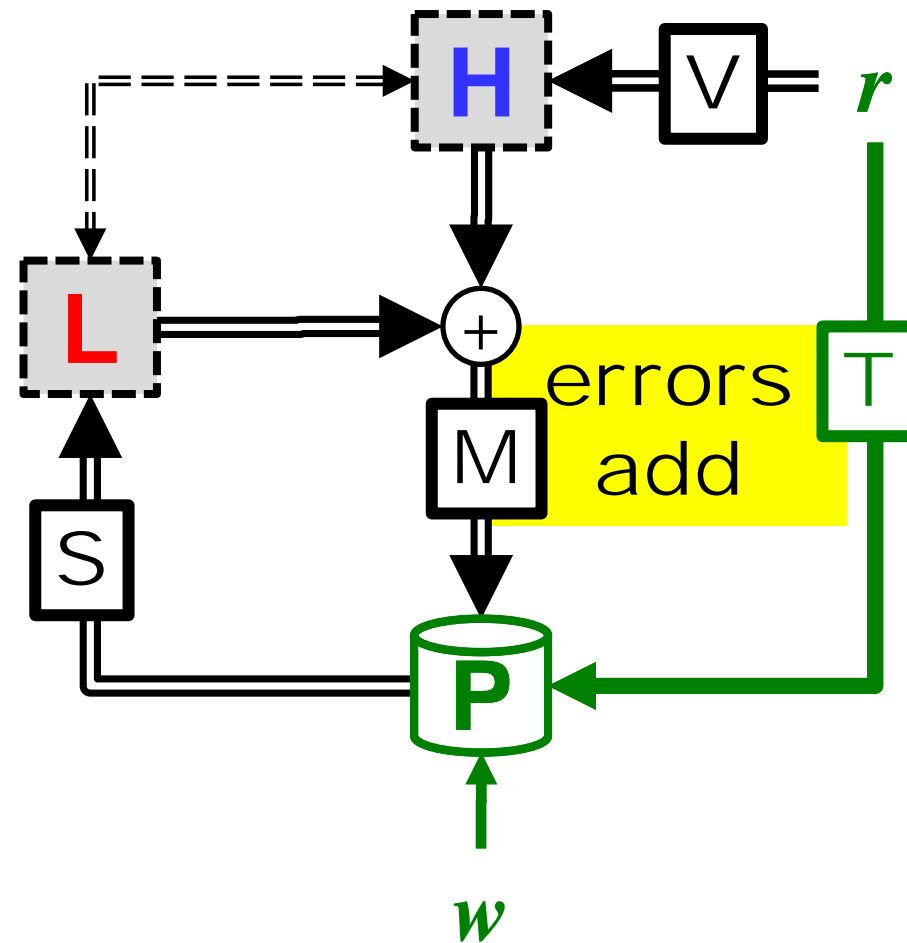
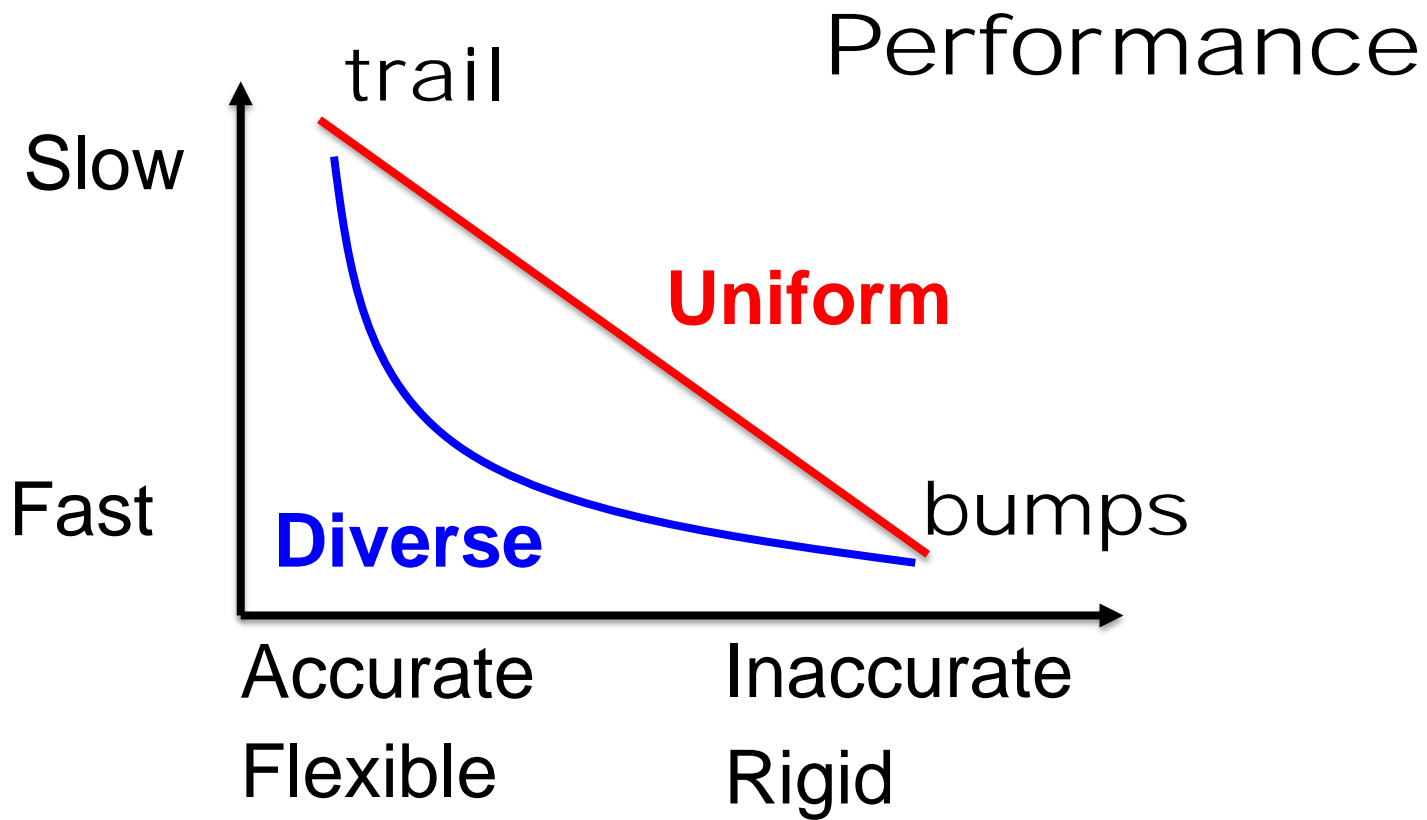
Nerve fiber diameter (μm)





Diversity sweet spots





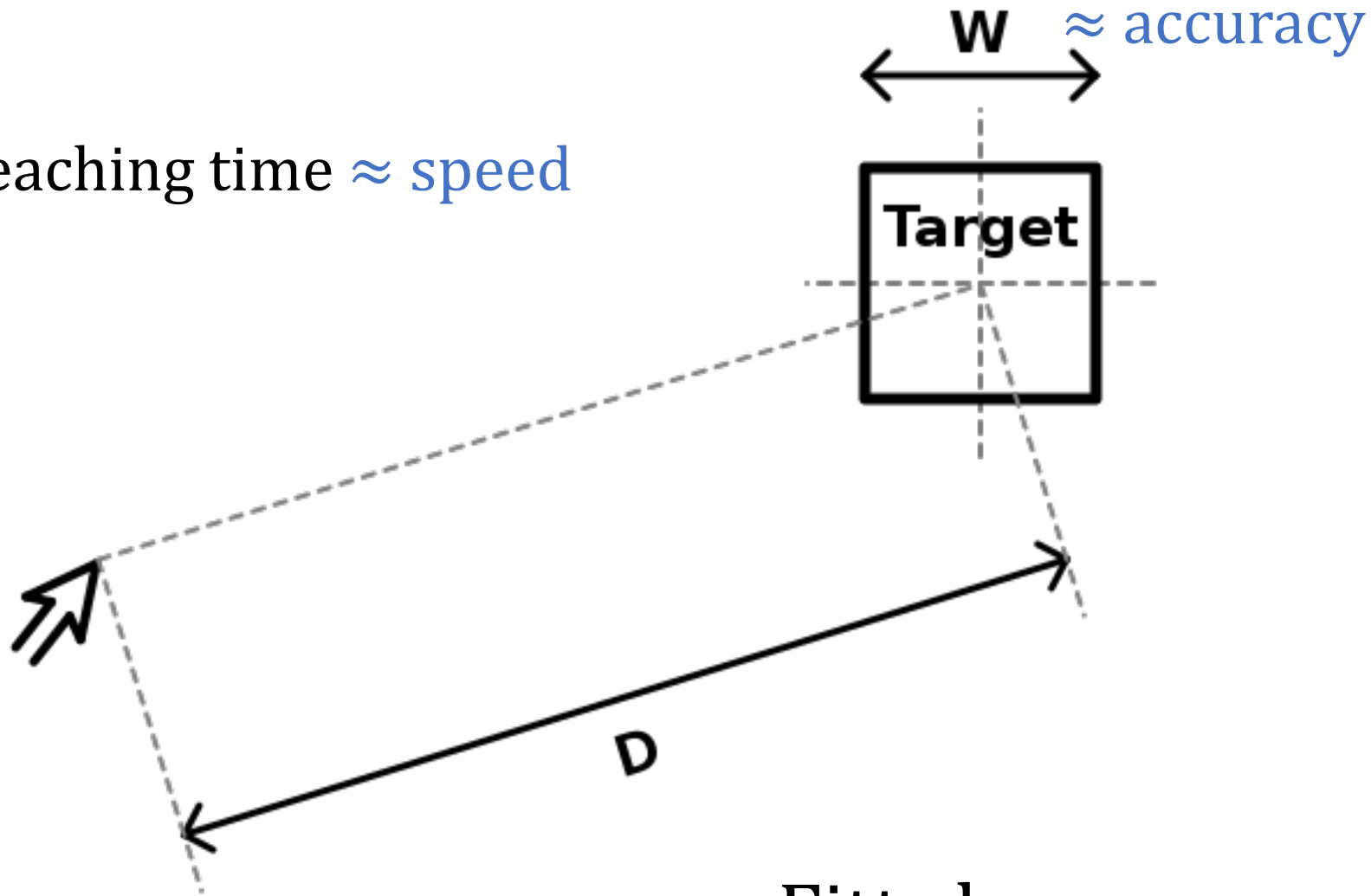
Diversity sweet spot
Diverse layers
(between nerves)

bumps

trail

$$\delta \left(\sum_{i=1}^T |a^{i-1}| + |a^T| \left(2^{\lambda T} - |a| \right)^{-1} \right) + \left(2^V - |a| \right)^{-1}$$

Reaching time \approx speed

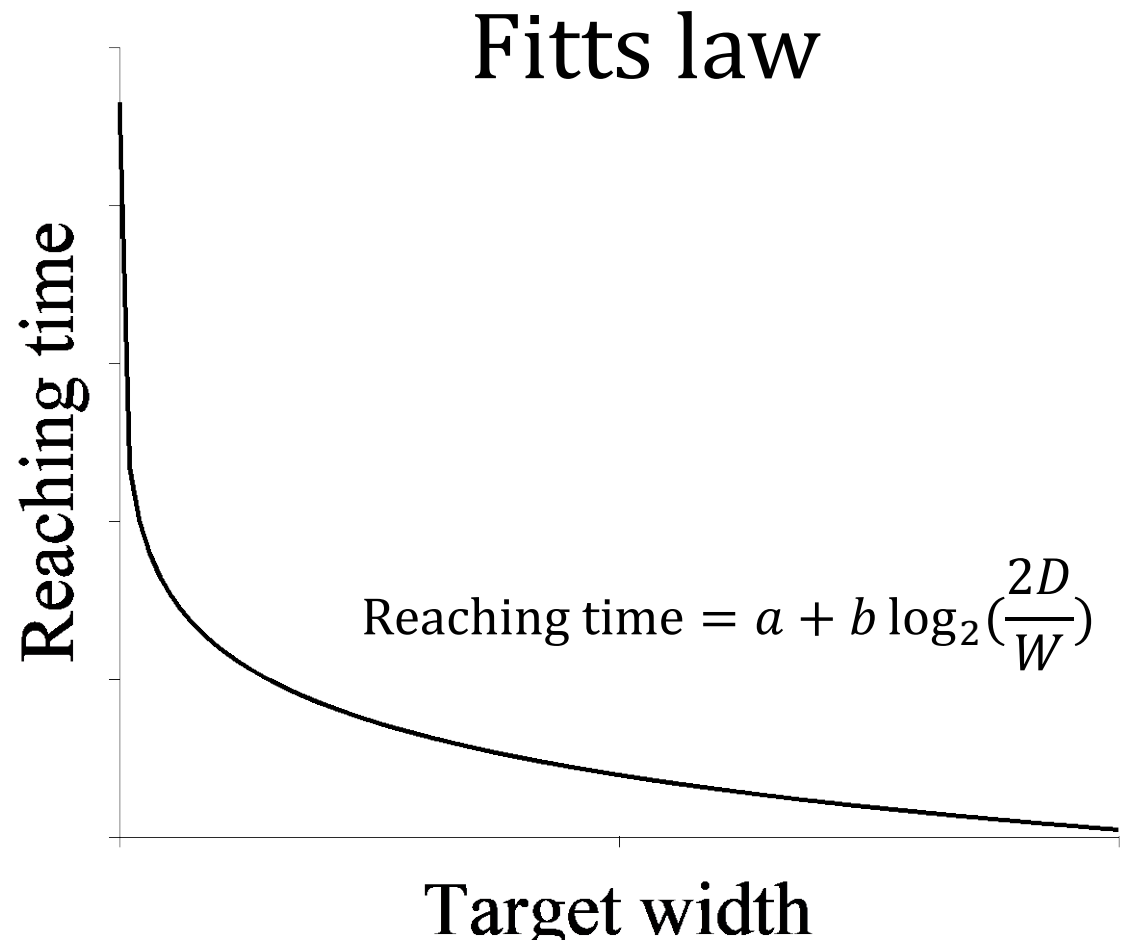
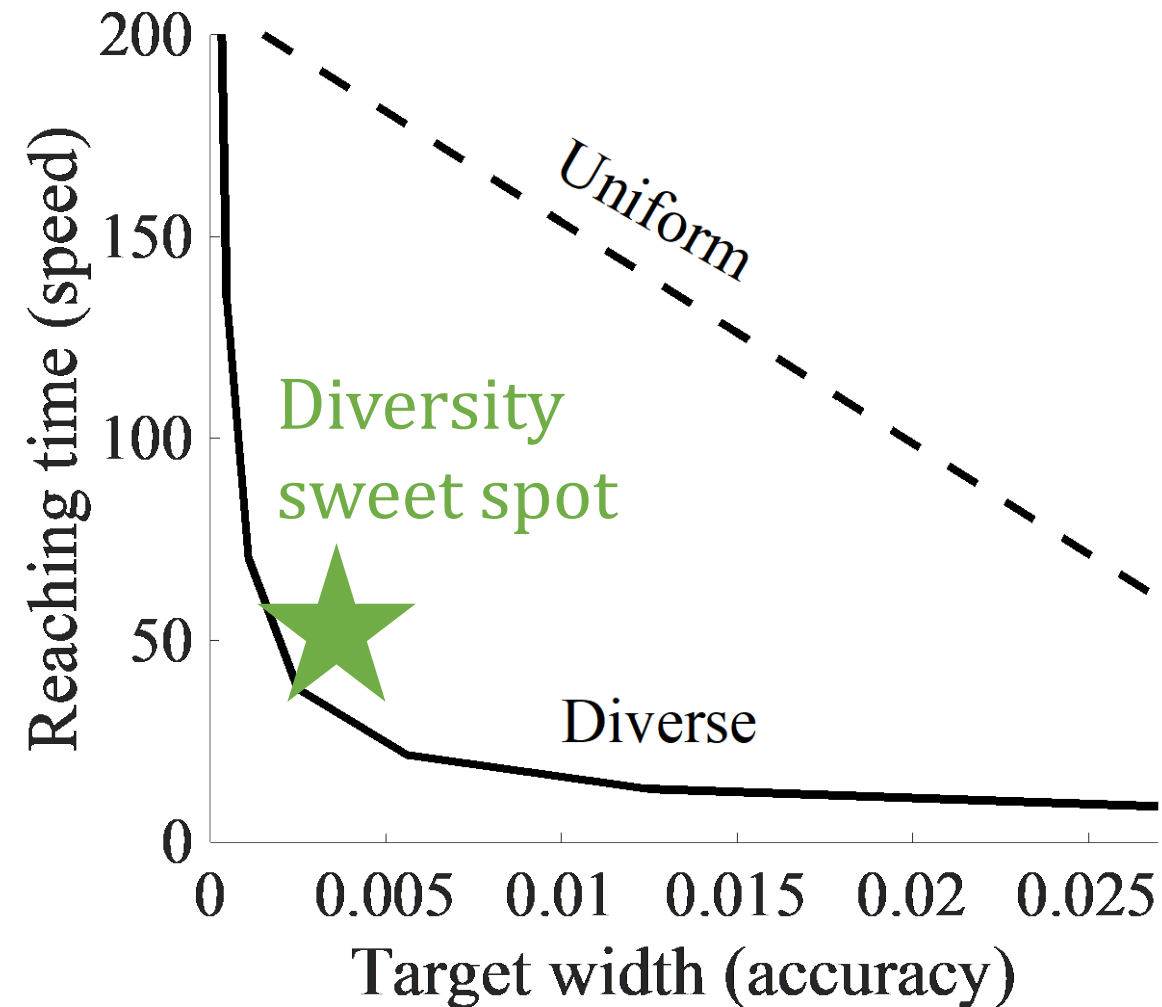


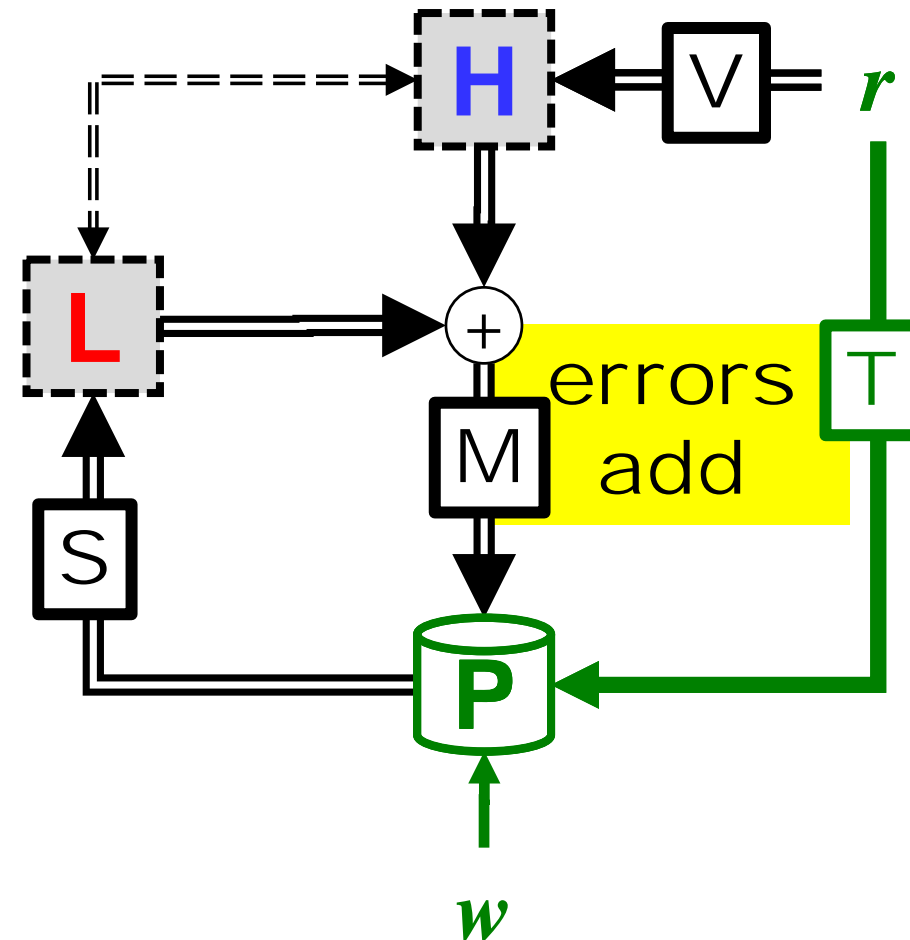
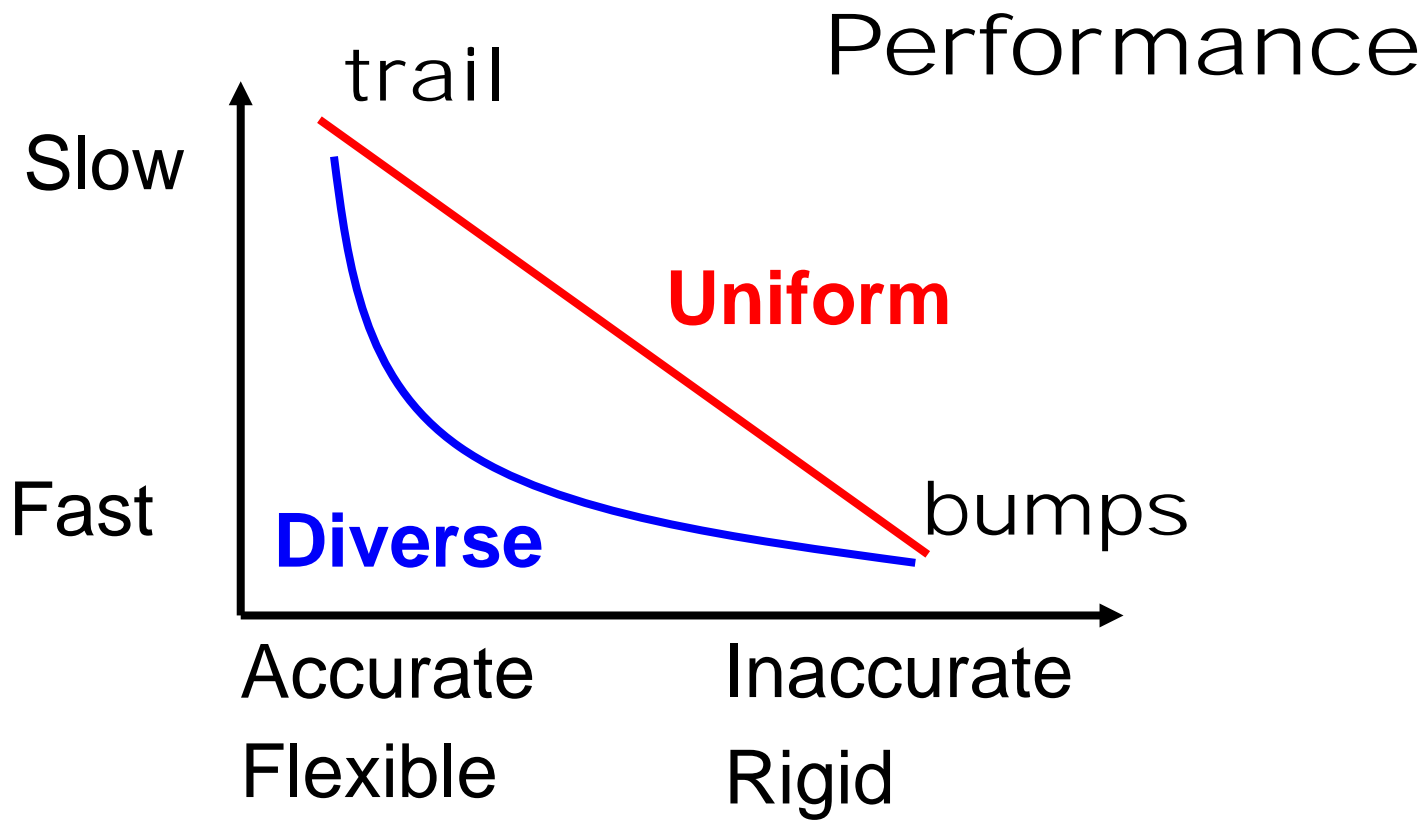
Fitts law

$$\text{Reaching time} = a + b \log_2 \left(\frac{2D}{W} \right)$$

const

$$\text{Reaching time} = a + b \log_2\left(\frac{2D}{W}\right)$$





Diversity sweet spot
Diverse layers
 (between nerves)

bumps

trail

$$\delta \left(\sum_{i=1}^T |a^{i-1}| + |a^T| \left(2^{\lambda T} - |a| \right)^{-1} \right) + \left(2^V - |a| \right)^{-1}$$

Game

Display 1 | Free Aspect

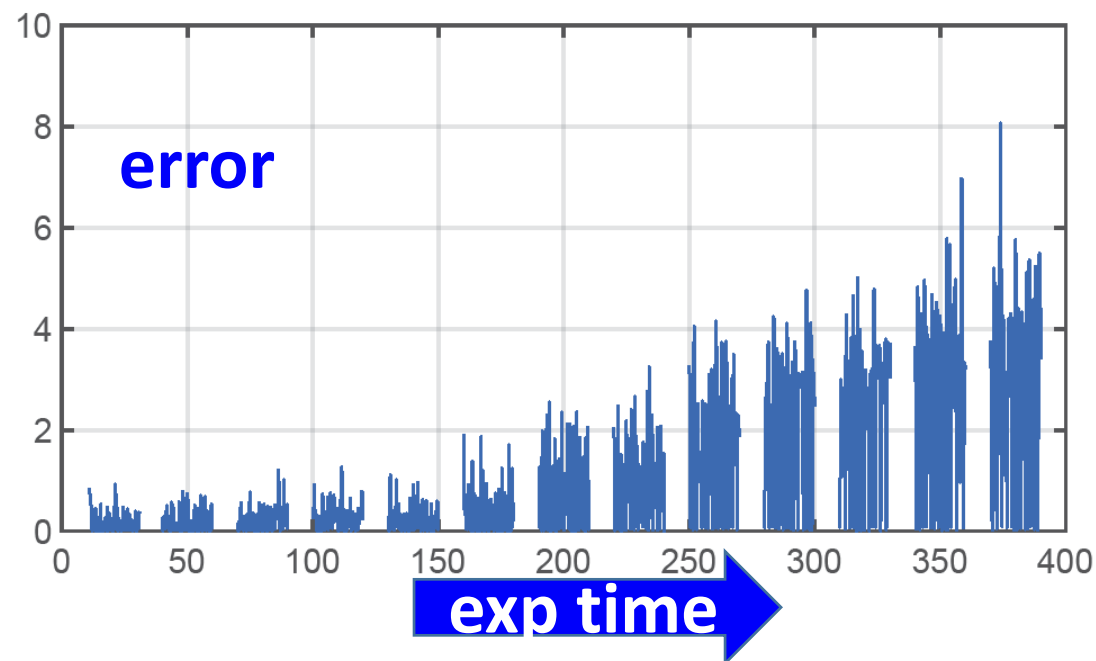
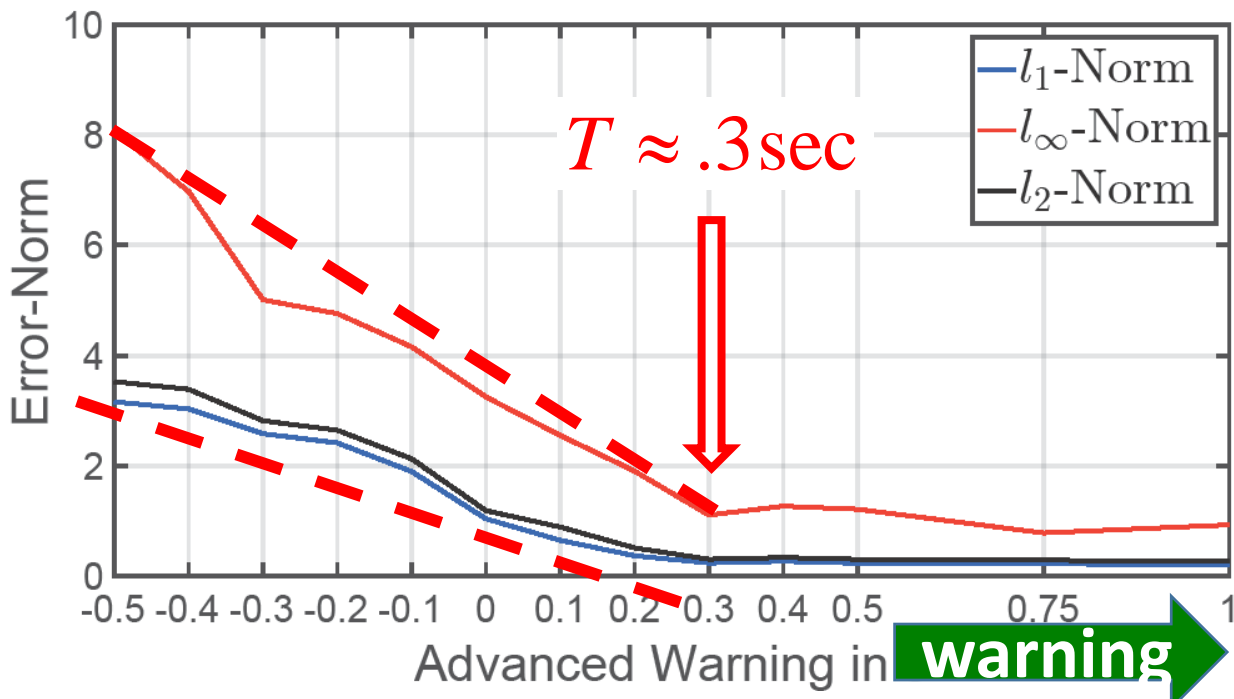
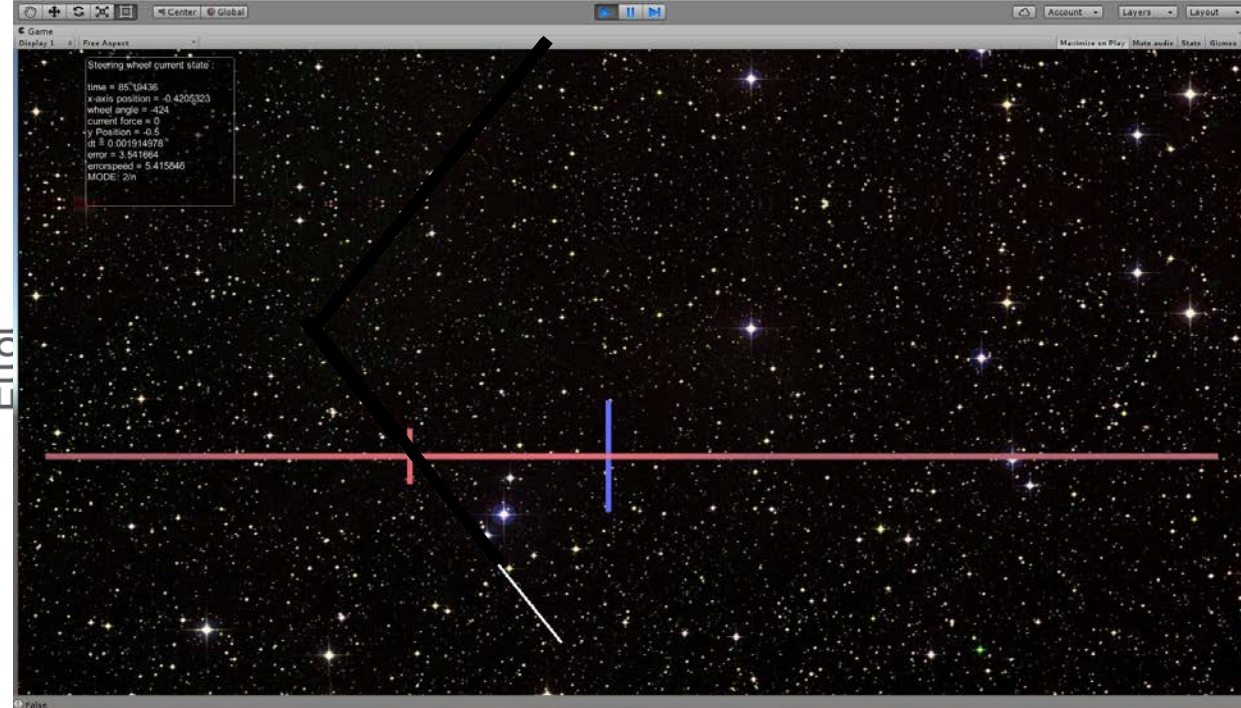
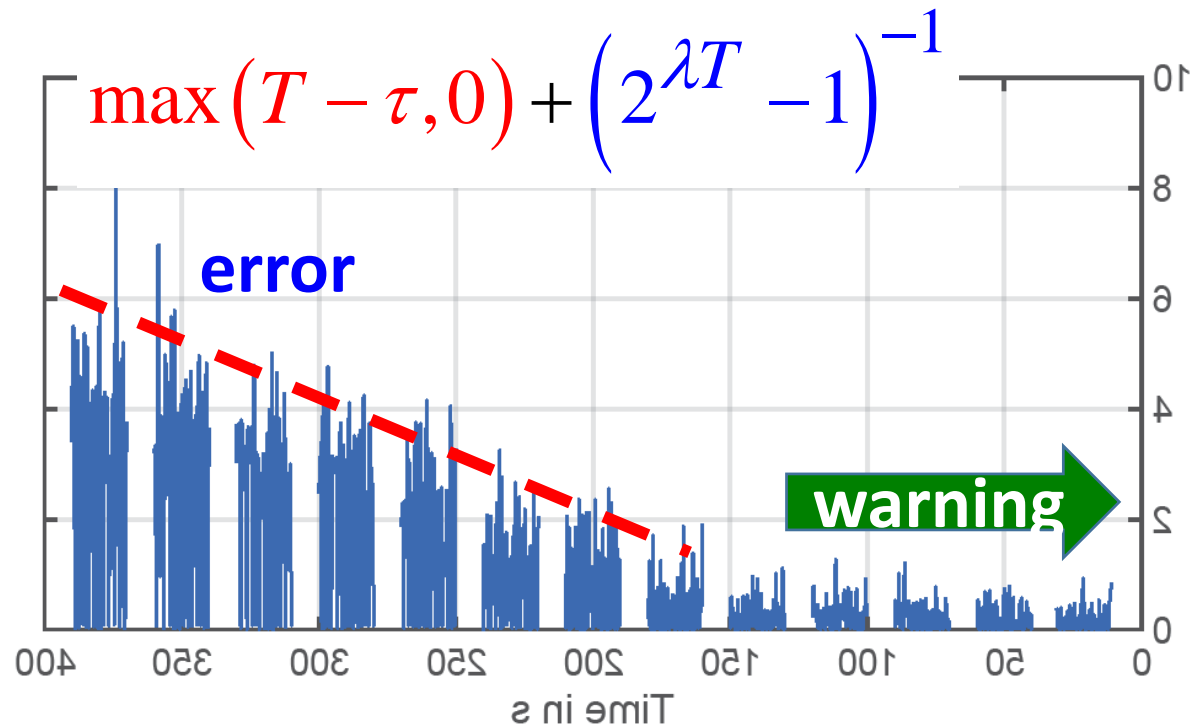
Maximize on Play | Mute audio | Stats | Gizmos

```
Steering wheel current state :  
time = 85.19436  
x-axis position = -0.4205323  
wheel angle = -424  
current force = 0  
y Position = -0.5  
dt = 0.001914978  
error = 3.541664  
errorspeed = 5.415846  
MODE: 2/n
```

Trail only

False

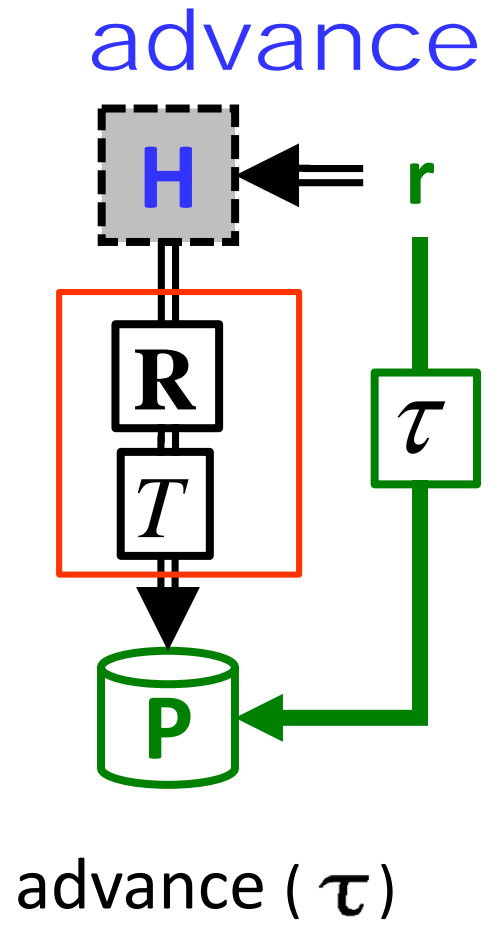
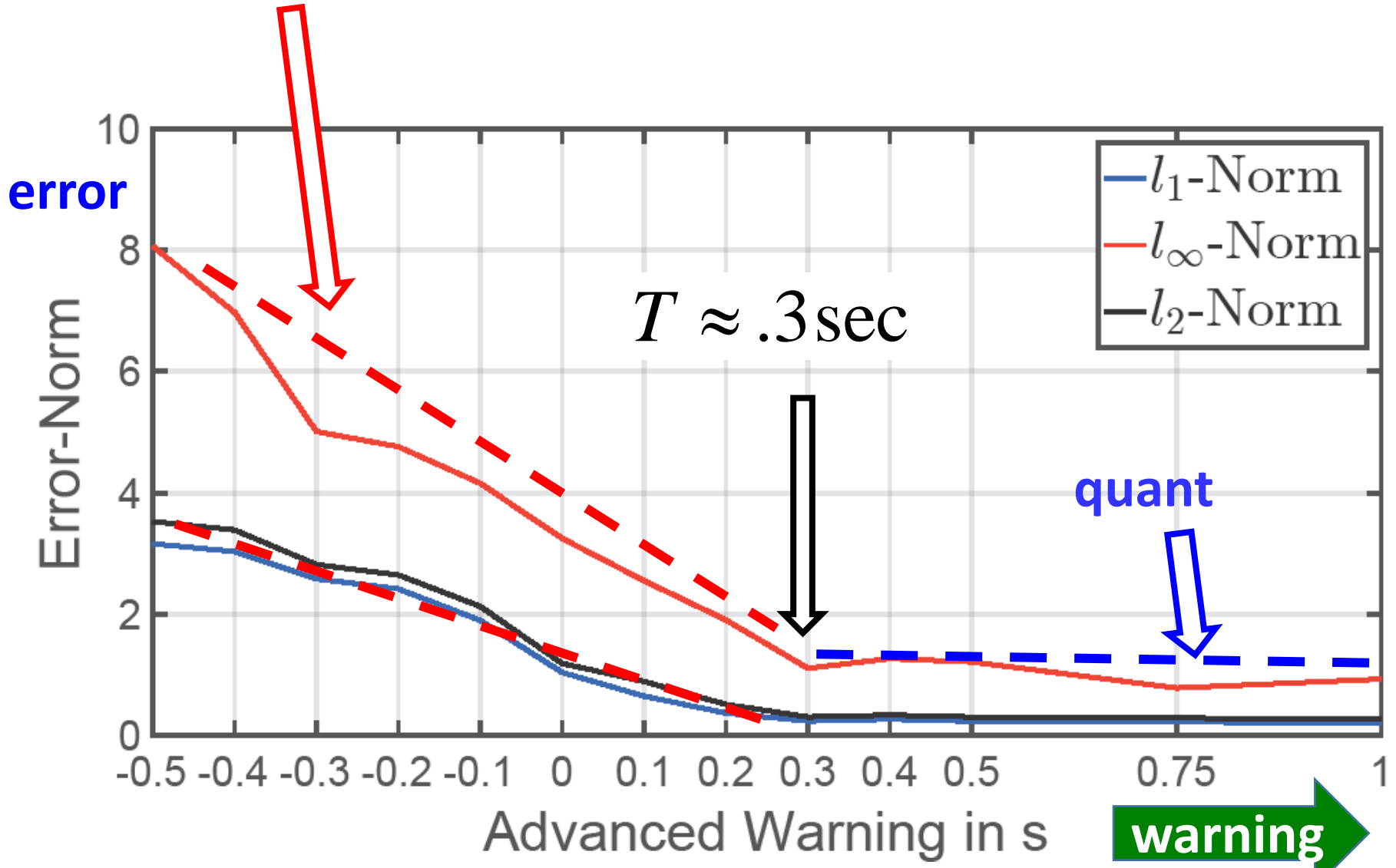
The image shows a game window with a starfield background. A white V-shaped trail is drawn across the center. A red horizontal line is drawn across the bottom, and a blue vertical line is drawn on the right side. A text box in the top-left corner displays the following data: "Steering wheel current state :", "time = 85.19436", "x-axis position = -0.4205323", "wheel angle = -424", "current force = 0", "y Position = -0.5", "dt = 0.001914978", "error = 3.541664", "errorspeed = 5.415846", and "MODE: 2/n". The text "Trail only" is written in red in the center of the window. The text "False" is at the bottom-left corner.

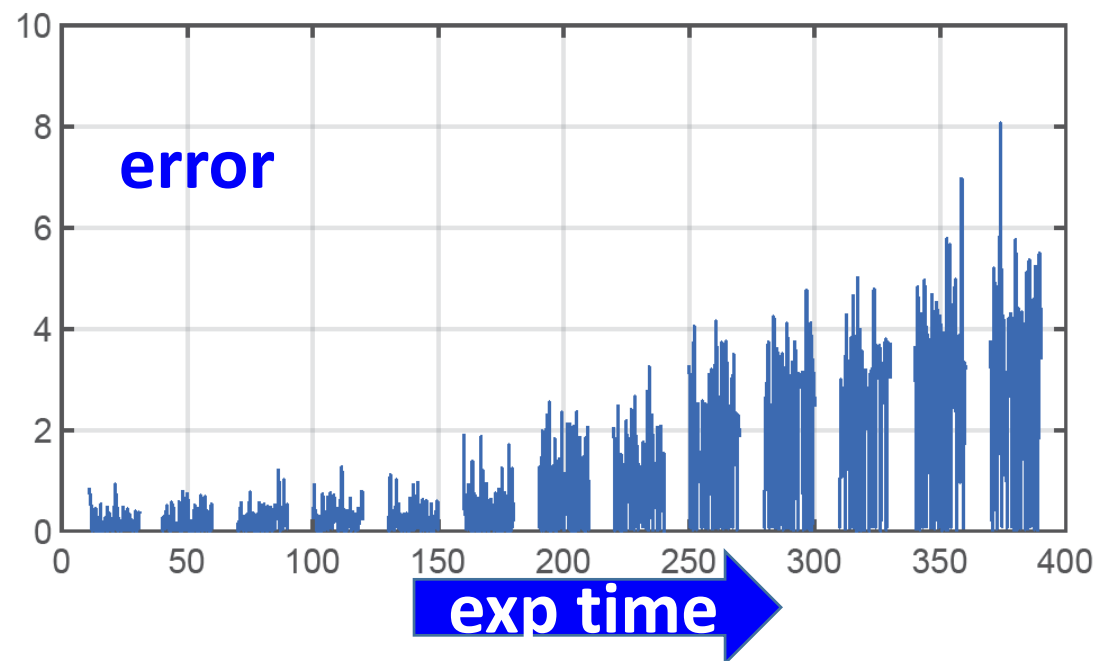
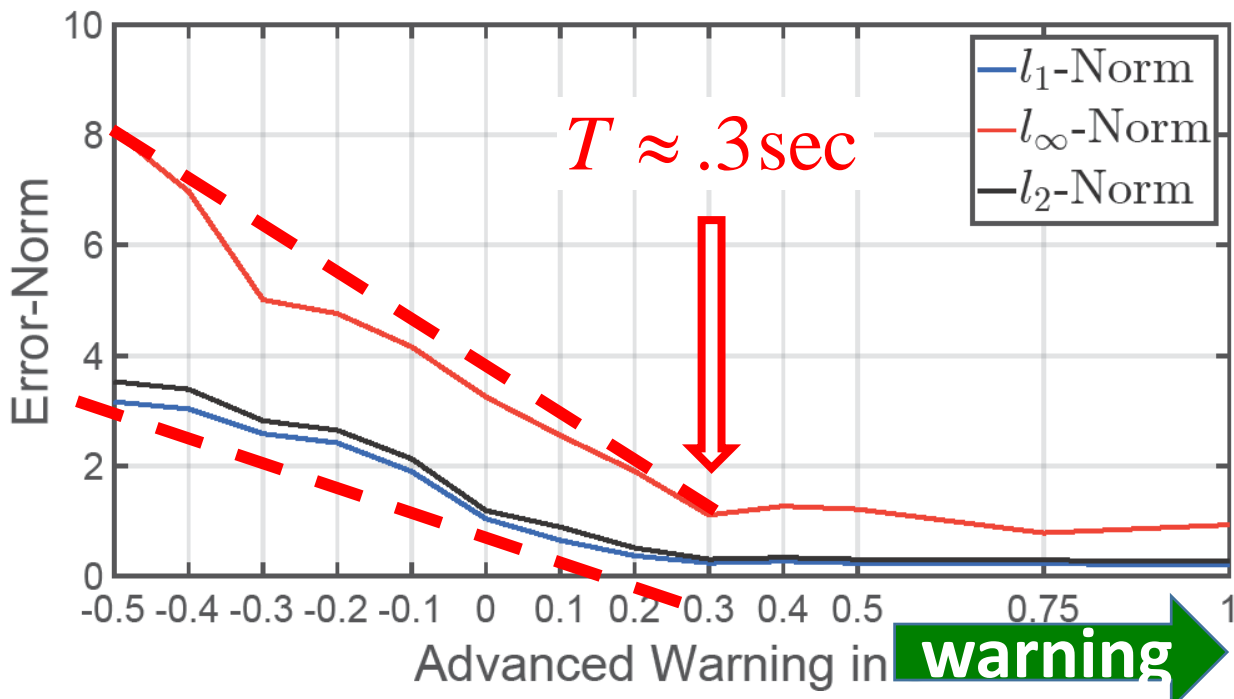
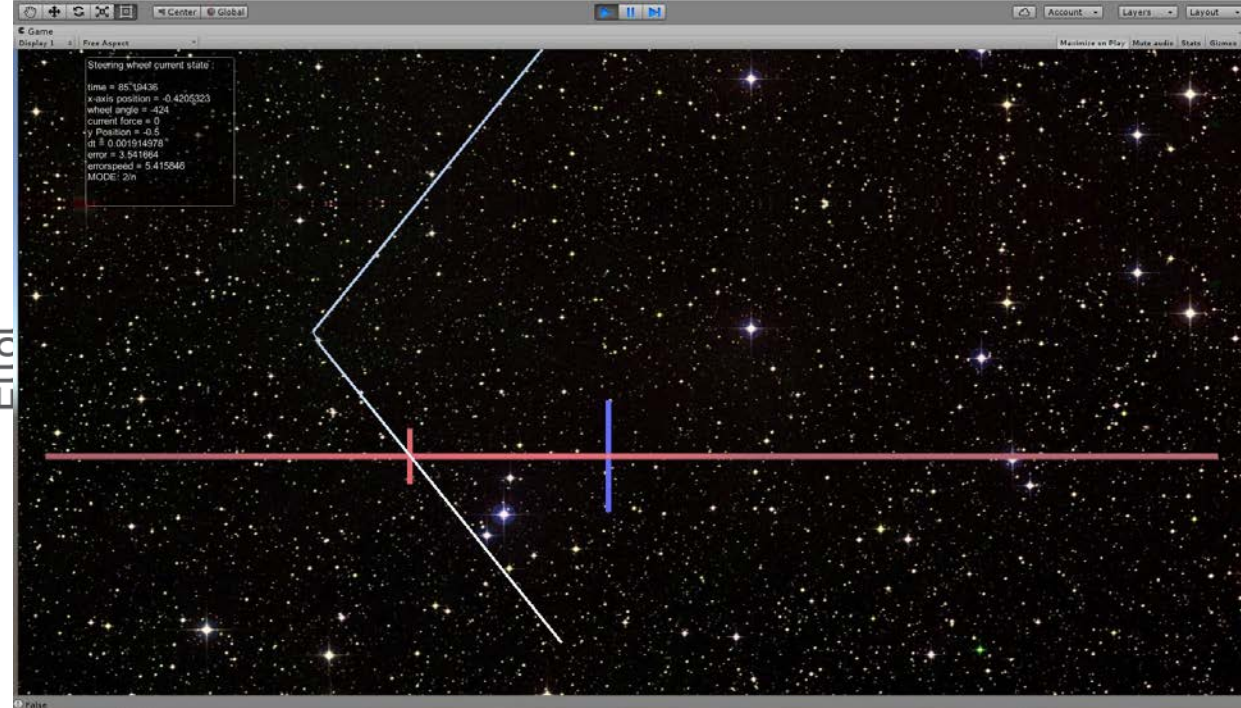
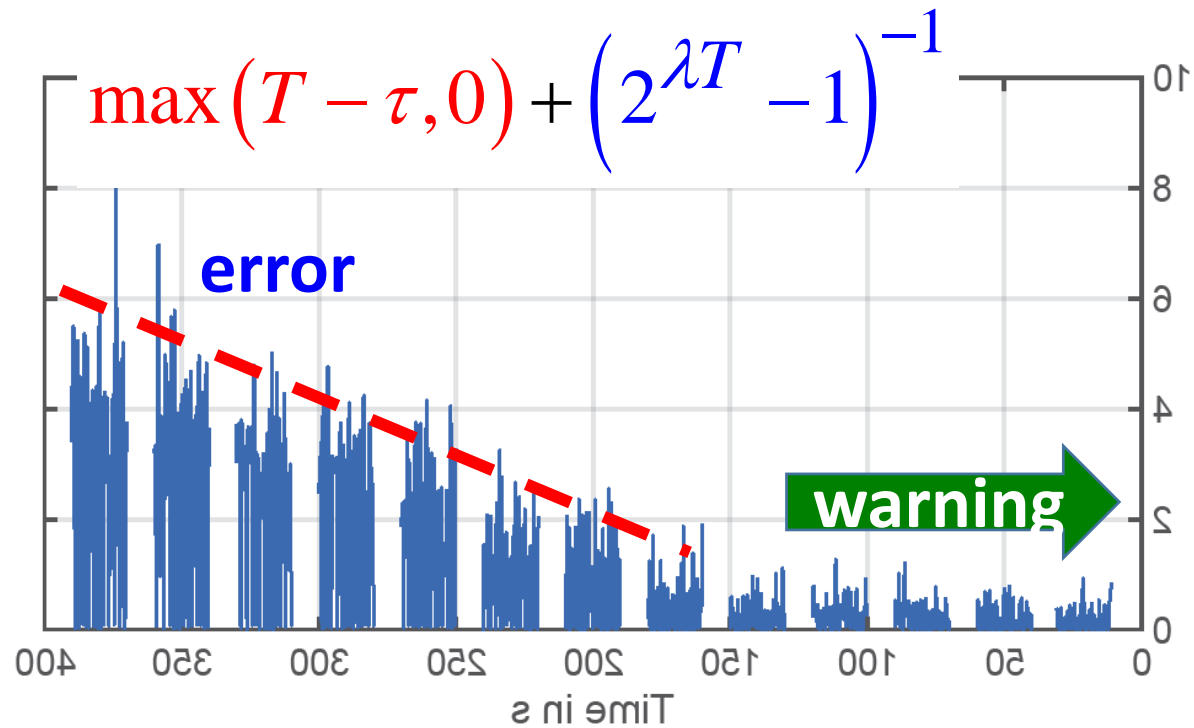


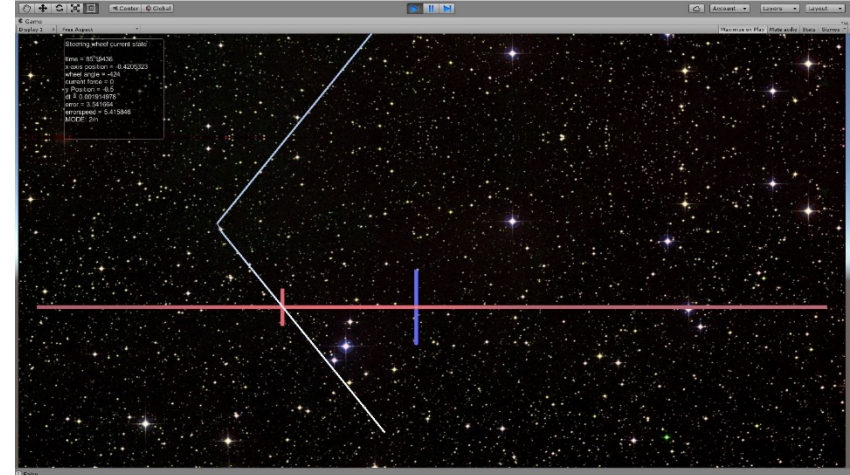
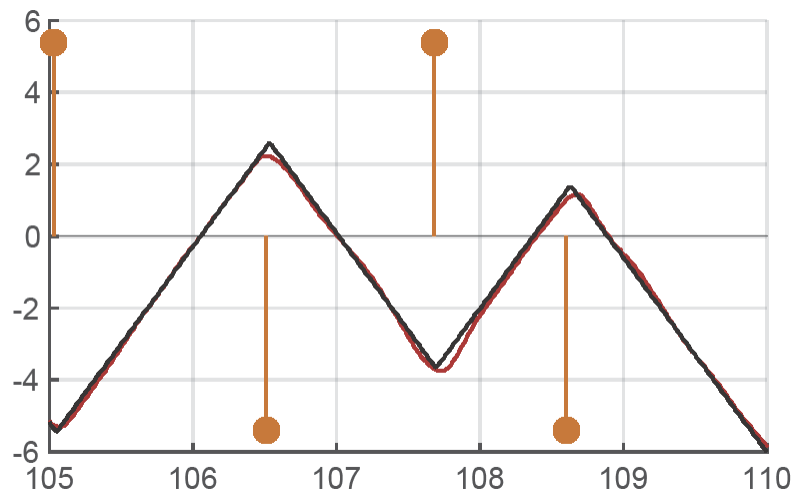
Warned system

$$\max(T - \tau, 0) + \left(2^{\lambda T} - 1\right)^{-1}$$

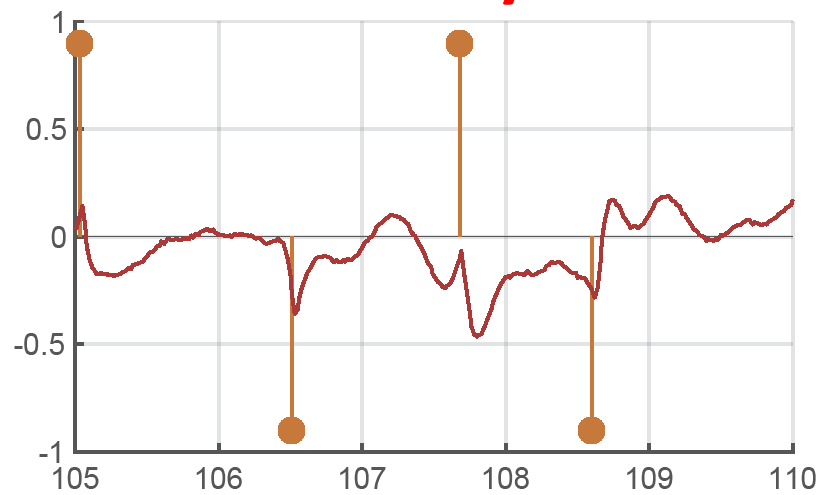
delay **quant**



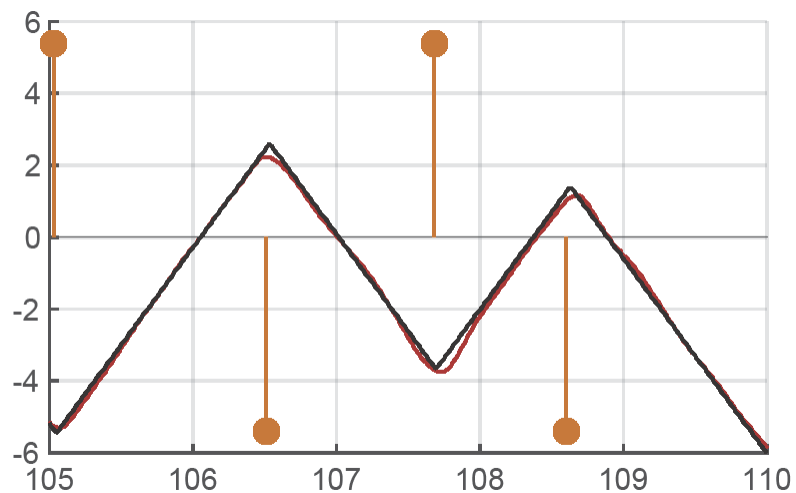
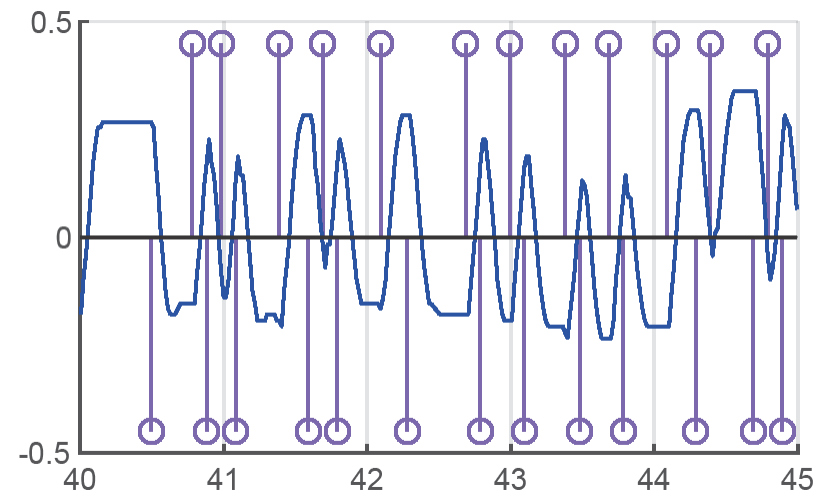




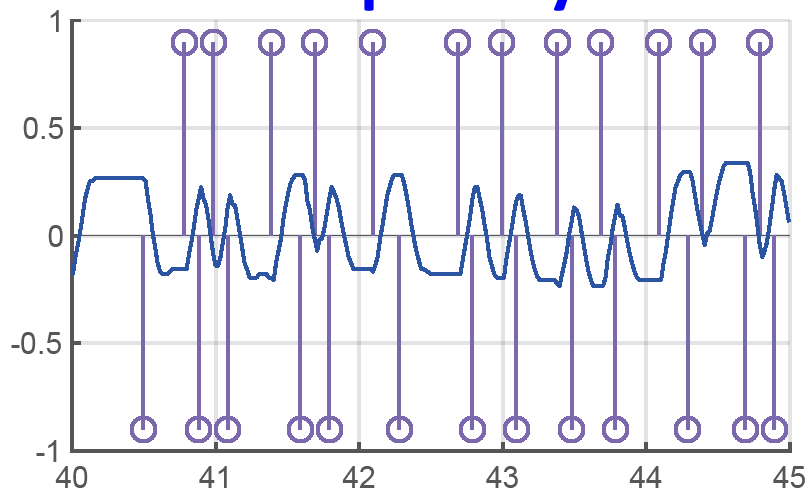
Trail only



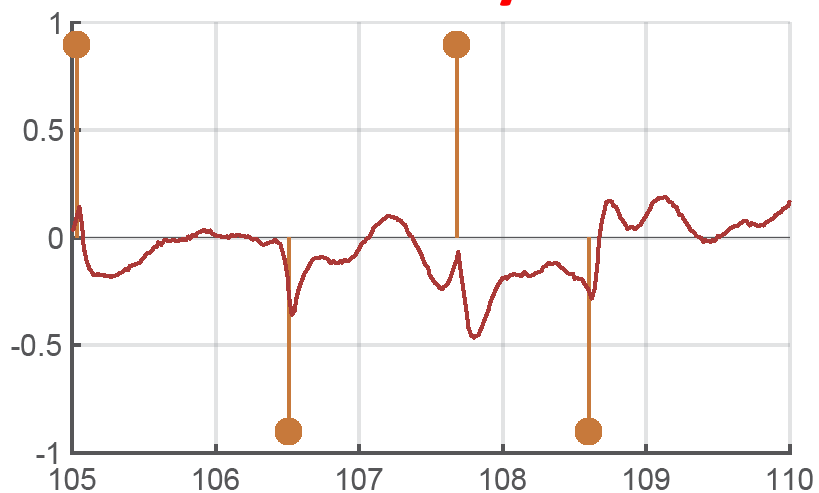
Errors



Bumps only

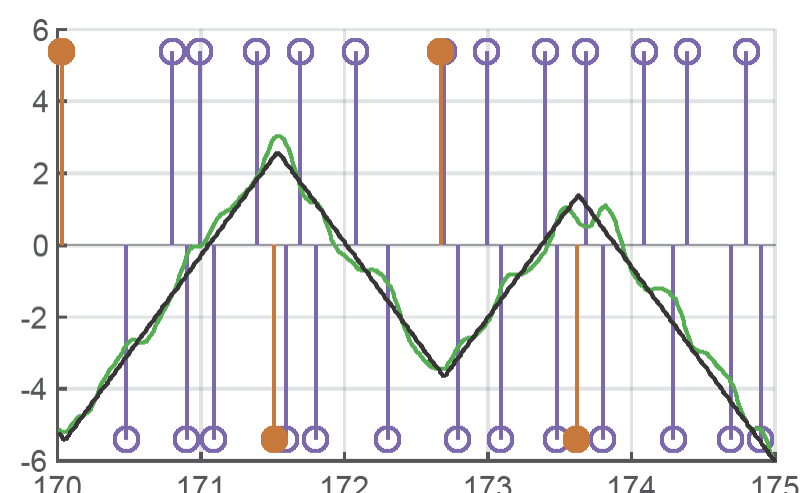
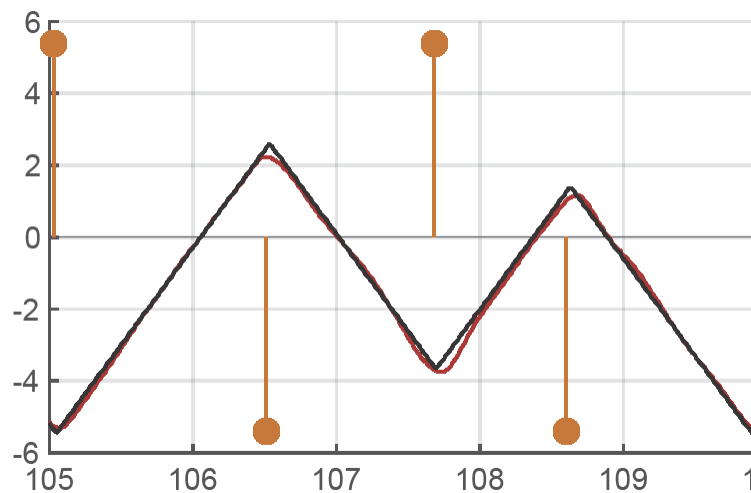
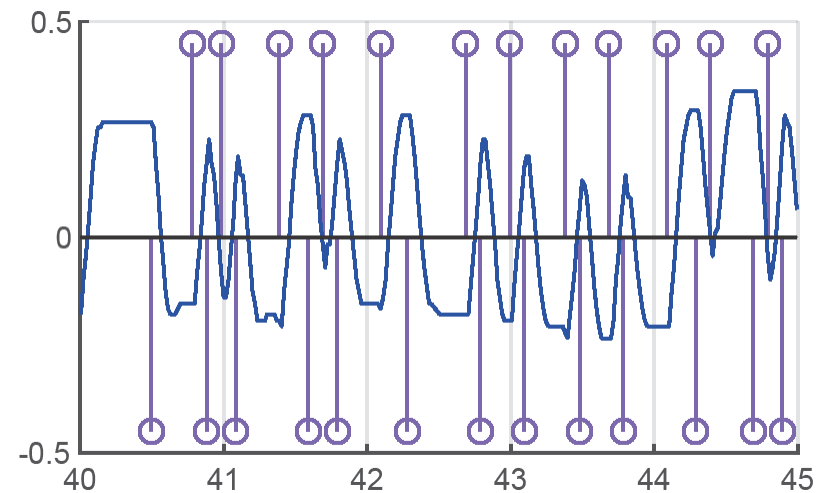


Trail only

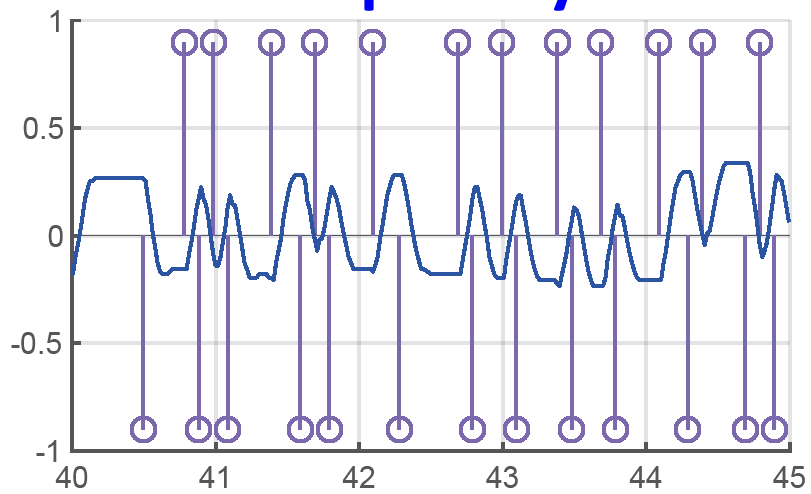


Errors

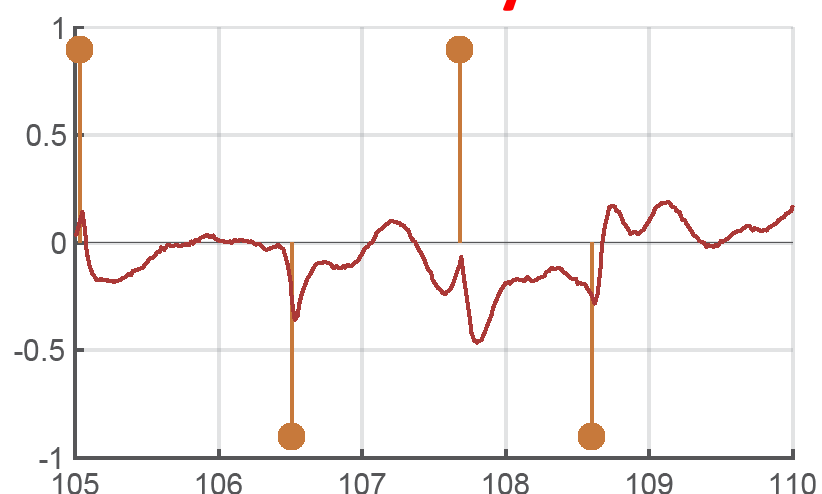
Errors



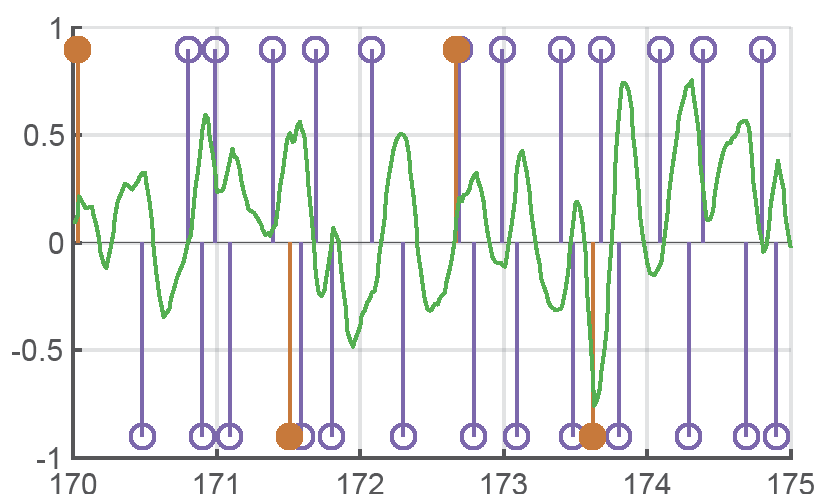
Bumps only



Trail only



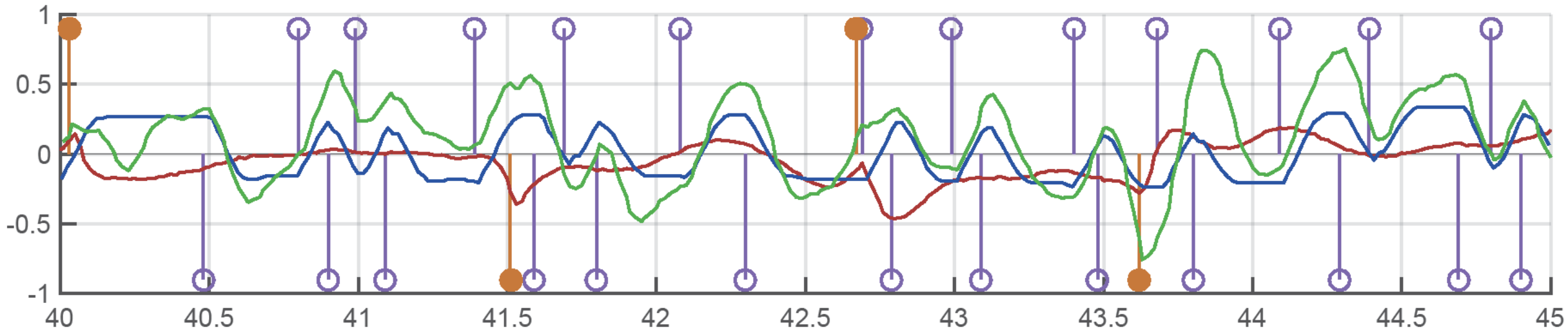
Both



Errors

Errors

Errors



Errors

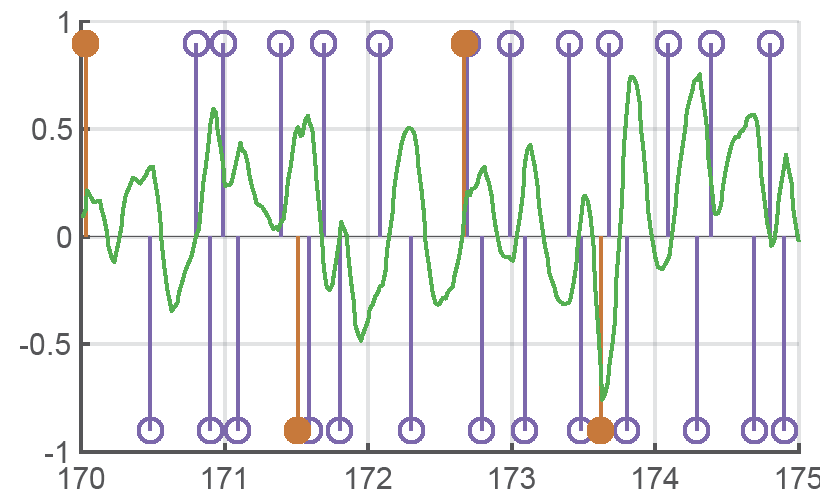
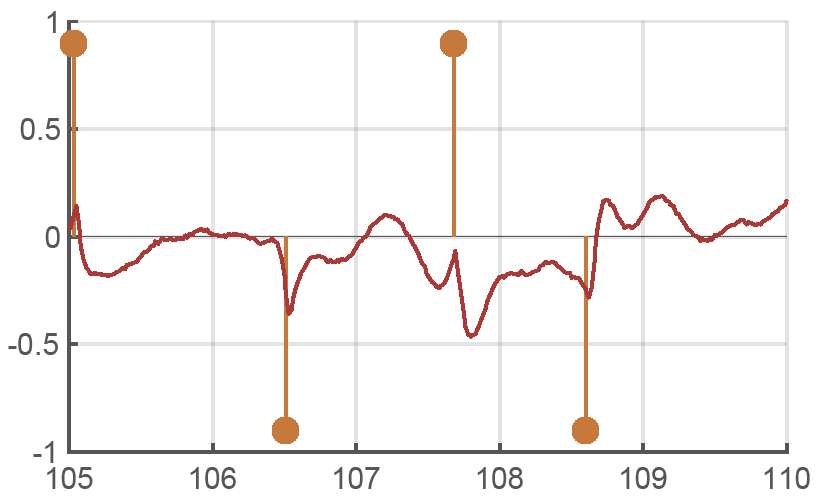
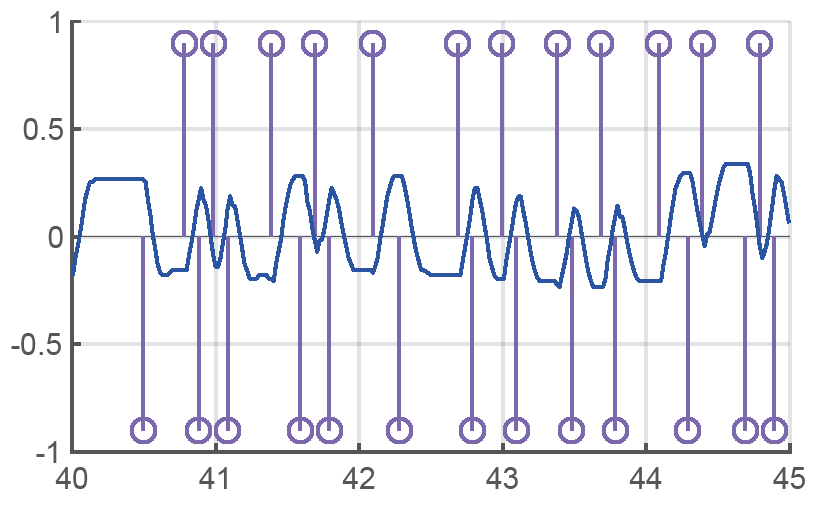
Bumps only

+

Trail only

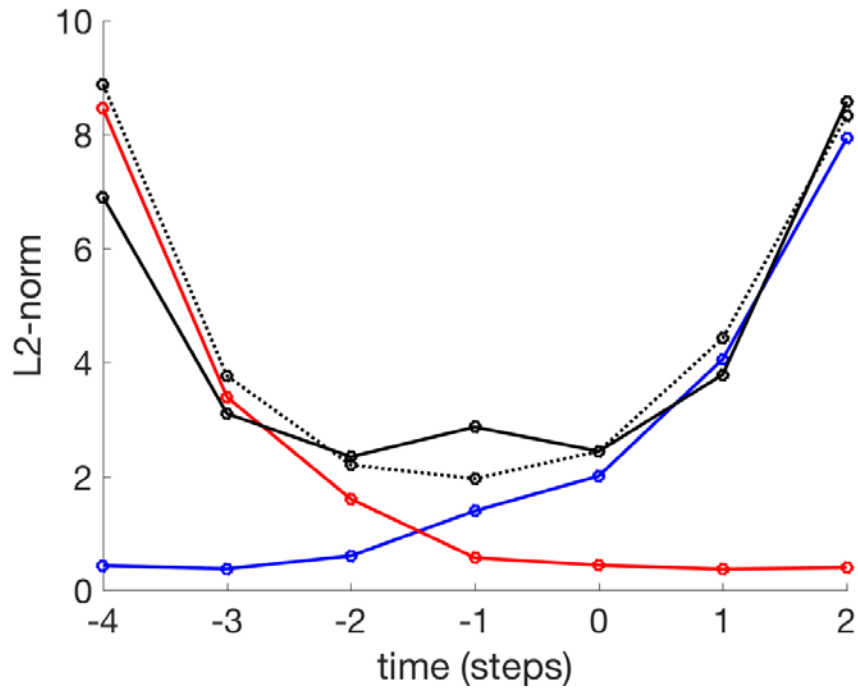
≈

Both



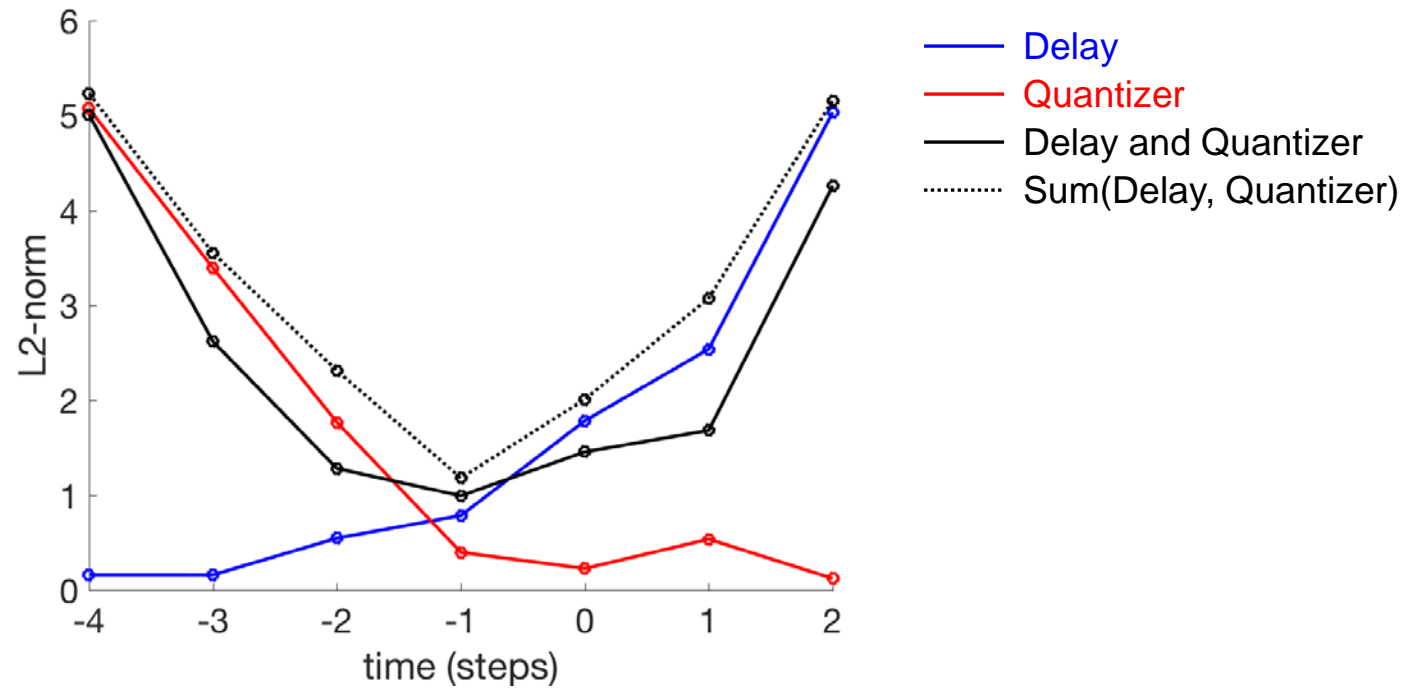
Virtualized (added) speed-accuracy tradeoff

- Delay session: 30 second for each setting ($T = -4, -3, -2, -1, 0, 1, 2$)
- Quantizer session: 30 second (L = 1, 2, ..., 7)
- Delay and Quantizer session: 30 second for each pair of settings



Advance warning

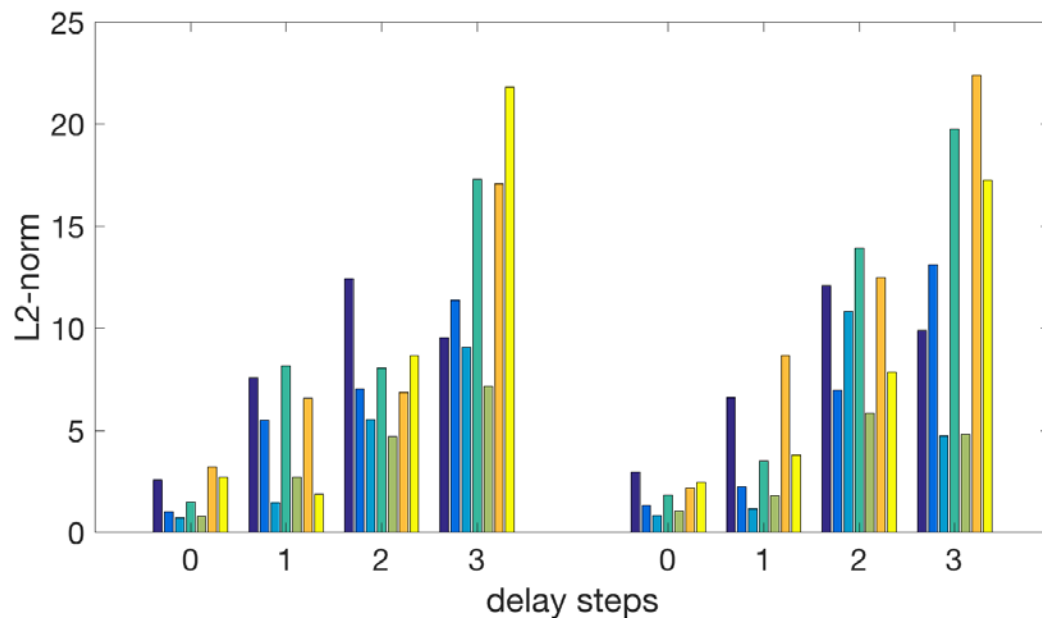
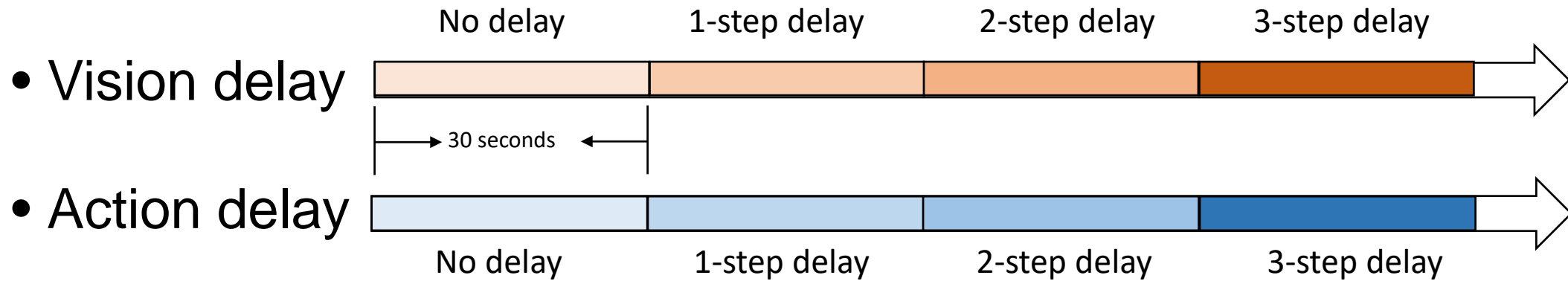
Delay



Advance warning

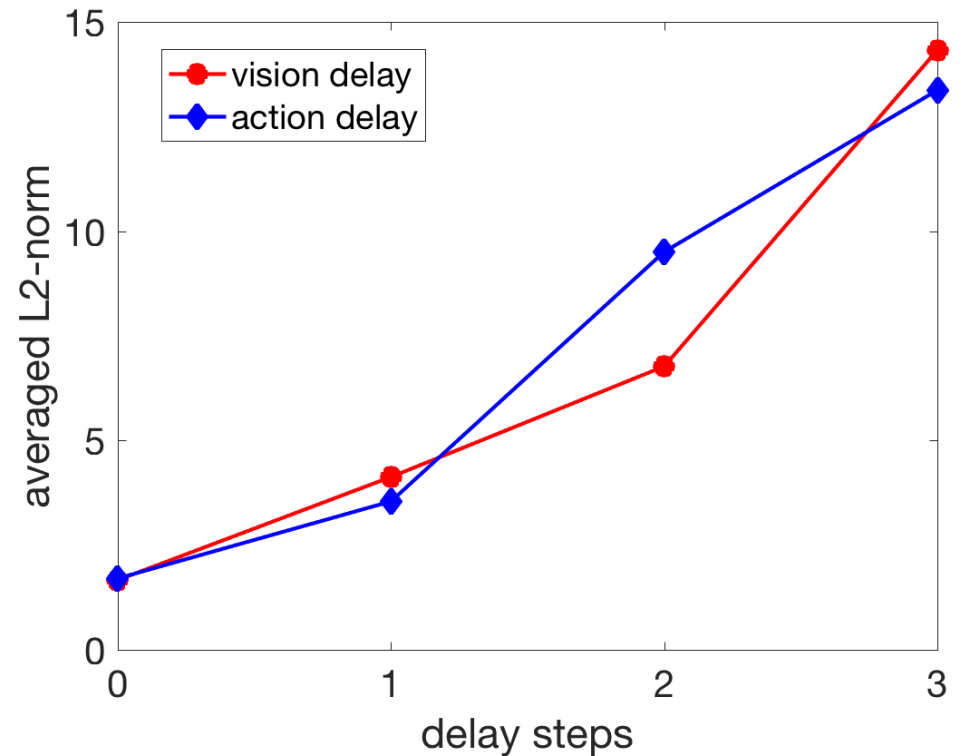
Delay

Delay in vision and in action

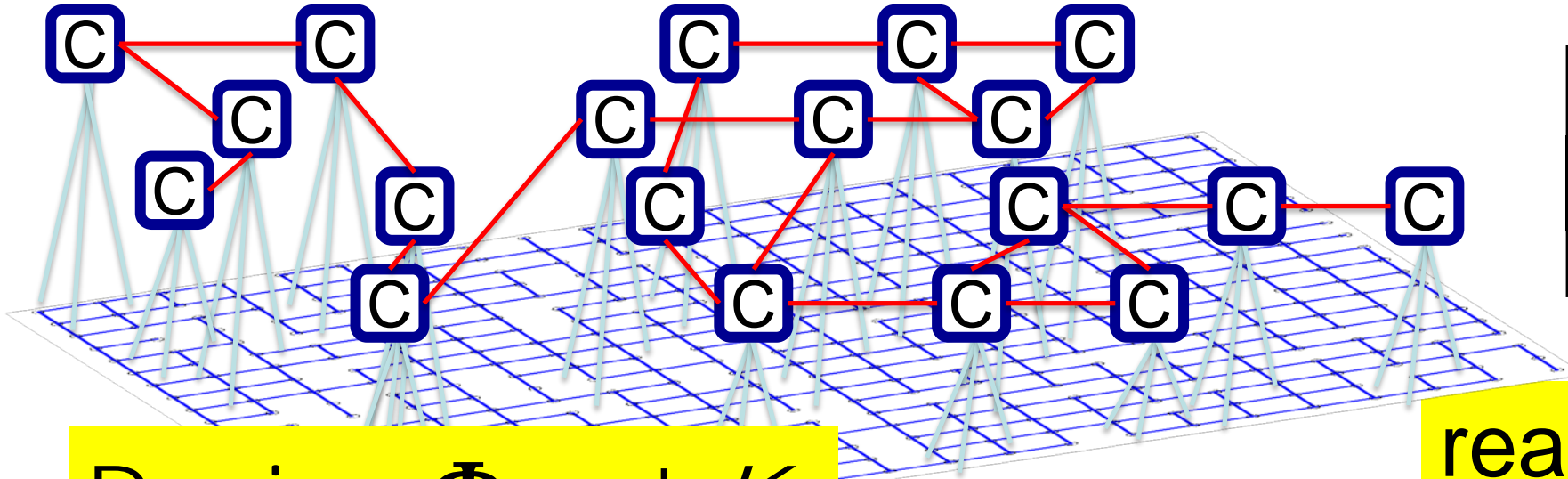


Vision delay

Action delay



Sparse sense, comms, comp, ctrl, act



$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

Design Φ not K .

realizable ($\exists K$) iff

Affine constraint

$$\begin{bmatrix} zI - A & -B \end{bmatrix} \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} = I$$

State feedback

$$K = \Phi_{21} (\Phi_{11})^{-1}$$

Spacetime/sparsity constraints
are convex in Φ but not in K .

$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

local, strictly causal,
sparse, structured

Design Φ not K .

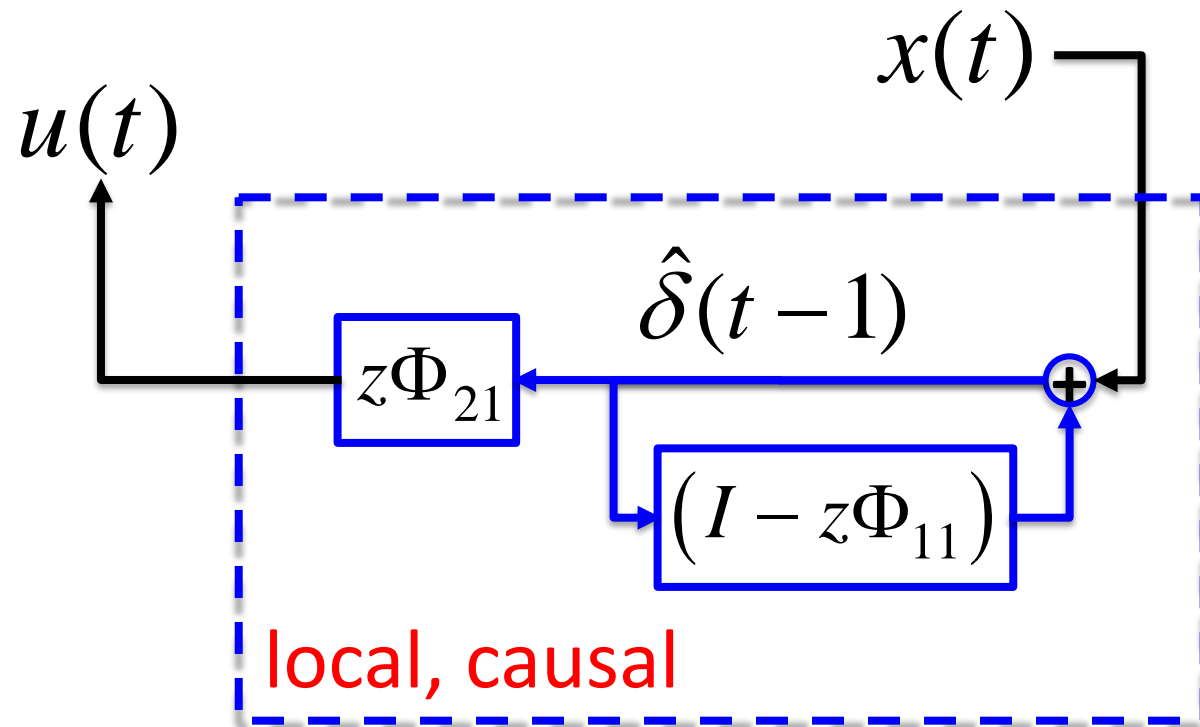
$$K = \Phi_{21} (\Phi_{11})^{-1}$$

Spacetime/sparsity constraints are convex in Φ but not in K .

This is a very complicated but interesting way to implement K .

$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

local, strictly causal



$$\begin{aligned} K &= \Phi_{21} (\Phi_{11})^{-1} \\ &= z\Phi_{21} (z\Phi_{11})^{-1} \\ &= z\Phi_{21} [I - (I - z\Phi_{11})]^{-1} \end{aligned}$$

local, causal

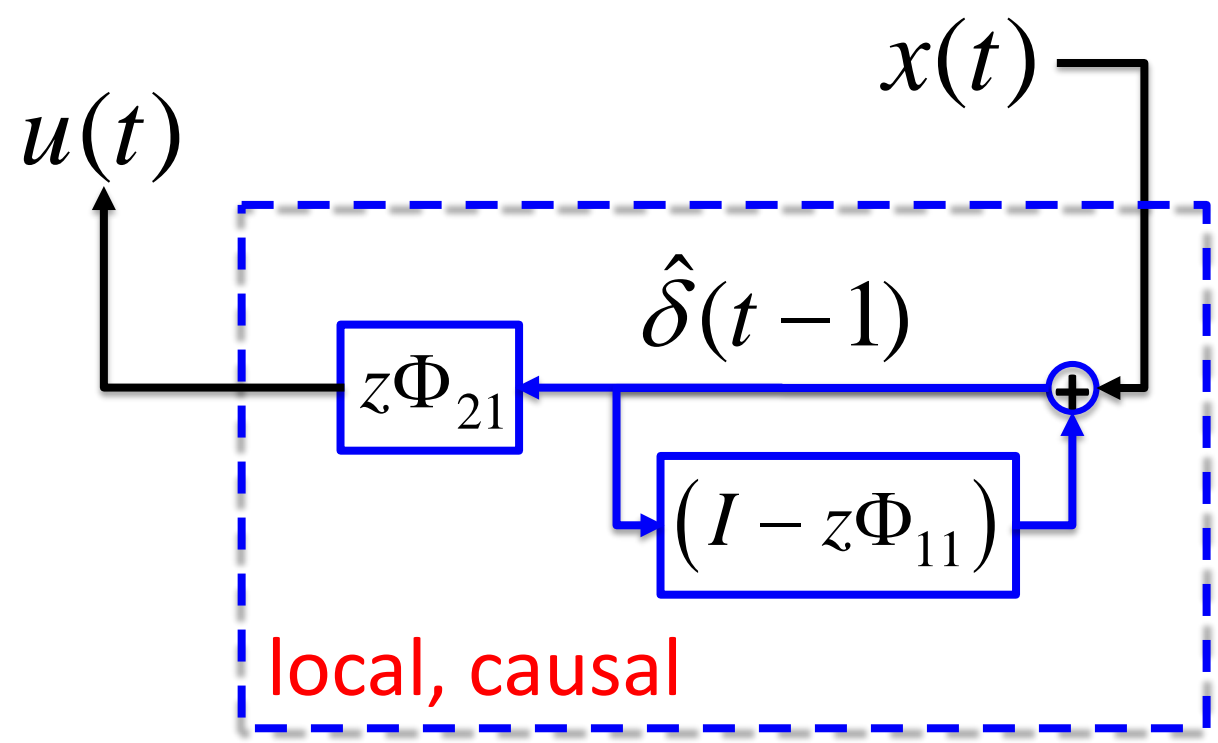
Spacetime/sparsity constraints are convex in Φ but not in K .

This is a very complicated but interesting way to implement K .

The interpretation of the controller components is clear however

$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

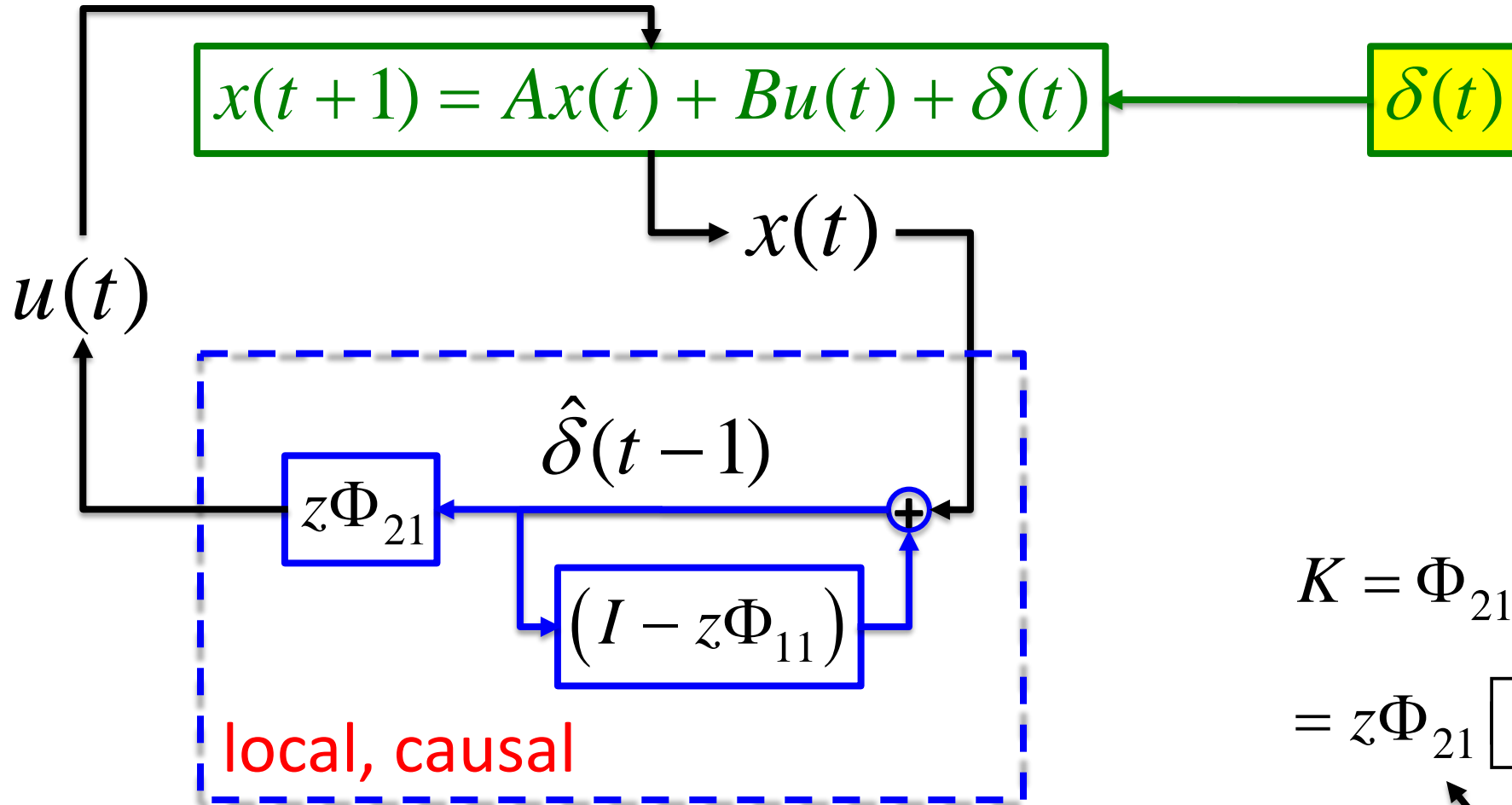
local, strictly causal



$$\begin{aligned} K &= \Phi_{21} (\Phi_{11})^{-1} \\ &= z\Phi_{21} (z\Phi_{11})^{-1} \\ &= z\Phi_{21} [I - (I - z\Phi_{11})]^{-1} \end{aligned}$$

local, causal

Plant



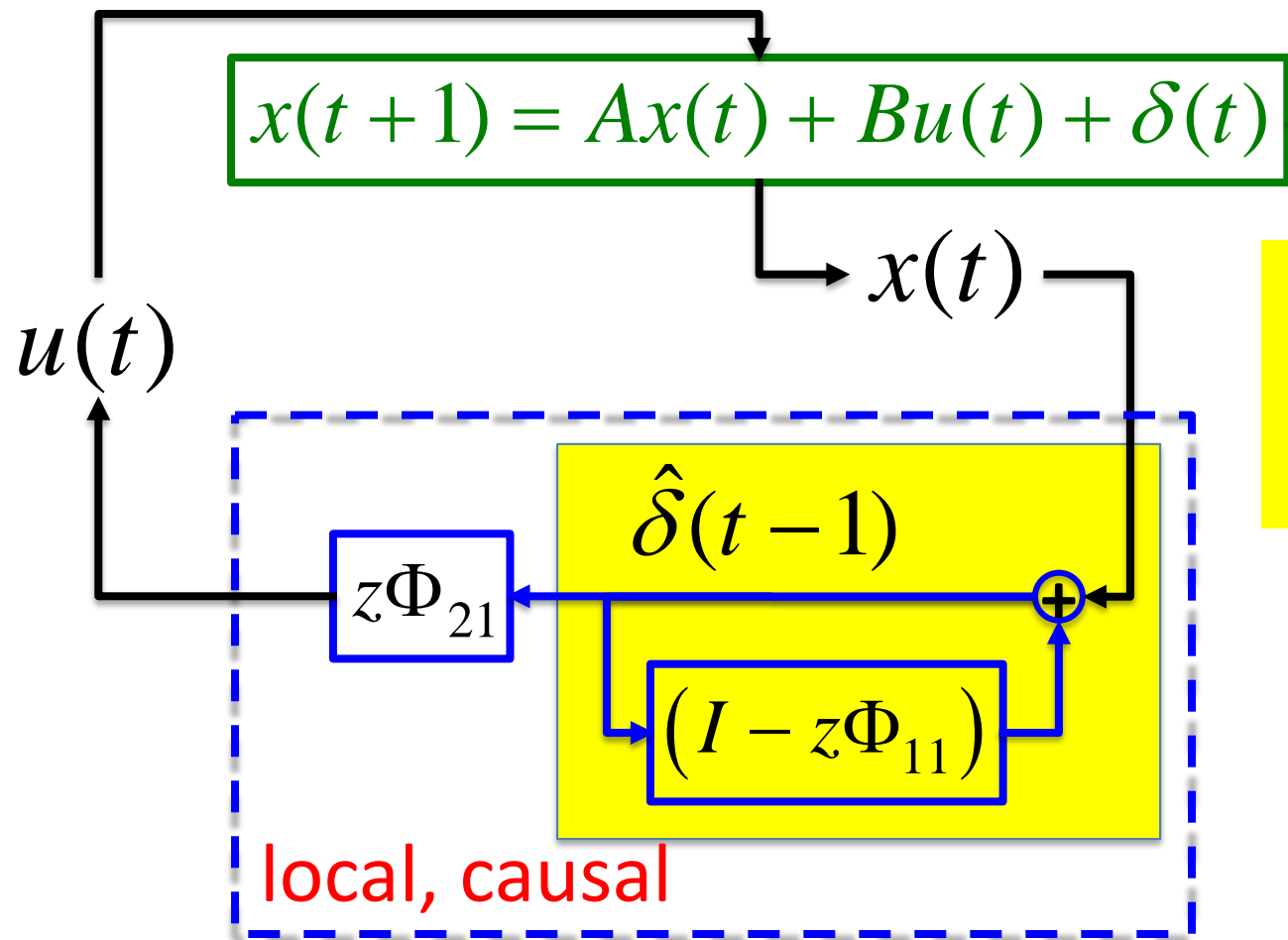
$$K = \Phi_{21} (\Phi_{11})^{-1}$$

$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

$$K = \Phi_{21} (\Phi_{11})^{-1}$$

$$= z\Phi_{21} [I - (I - z\Phi_{11})]^{-1}$$

local, causal



$$K = \Phi_{21} (\Phi_{11})^{-1}$$

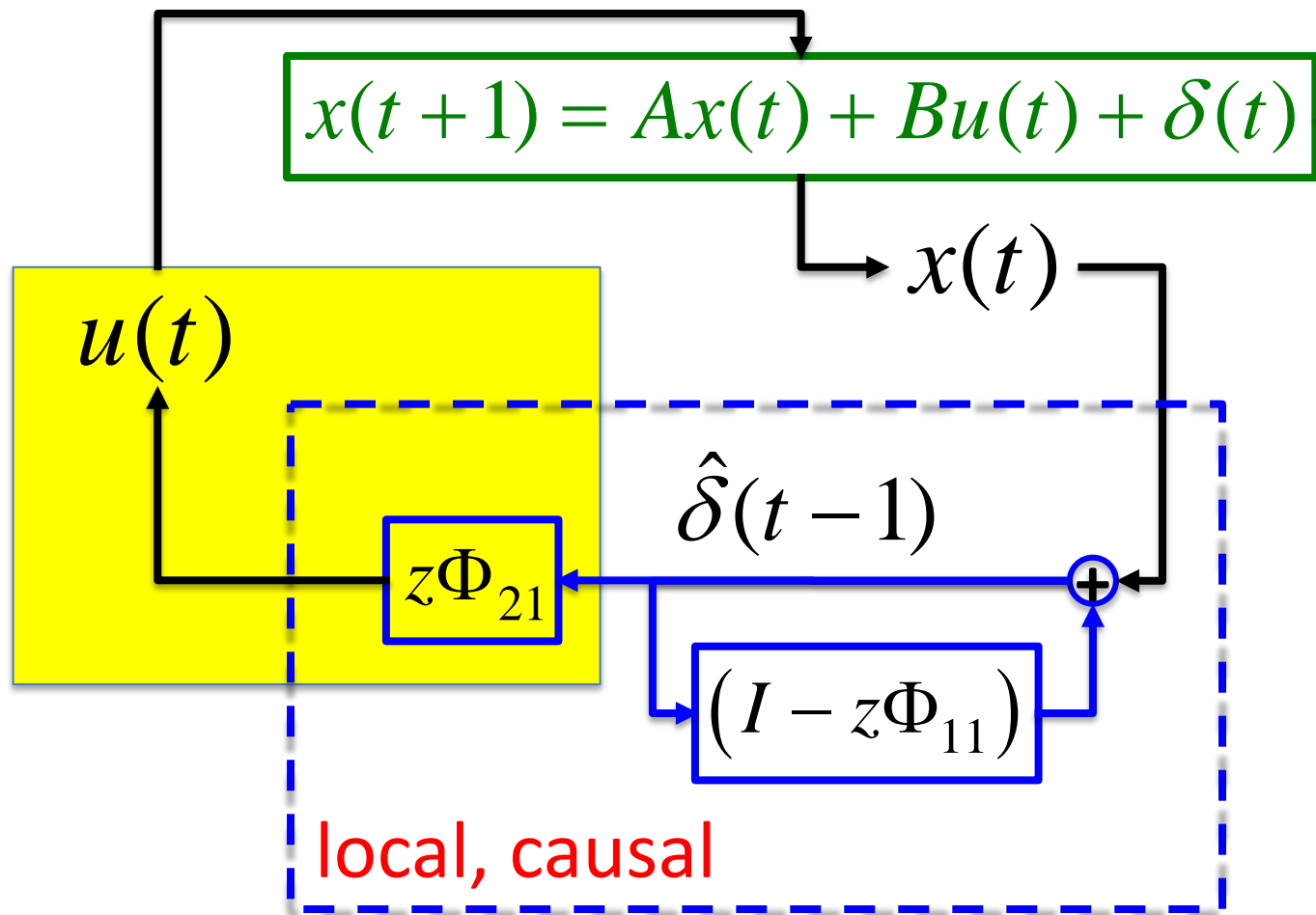
First, reconstruct δ from x

$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

$$K = \Phi_{21} (\Phi_{11})^{-1}$$

$$= z\Phi_{21} [I - (I - z\Phi_{11})]^{-1}$$

local, causal



$$K = \Phi_{21} (\Phi_{11})^{-1}$$

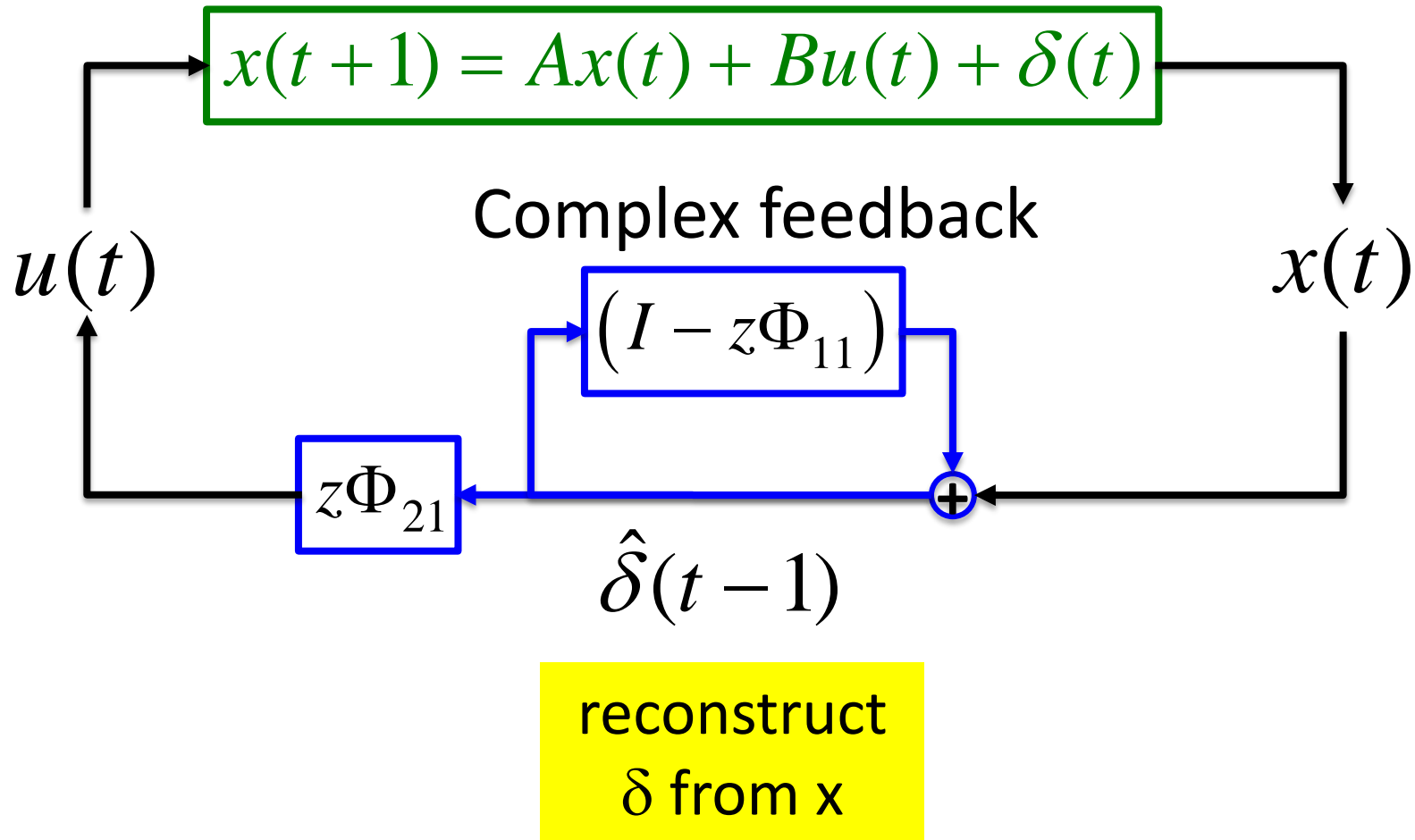
Then u is given

$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

$$K = \Phi_{21} (\Phi_{11})^{-1}$$

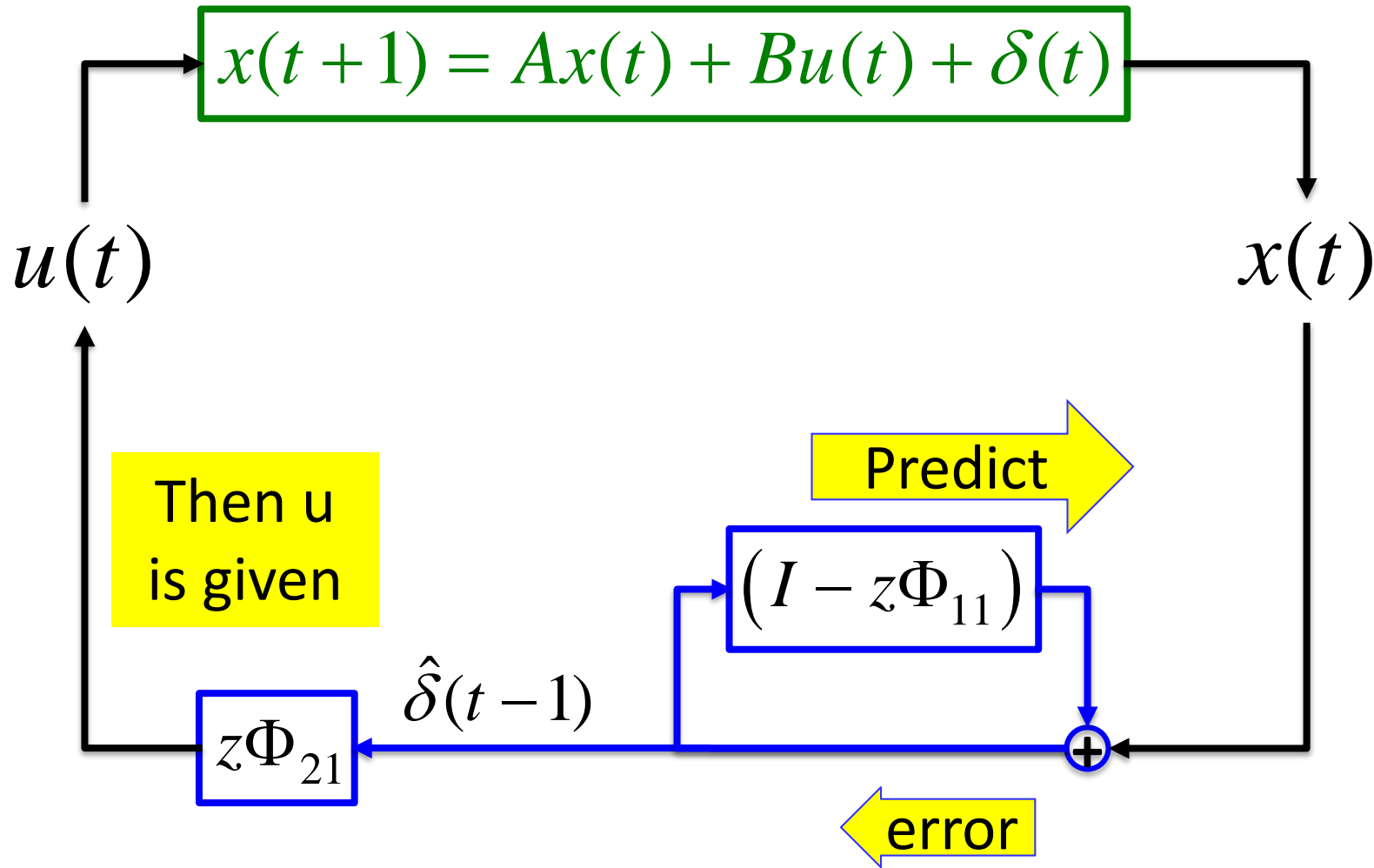
$$= z\Phi_{21} [I - (I - z\Phi_{11})]^{-1}$$

local, causal



$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

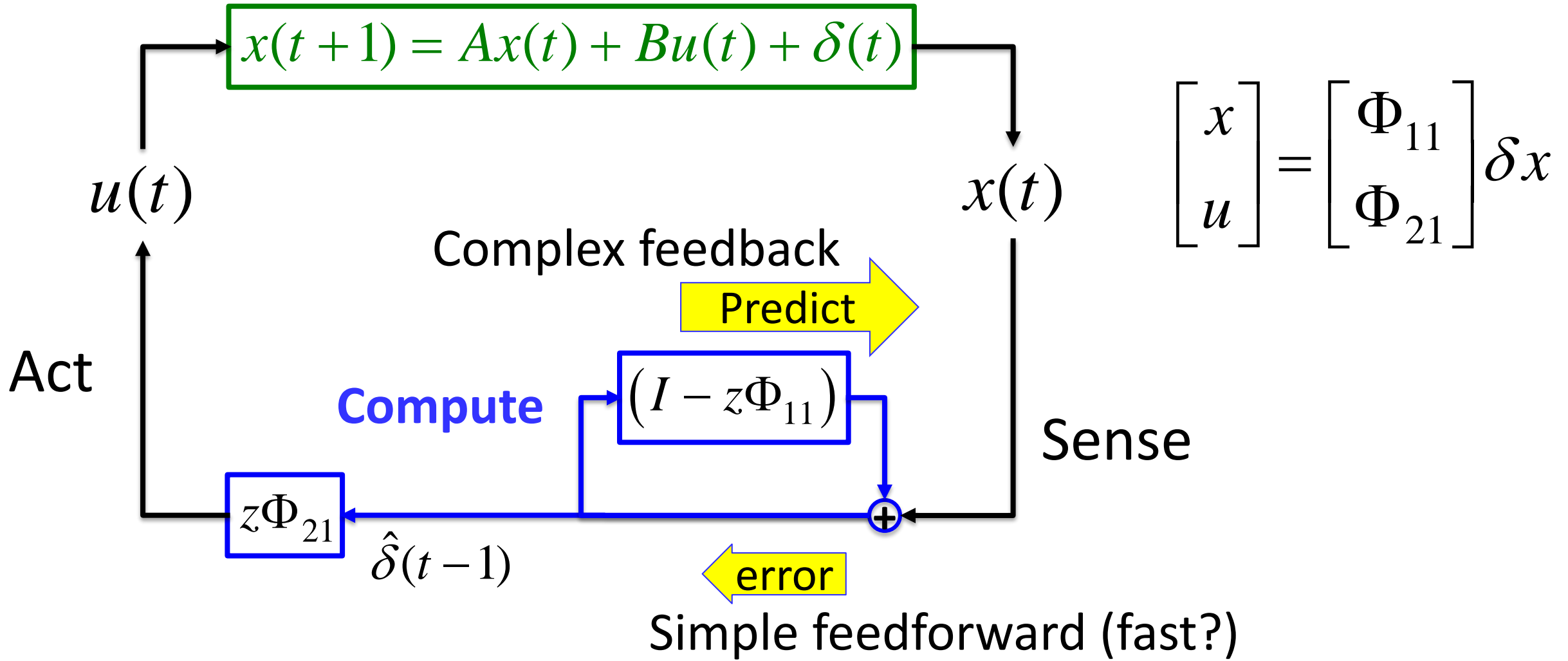
Why the feedback?



$$\begin{bmatrix} x \\ u \end{bmatrix} = \begin{bmatrix} \Phi_{11} \\ \Phi_{21} \end{bmatrix} \delta x$$

Why the feedback?

Controlled plant



A System Level Approach to Controller Synthesis

Yuh-Shyang Wang, *Member, IEEE*, Nikolai Matni, *Member, IEEE*, and John C. Doyle

Output feedback

$$\begin{bmatrix} zI - A & -B_2 \end{bmatrix} \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = \begin{bmatrix} I & 0 \end{bmatrix} \quad (20a)$$

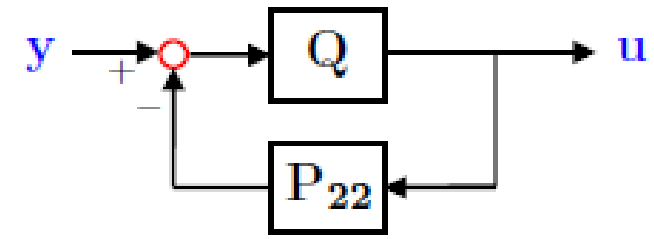
$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix} \quad (20b)$$

$$\mathbf{R}, \mathbf{M}, \mathbf{N} \in \frac{1}{\gamma} \mathcal{RH}_\infty, \quad \mathbf{L} \in \mathcal{RH}_\infty \quad (20c)$$

**Affine
constraint**

Special case: stable plant

$$\mathbf{Q} = \mathbf{L}$$

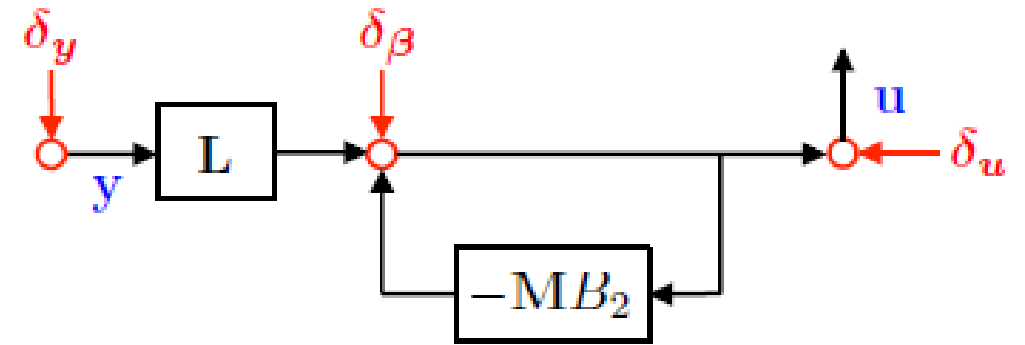


(a) Internal Model Control

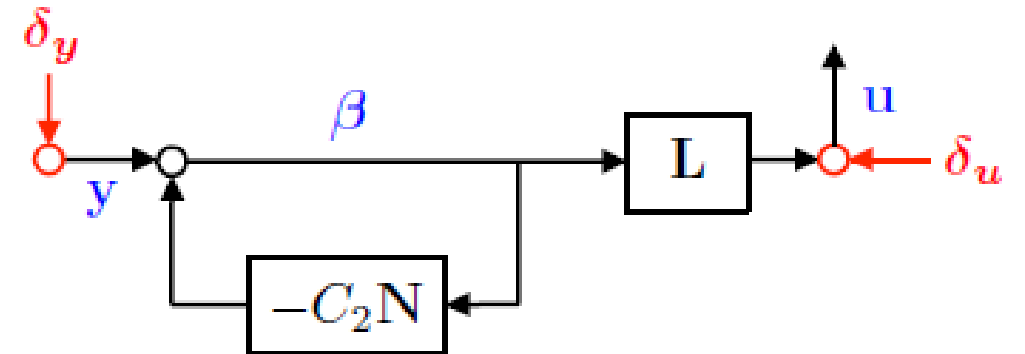
$$\begin{bmatrix} zI - A & -B_2 \end{bmatrix} \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = \begin{bmatrix} I & 0 \end{bmatrix} \quad (20a)$$

$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix} \quad (20b)$$

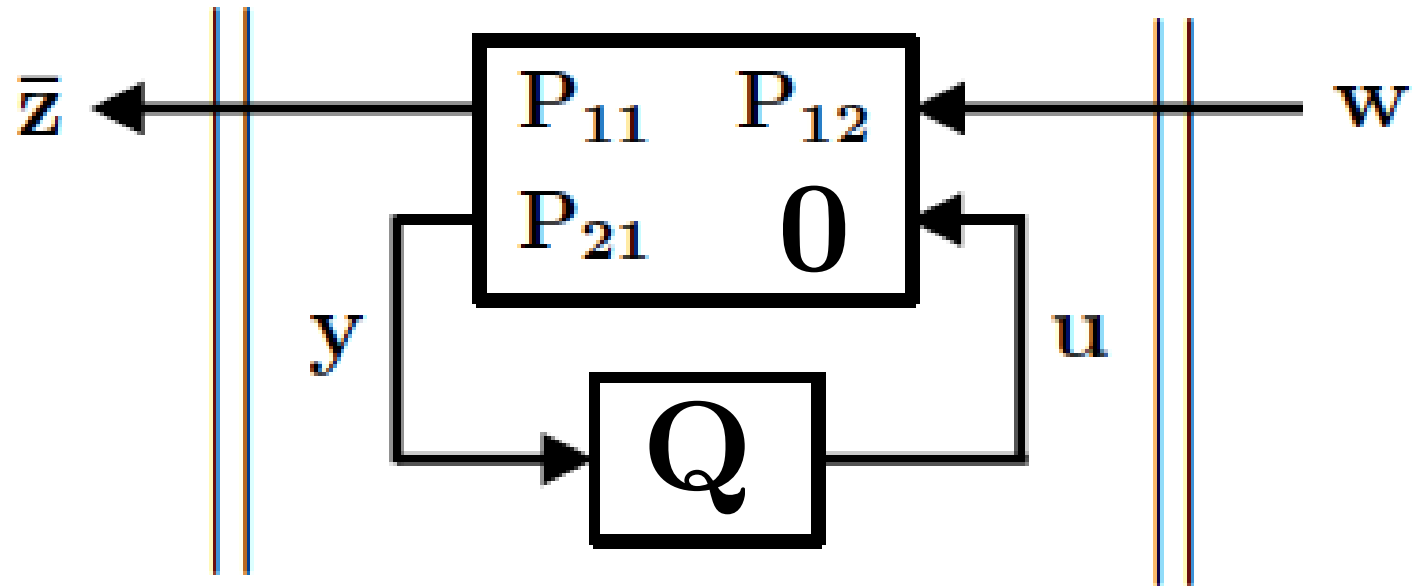
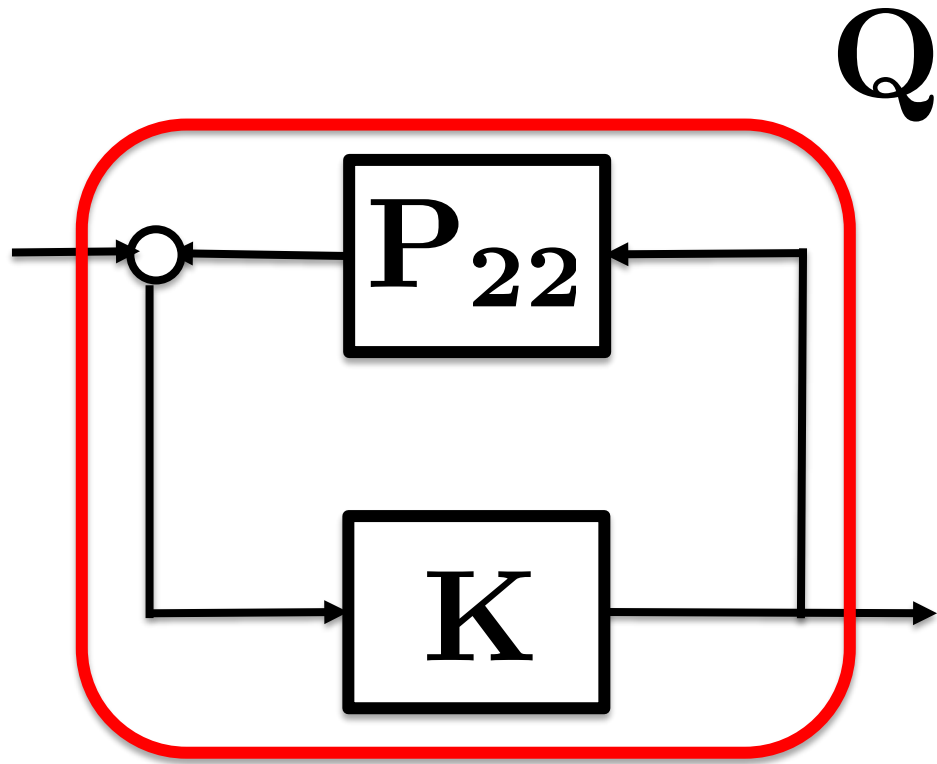
$$\mathbf{R}, \mathbf{M}, \mathbf{N} \in \frac{1}{z} \mathcal{RH}_\infty, \quad \mathbf{L} \in \mathcal{RH}_\infty \quad (20c)$$



(b) Structure 1

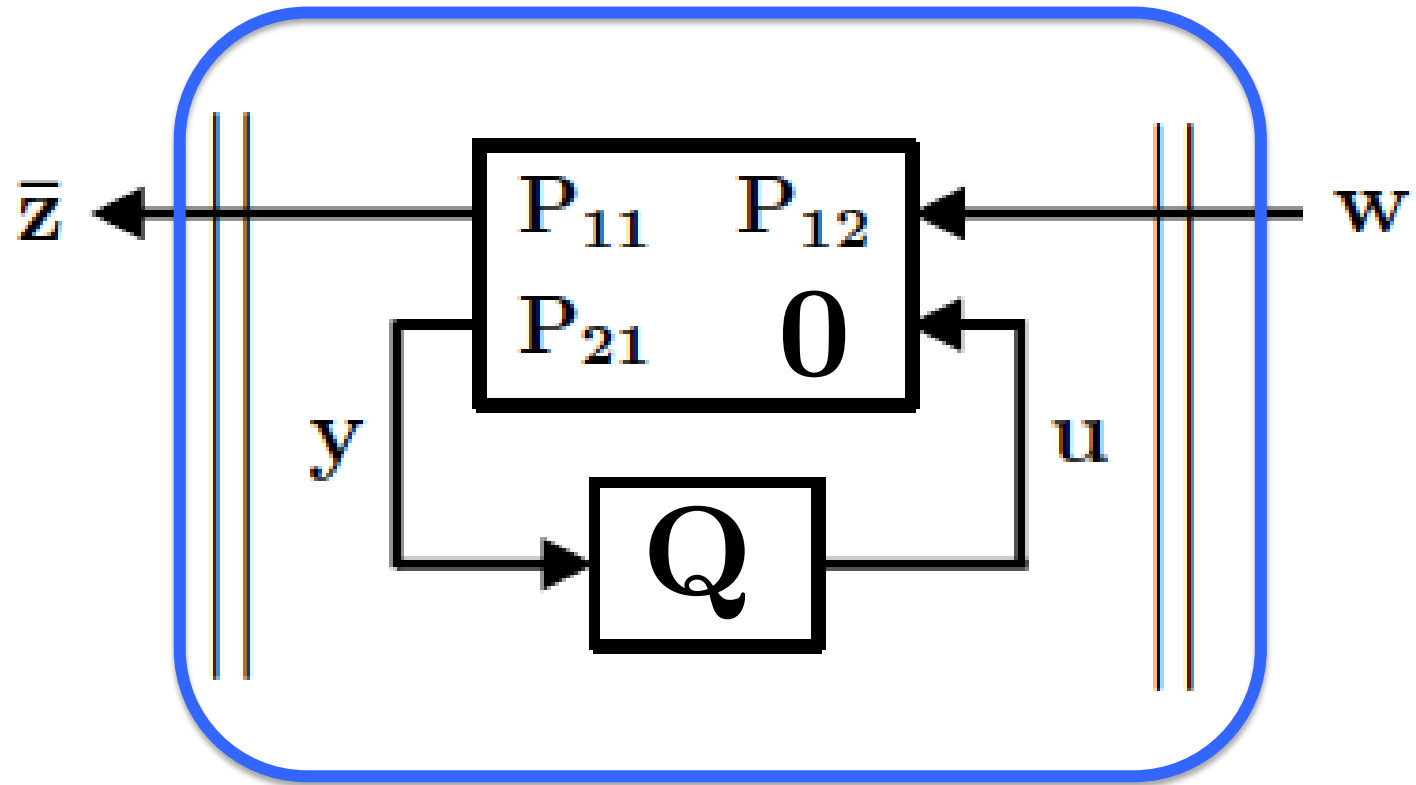
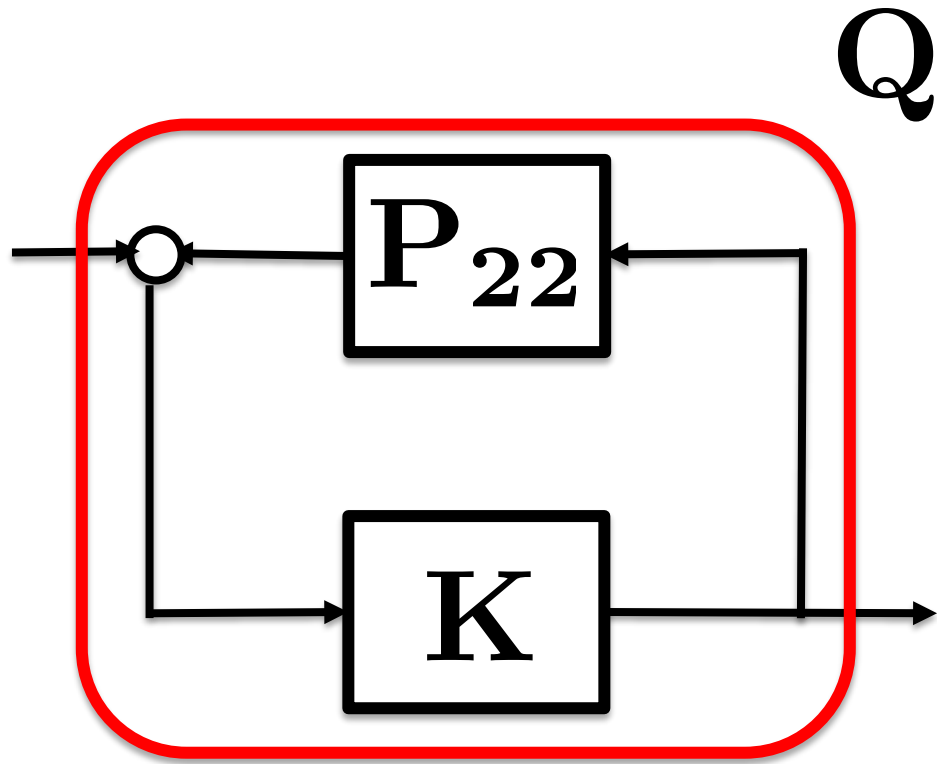


(c) Structure 2



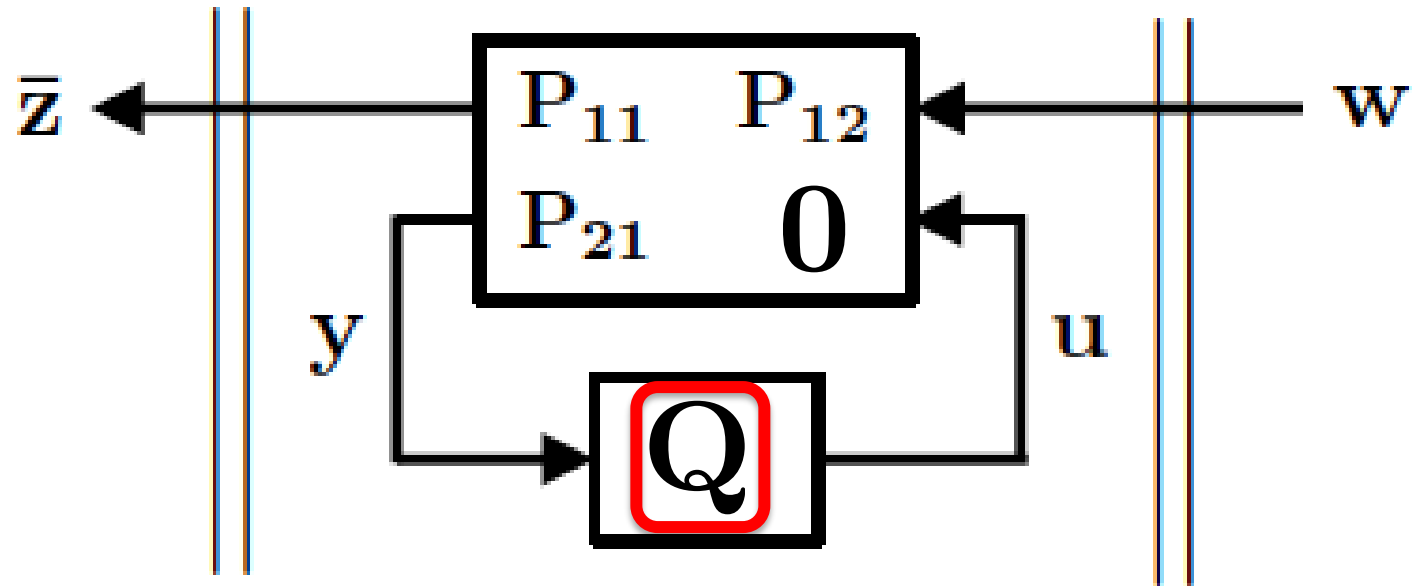
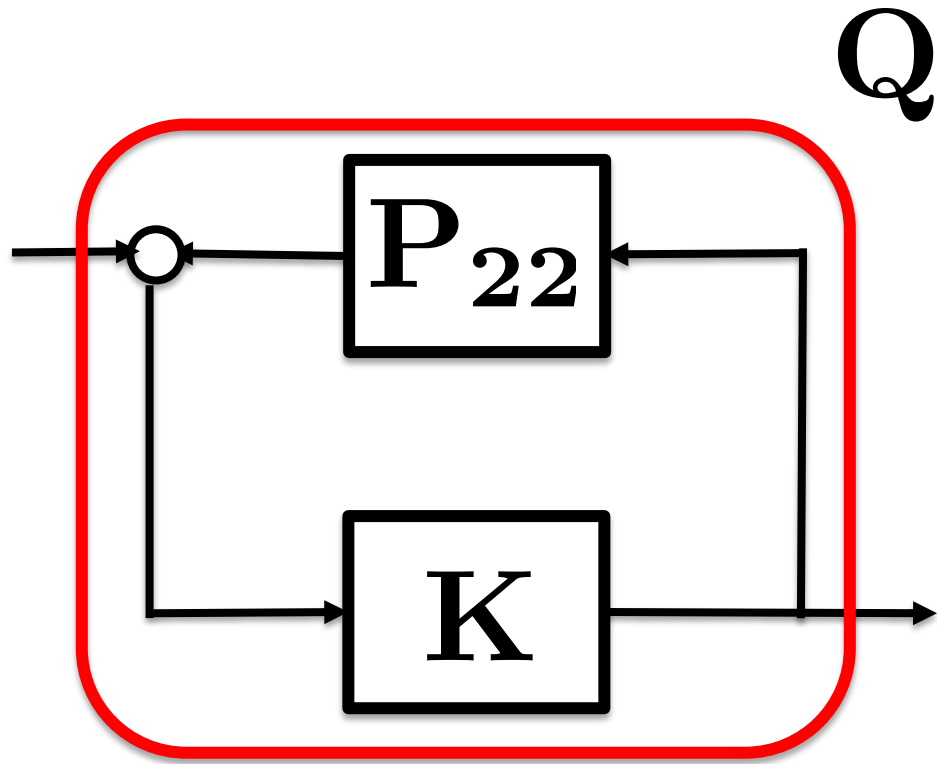
convex!

$$\begin{aligned} & \text{minimize } \| \mathbf{P}_{11} - \mathbf{P}_{12} \mathbf{Q} \mathbf{P}_{21} \| \\ & \text{subject to } \mathbf{Q} \text{ stable} \\ & \mathbf{K} \in \mathcal{C} \end{aligned}$$



minimize $\| \mathbf{P}_{11} - \mathbf{P}_{12} \mathbf{Q} \mathbf{P}_{21} \|$
 subject to \mathbf{Q} stable
 $\mathbf{K} \in \mathcal{C}$

**What we
 care about**

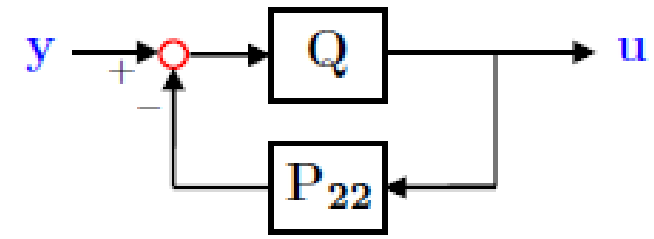


minimize $\| \mathbf{P}_{11} - \mathbf{P}_{12} \mathbf{Q} \mathbf{P}_{21} \|$
 subject to \mathbf{Q} stable
 $\mathbf{K} \in \mathcal{C}$

model matching

Special case: stable plant

$$\mathbf{Q} = \mathbf{L}$$

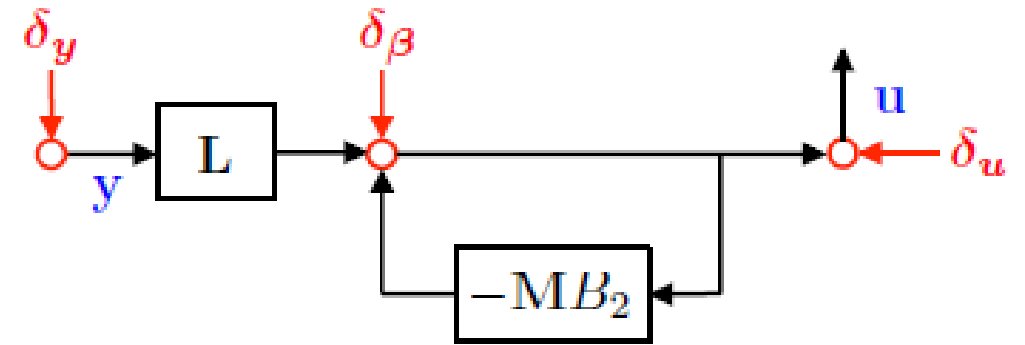


(a) Internal Model Control

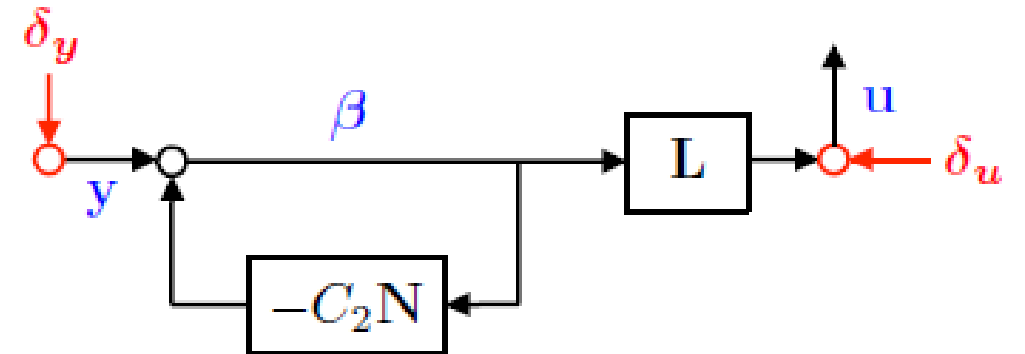
$$\begin{bmatrix} zI - A & -B_2 \end{bmatrix} \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = \begin{bmatrix} I & 0 \end{bmatrix} \quad (20a)$$

$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix} \quad (20b)$$

$$\mathbf{R}, \mathbf{M}, \mathbf{N} \in \frac{1}{z} \mathcal{RH}_\infty, \quad \mathbf{L} \in \mathcal{RH}_\infty \quad (20c)$$



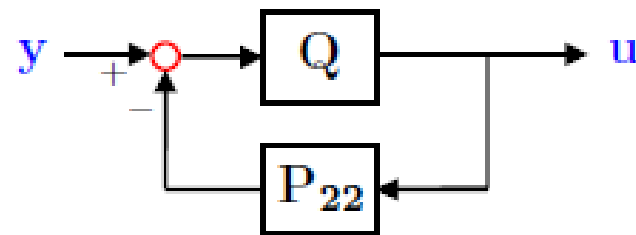
(b) Structure 1



(c) Structure 2

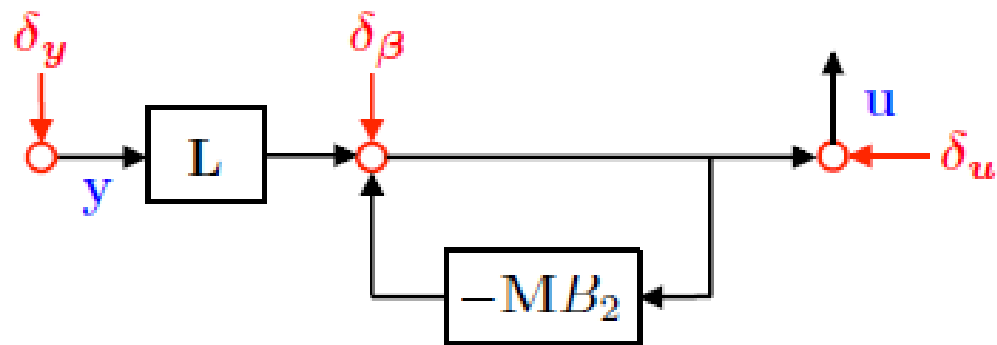
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$

$$\mathbf{Q} = \mathbf{L}$$



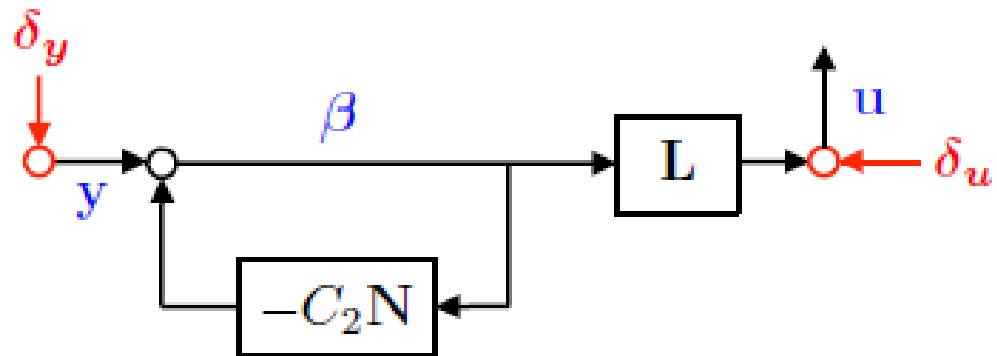
(a) Internal Model Control

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 & (zI - A)^{-1}B_2 \\ \mathbf{M} & \mathbf{L} & I + \mathbf{M}B_2 & I \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \\ \delta_\beta \end{bmatrix}$$



(b) Structure 1

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \\ \beta \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 \\ \mathbf{M} & \mathbf{L} & I + \mathbf{M}B_2 \\ C_2(zI - A)^{-1} & I & C_2(zI - A)^{-1}B_2 \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \end{bmatrix}$$



(c) Structure 2

$$\begin{bmatrix} zI - A & -B_2 \end{bmatrix} \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = \begin{bmatrix} I & 0 \end{bmatrix} \quad (20a)$$

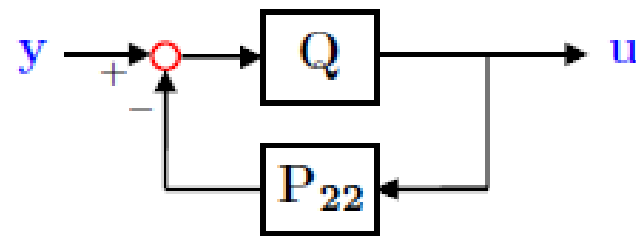
$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix} \quad (20b)$$

$$\mathbf{R}, \mathbf{M}, \mathbf{N} \in \frac{1}{z} \mathcal{RH}_\infty, \quad \mathbf{L} \in \mathcal{RH}_\infty \quad (20c)$$

**Affine
constraint**

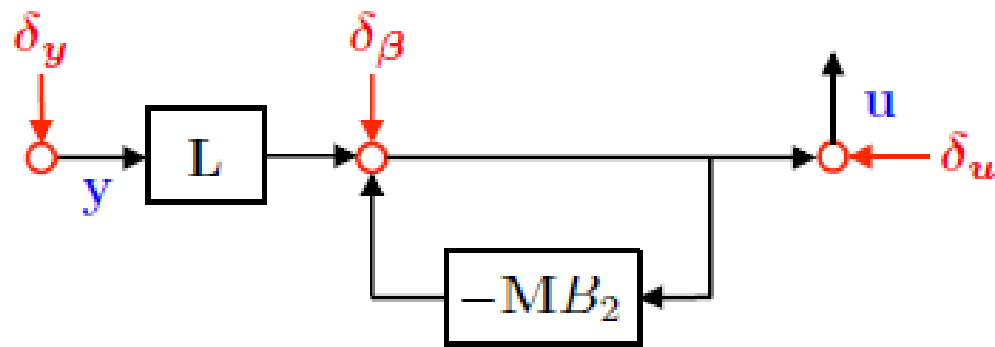
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$

$$\mathbf{Q} = \mathbf{L}$$



(a) Internal Model Control

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 & (zI - A)^{-1}B_2 \\ \mathbf{M} & \mathbf{L} & I + \mathbf{M}B_2 & I \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \\ \delta_\beta \end{bmatrix}$$



(b) Structure 1

$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix}$$

$$M = LC(zI - A)^{-1}$$

$$\Rightarrow MB = LC(zI - A)^{-1}B = LP_{22}$$

$$\begin{bmatrix} zI - A & -B_2 \end{bmatrix} \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = \begin{bmatrix} I & 0 \end{bmatrix} \quad (20a)$$

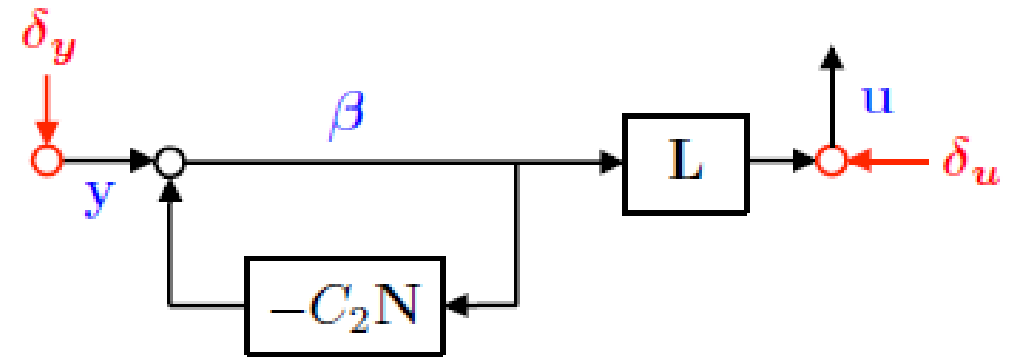
$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix} \quad (20b)$$

$$\mathbf{R}, \mathbf{M}, \mathbf{N} \in \frac{1}{z} \mathcal{RH}_\infty, \quad \mathbf{L} \in \mathcal{RH}_\infty \quad (20c)$$

$$N = (zI - A)^{-1} BL \quad \Rightarrow \quad CN = C(zI - A)^{-1} BL = P_{22}L$$

$$\boxed{[zI - A \quad -B_2] \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = [I \quad 0]}$$

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \\ \beta \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 \\ \mathbf{M} & \mathbf{L} & I + \mathbf{M}B_2 \\ C_2(zI - A)^{-1} & I & C_2(zI - A)^{-1}B_2 \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \end{bmatrix}$$

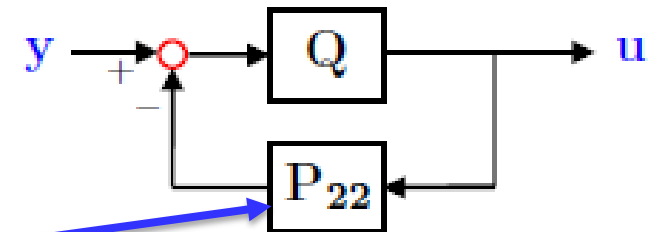


(c) Structure 2

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$

$$\mathbf{Q} = \mathbf{L}$$

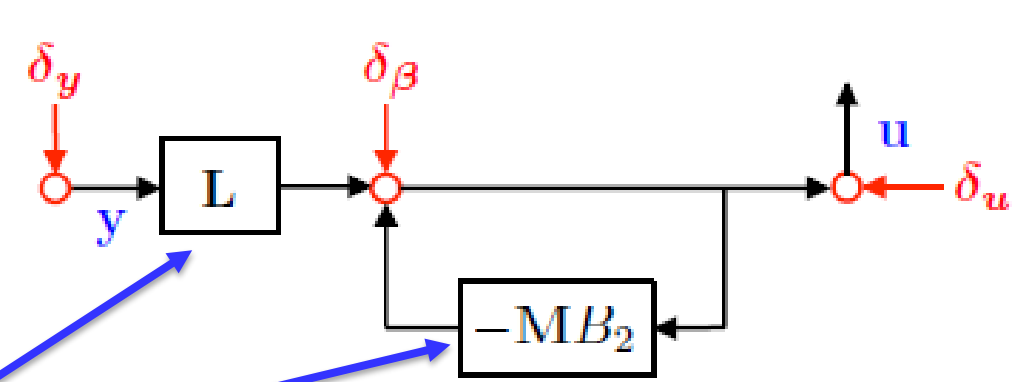
May be dense



(a) Internal Model Control

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 \\ \mathbf{M} & \mathbf{L} & \mathbf{I} + \mathbf{M}B_2 \end{bmatrix} \begin{bmatrix} (z\mathbf{I} - \mathbf{A})^{-1}\mathbf{B}_2 \\ \mathbf{I} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \\ \delta_\beta \end{bmatrix}$$

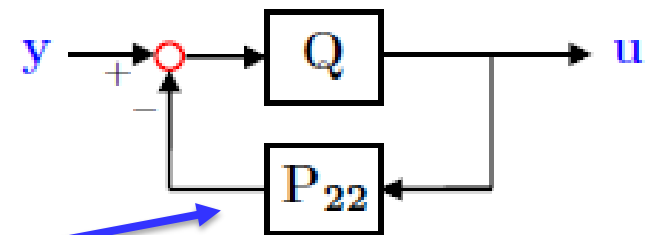
Can be made sparse



(b) Structure 1

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix} \quad \mathbf{Q} = \mathbf{L}$$

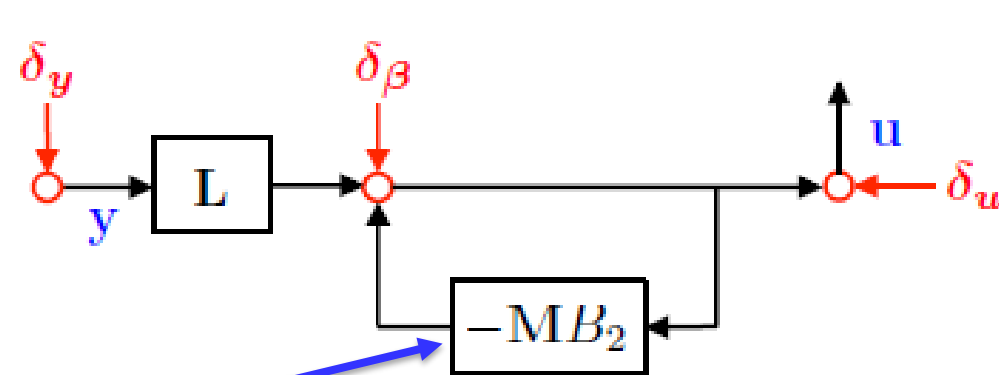
Cancels feedback from P



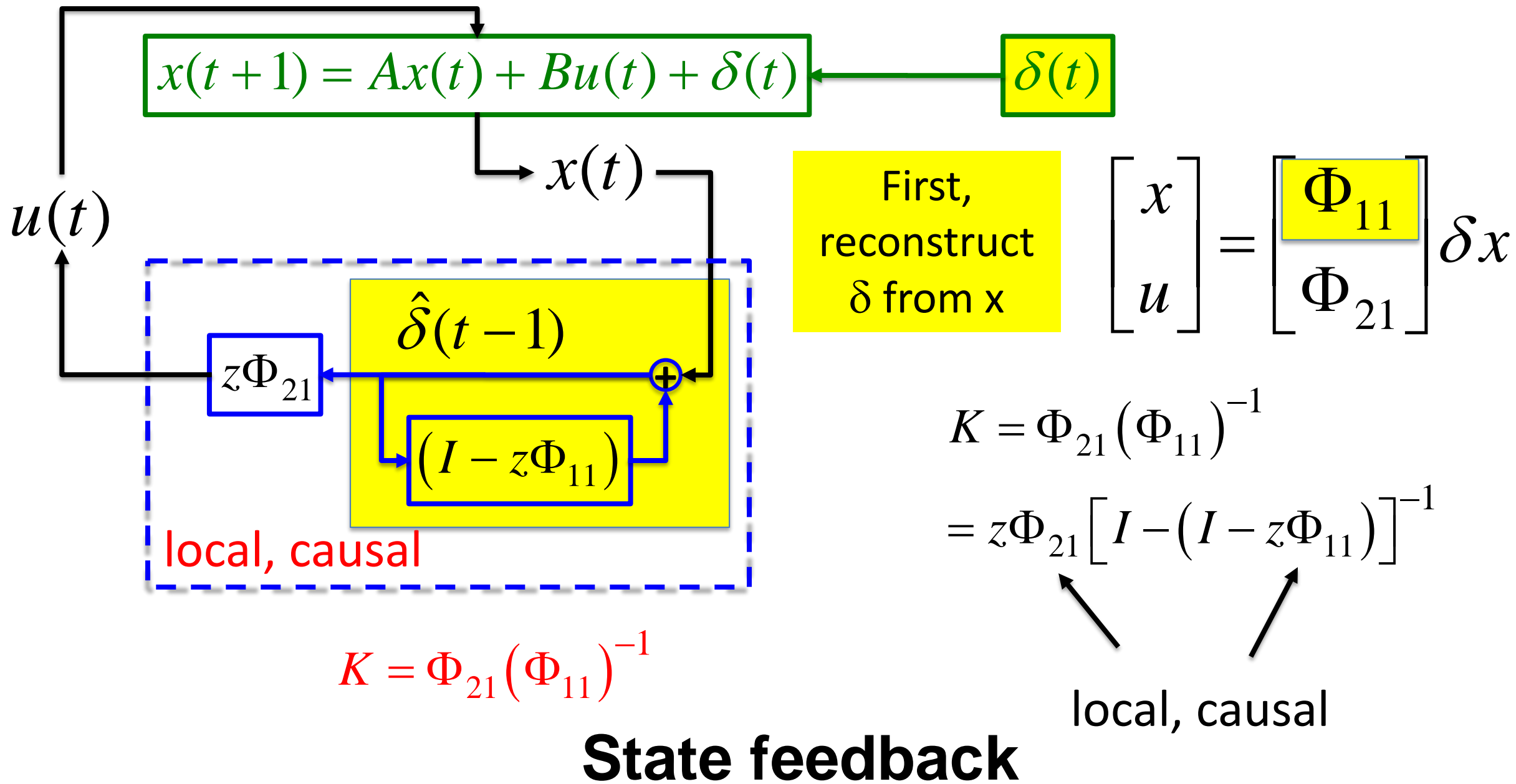
(a) Internal Model Control

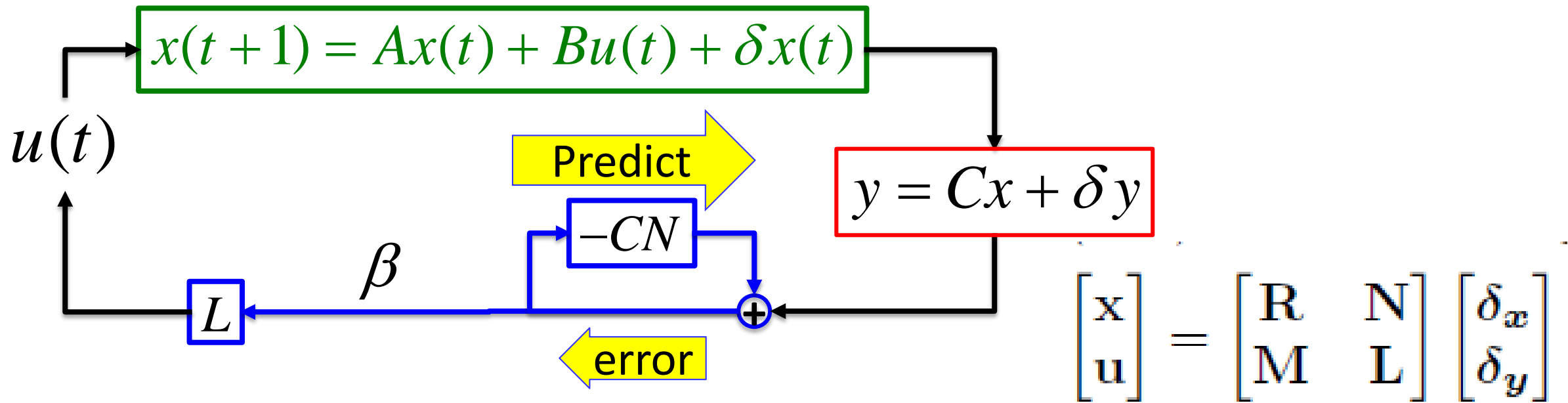
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 & (zI - A)^{-1}B_2 \\ \mathbf{M} & \mathbf{L} & I + \mathbf{M}B_2 & I \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \\ \delta_\beta \end{bmatrix}$$

Cancels feedback from P



(b) Structure 1

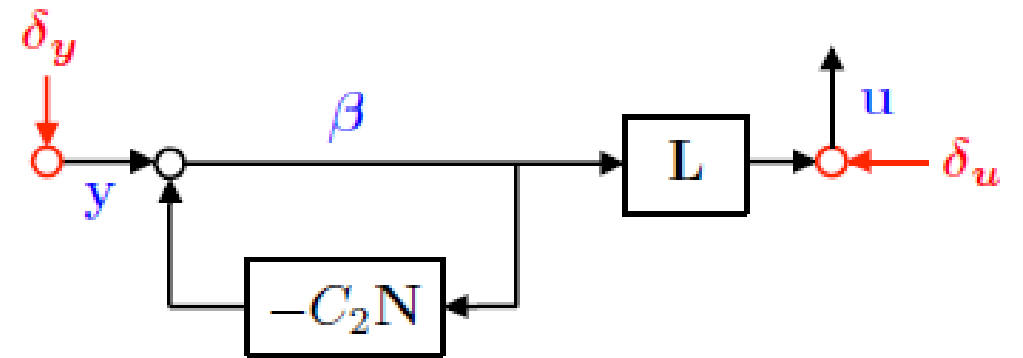




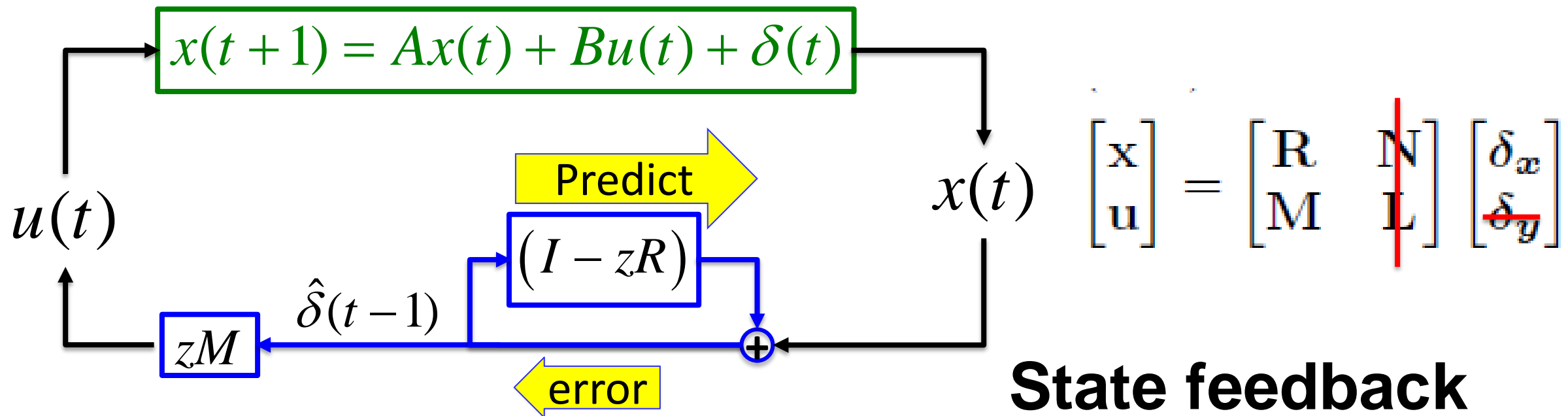
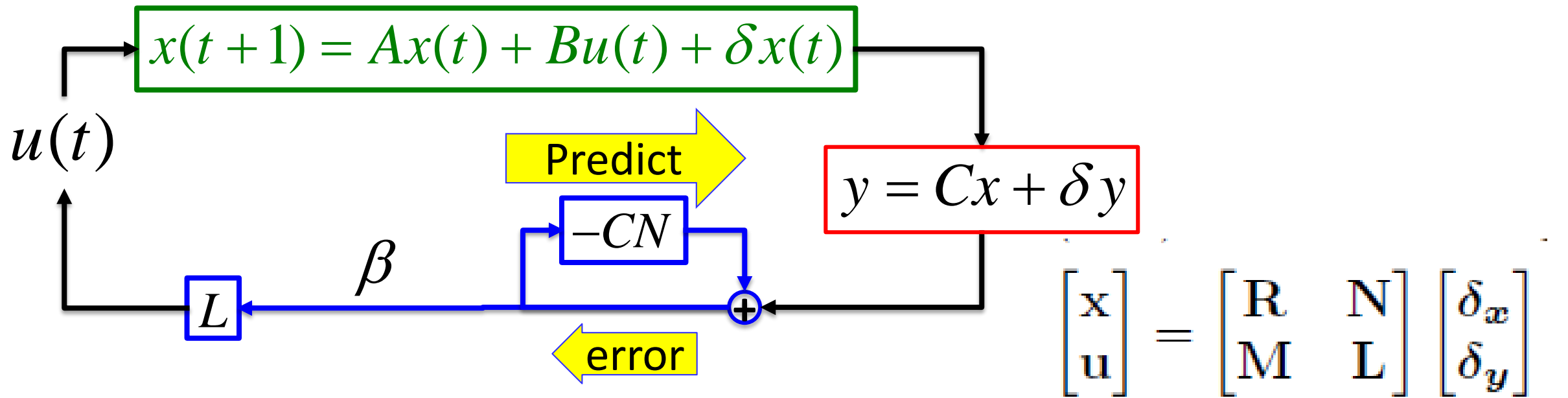
$$N = (zI - A)^{-1} BL \quad \Rightarrow \quad CN = C(zI - A)^{-1} BL = P_{22}L$$

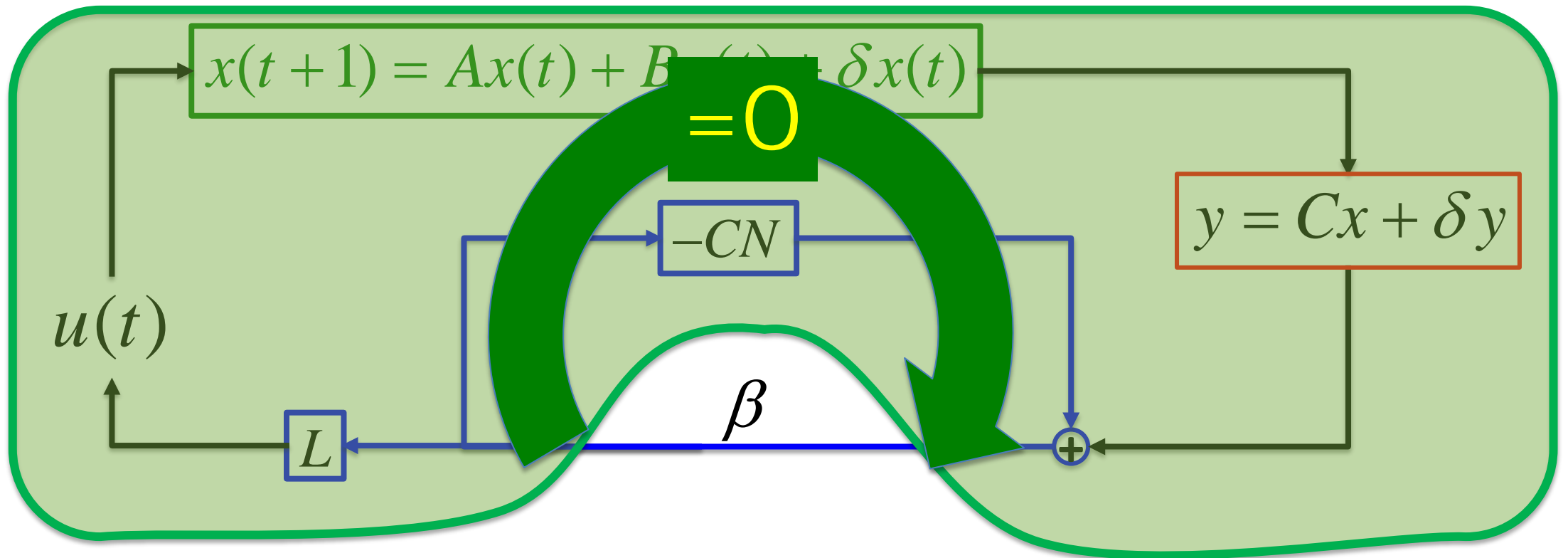
$$[zI - A \quad -B_2] \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} = [I \quad 0]$$

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$



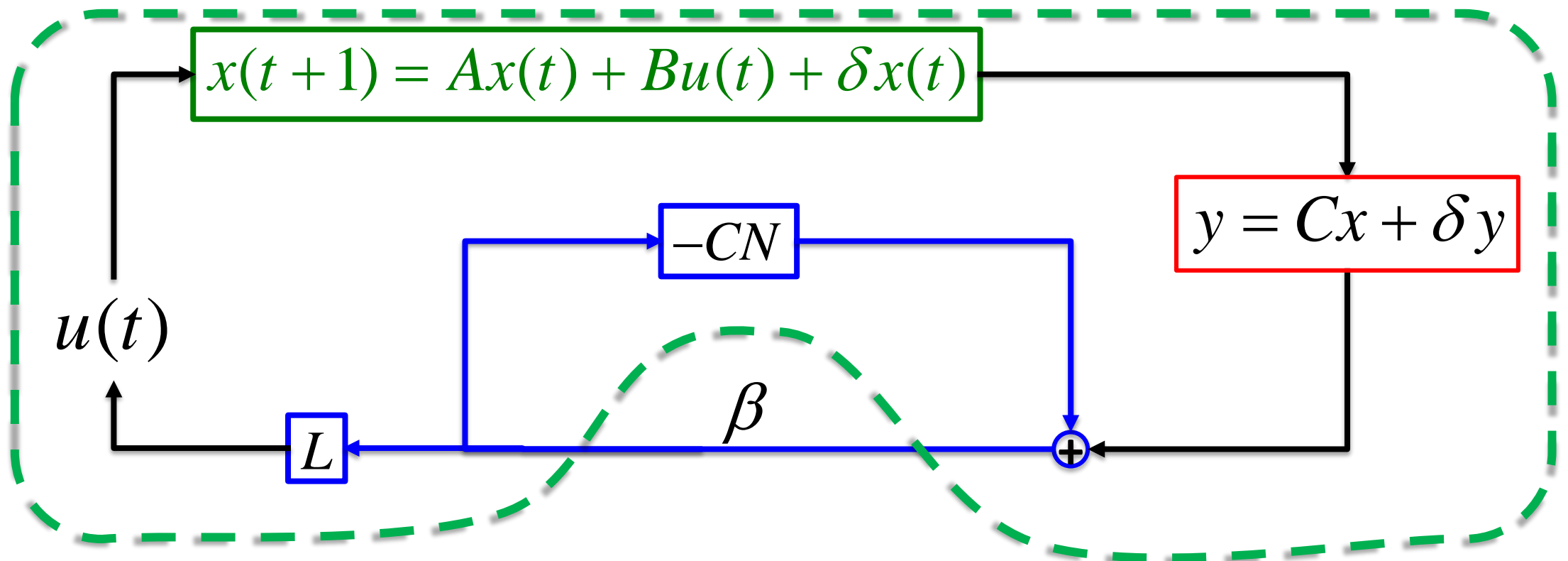
(c) Structure 2





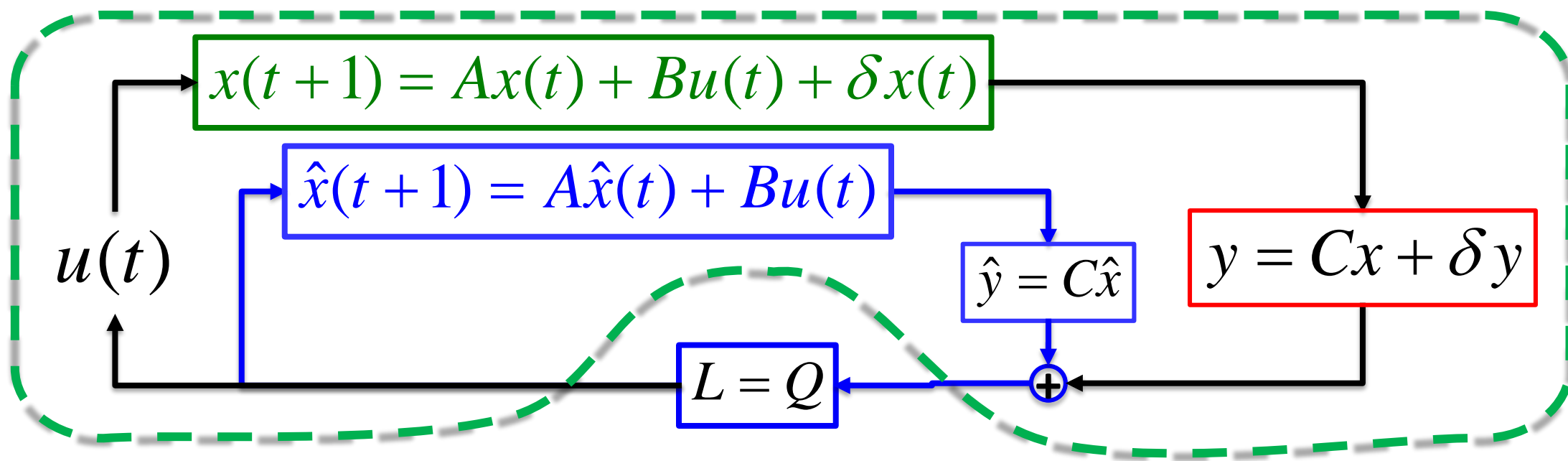
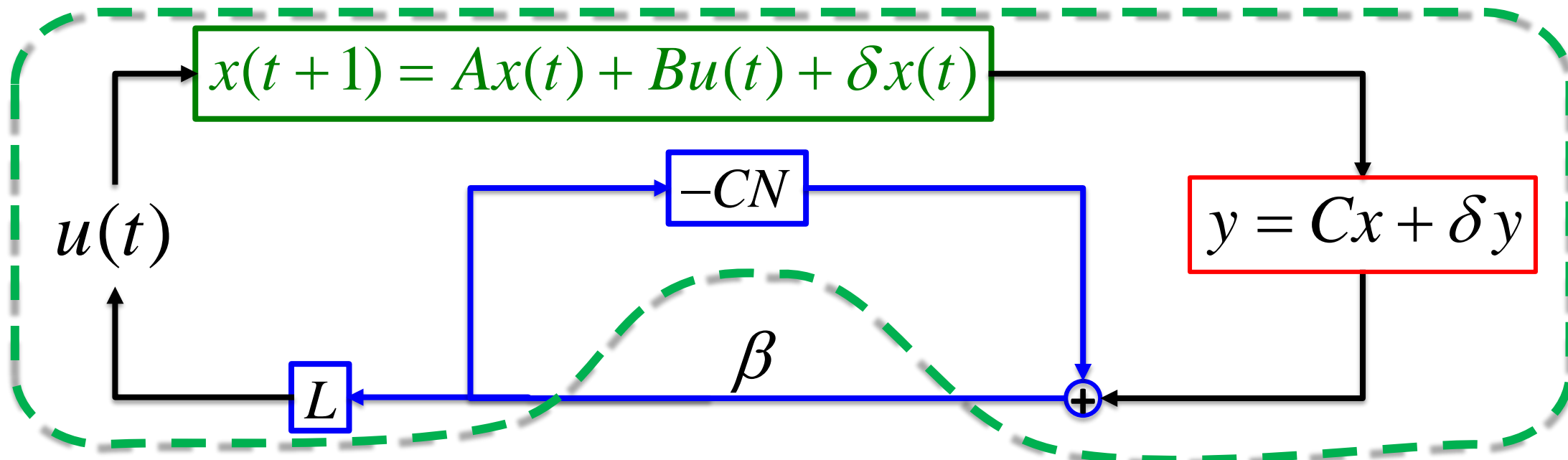
$$-CN + C(zI - A)^{-1}BL = 0$$

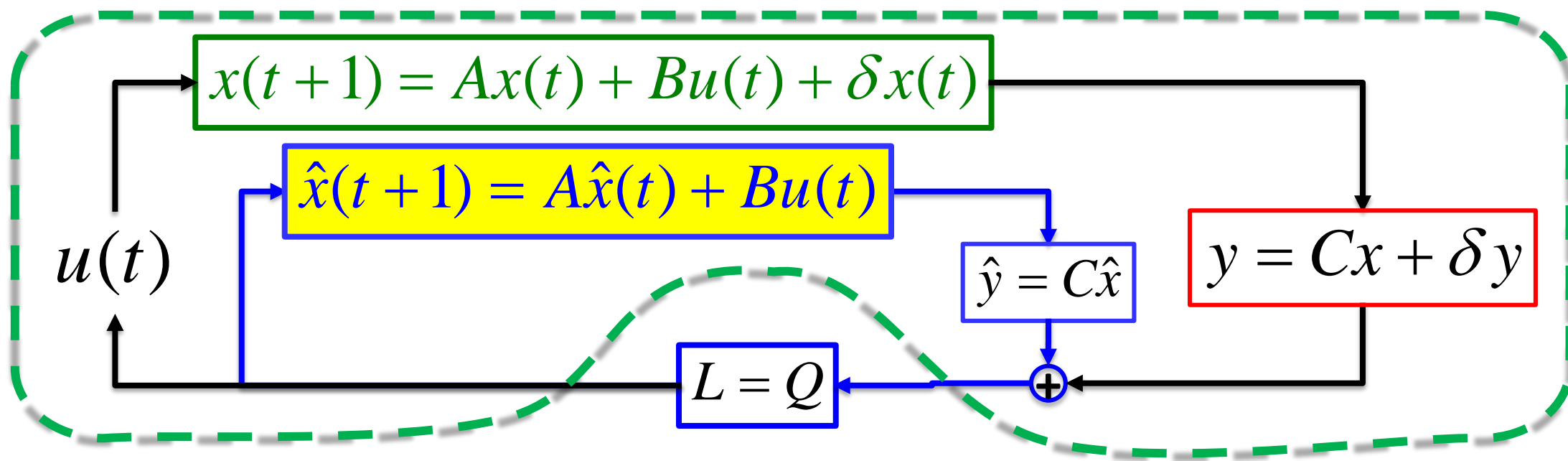
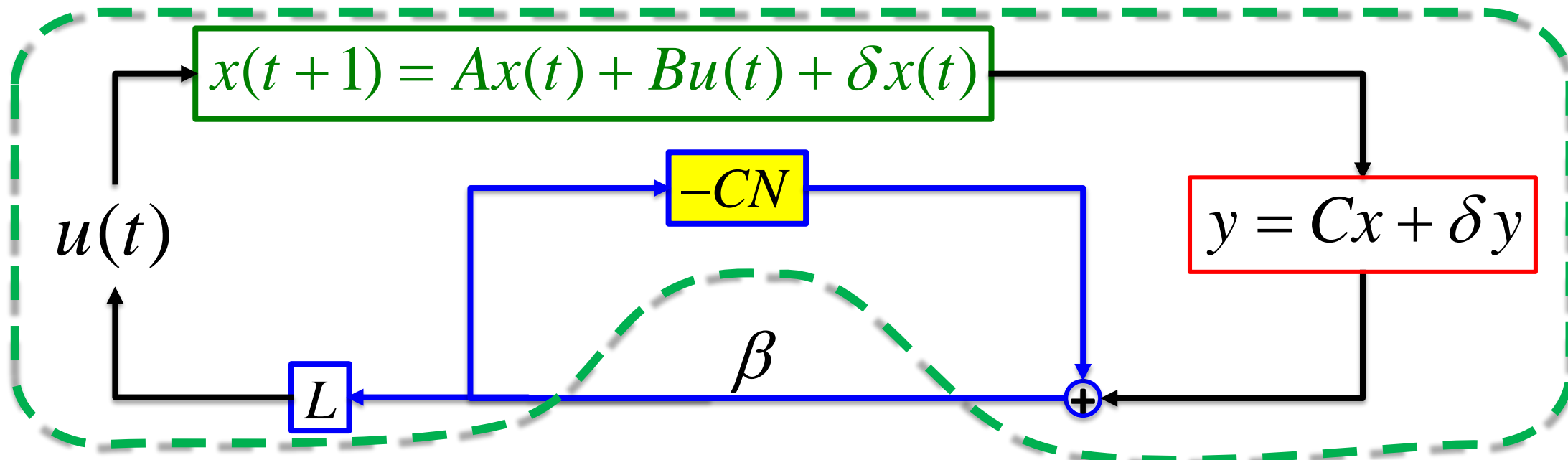
$$N = (zI - A)^{-1}BL \quad \Rightarrow \quad CN = C(zI - A)^{-1}BL = P_{22}L$$

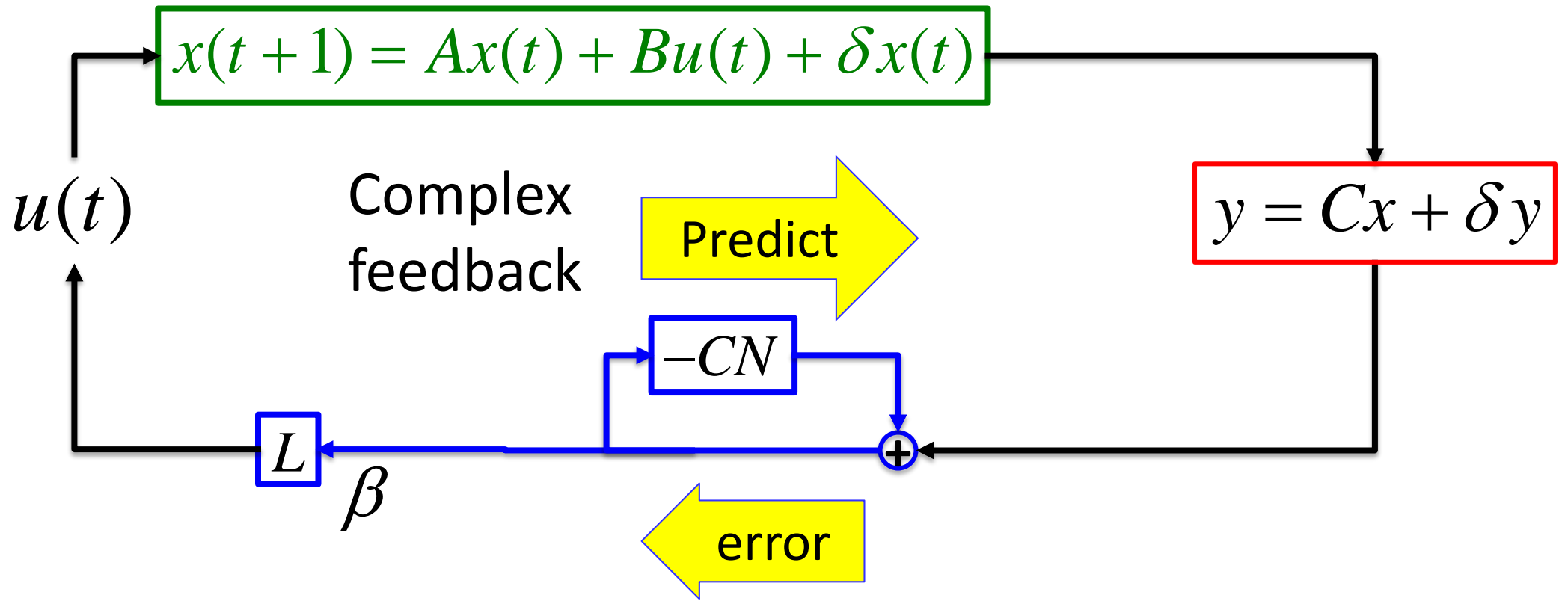


$$-CN + C(zI - A)^{-1}BL = 0$$

$$N = (zI - A)^{-1}BL \quad \Rightarrow \quad CN = C(zI - A)^{-1}BL = P_{22}L$$

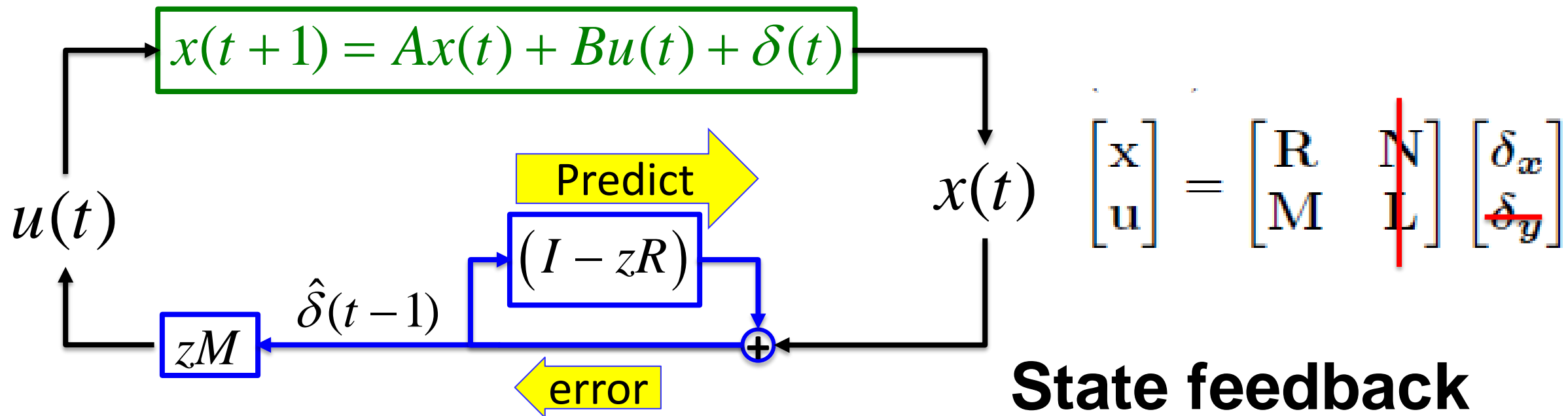
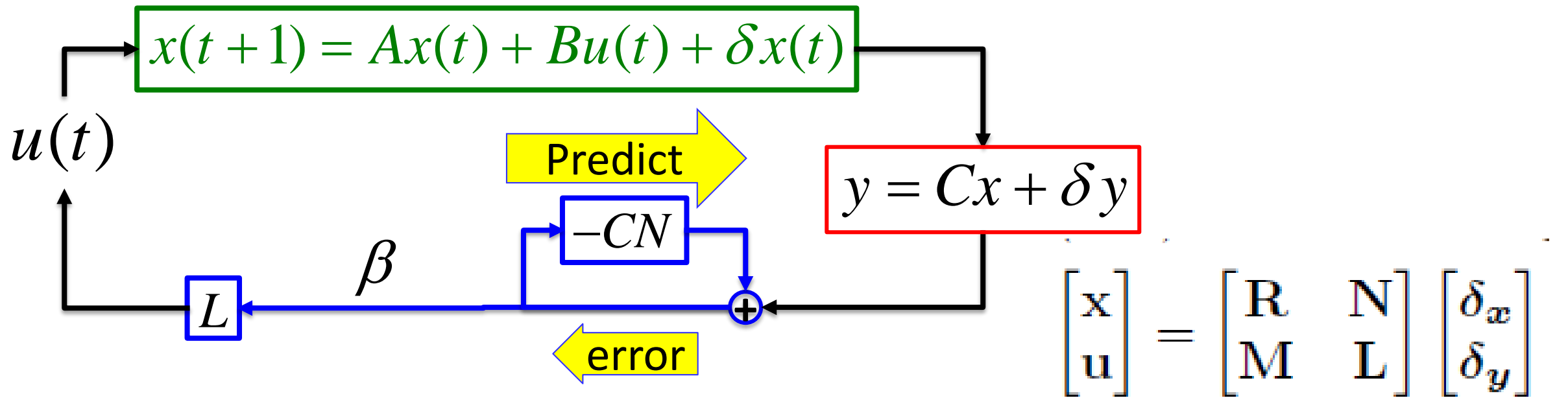






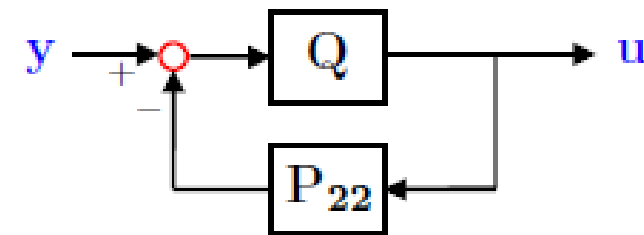
Simple feedforward (fast?)

$$N = (zI - A)^{-1} BL \quad \Rightarrow \quad CN = C(zI - A)^{-1} BL = P_{22}L$$

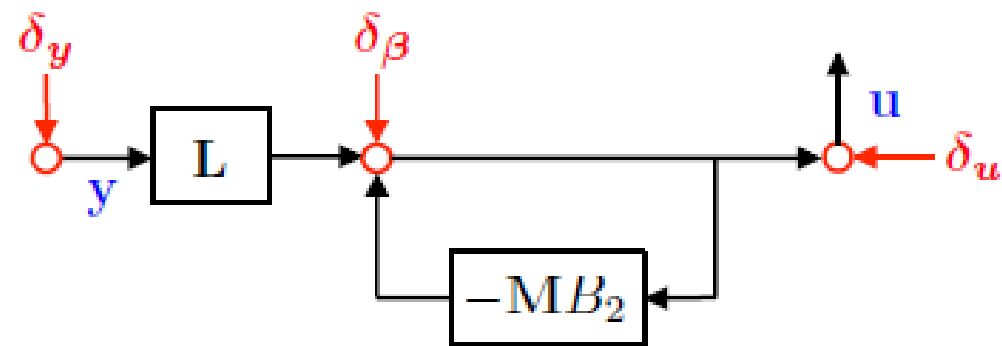


$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$

$$\mathbf{Q} = \mathbf{L}$$

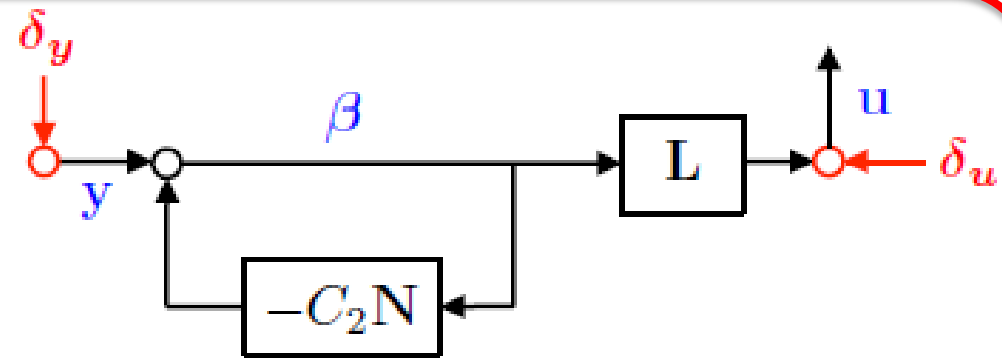


(a) Internal Model Control

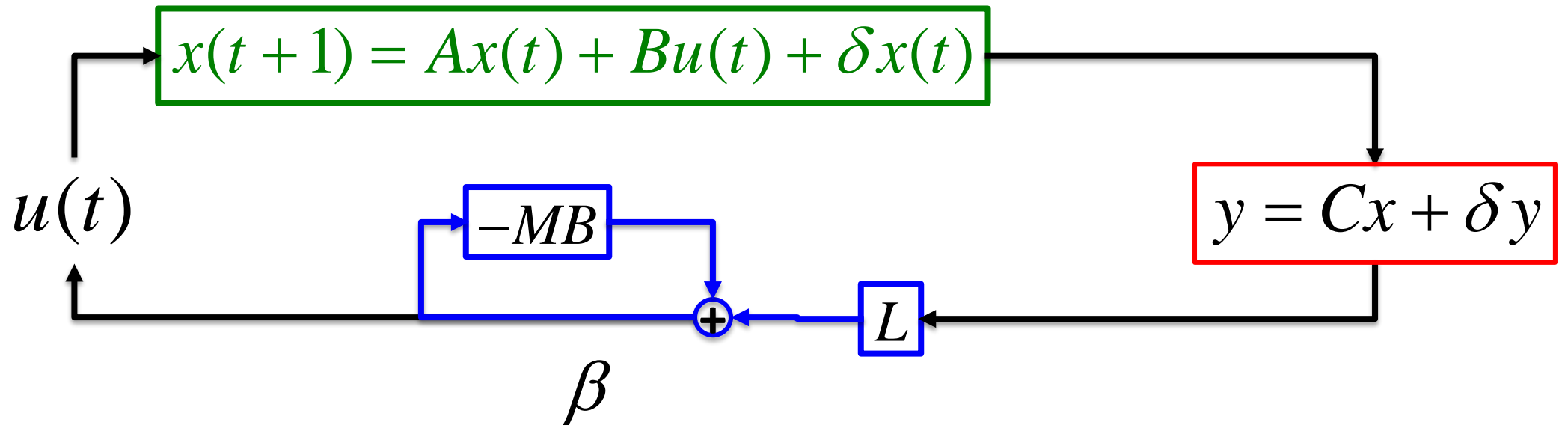


(b) Structure 1

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \\ \beta \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} & \mathbf{R}B_2 \\ \mathbf{M} & \mathbf{L} & I + \mathbf{M}B_2 \\ C_2(zI - A)^{-1} & I & C_2(zI - A)^{-1}B_2 \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \\ \delta_u \end{bmatrix}$$



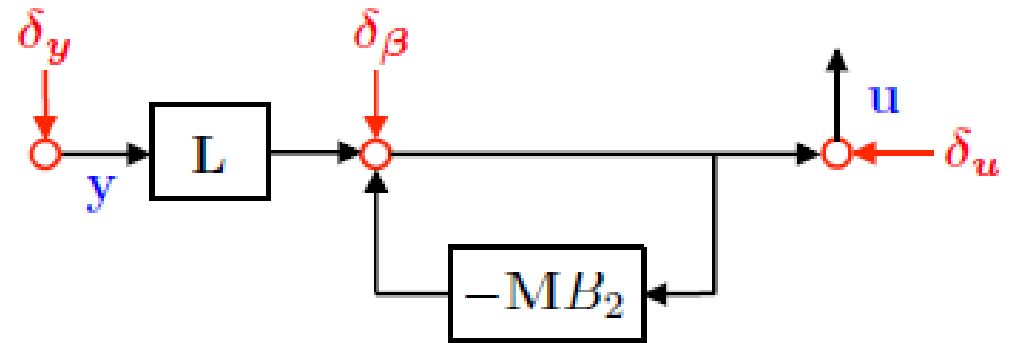
(c) Structure 2

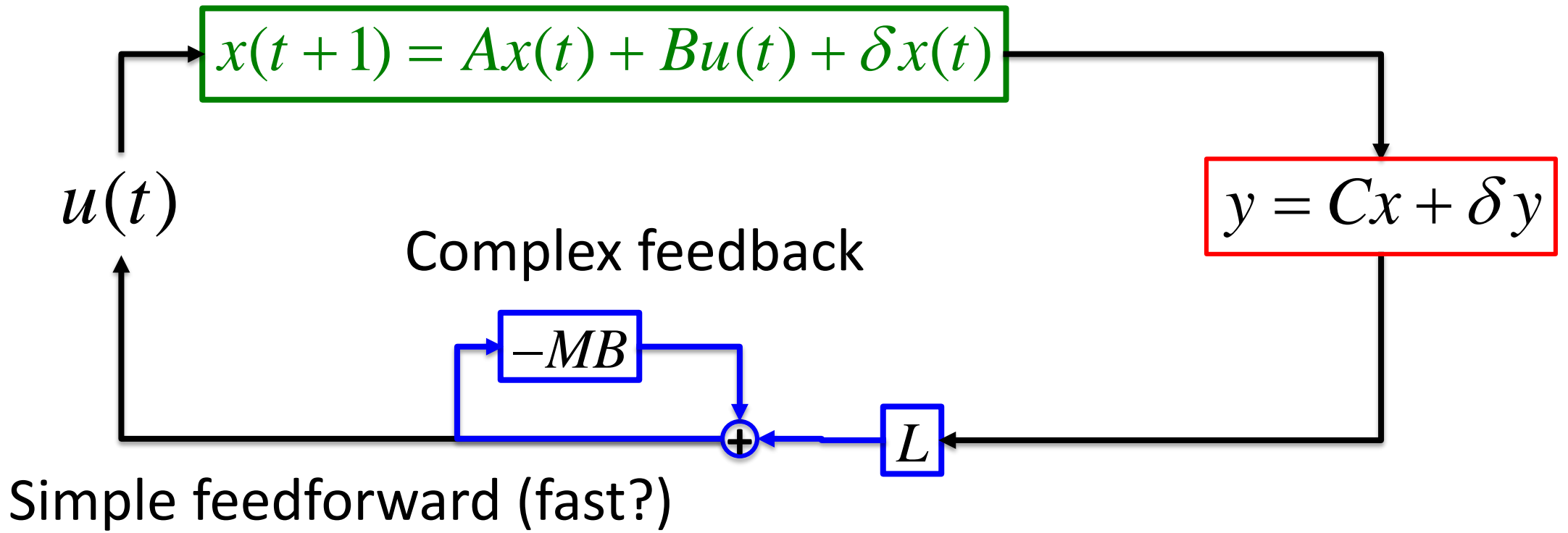


$$M = LC(zI - A)^{-1} \quad \Rightarrow \quad MB = LC(zI - A)^{-1} B = LP_{22}$$

$$\begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} zI - A \\ -C_2 \end{bmatrix} = \begin{bmatrix} I \\ 0 \end{bmatrix}$$

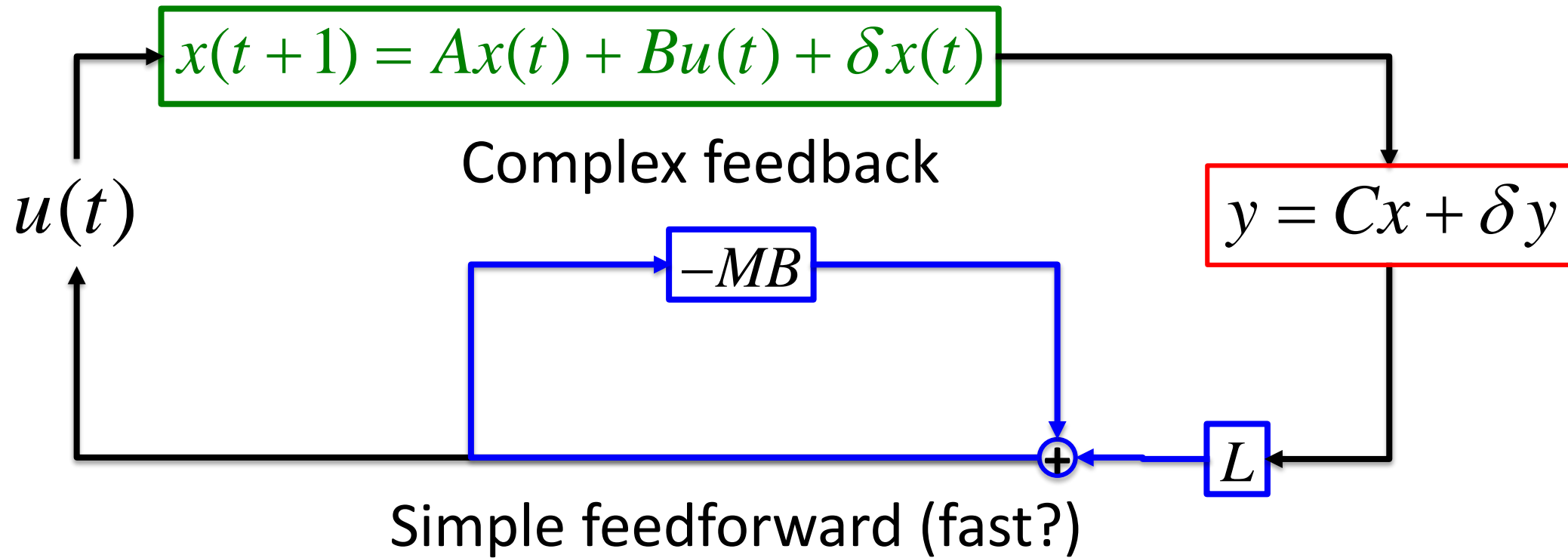
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_{\mathbf{x}} \\ \delta_{\mathbf{y}} \end{bmatrix}$$





$$M = LC(zI - A)^{-1} \quad \Rightarrow \quad MB = LC(zI - A)^{-1} B = LP_{22}$$

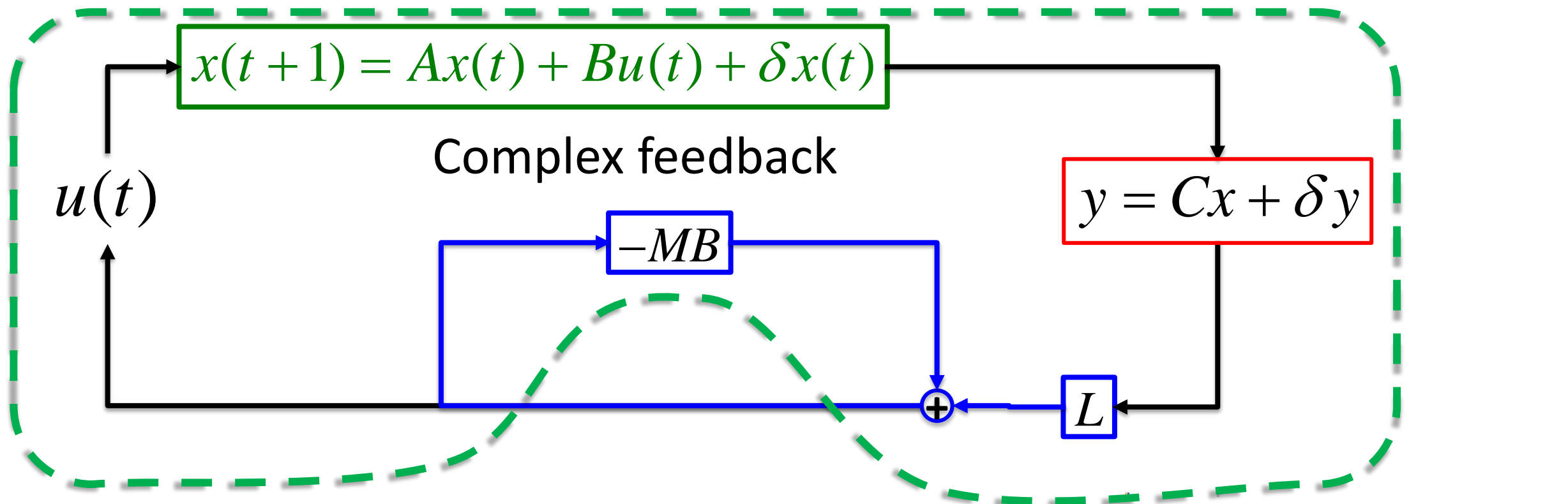
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_{\mathbf{x}} \\ \delta_{\mathbf{y}} \end{bmatrix}$$



$$-MB + LC(zI - A)^{-1}B = 0$$

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$

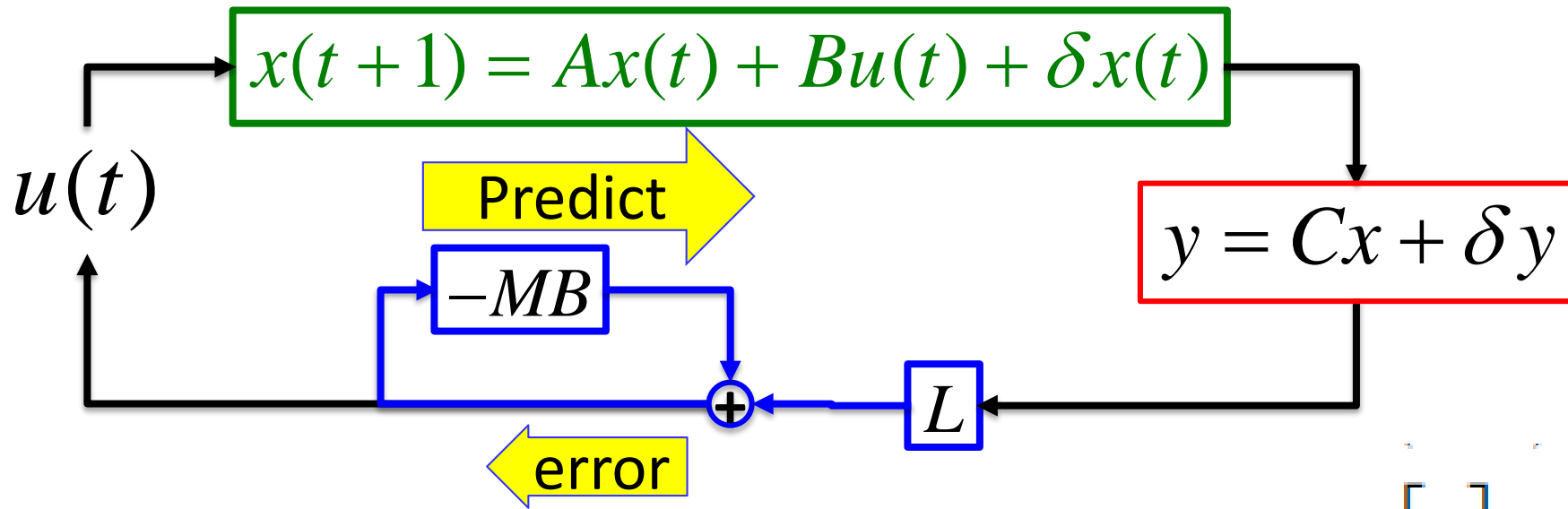
$$M = LC(zI - A)^{-1} \Rightarrow MB = LC(zI - A)^{-1}B = LP_{22}$$



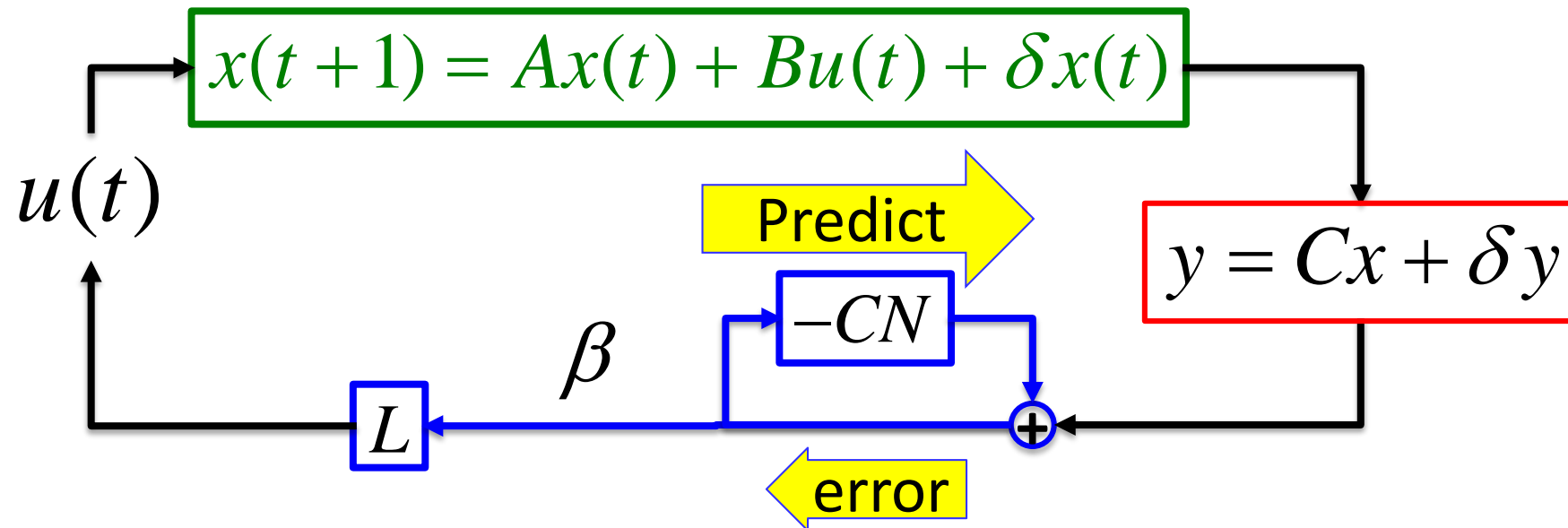
$$-MB + LC(zI - A)^{-1}B = 0$$

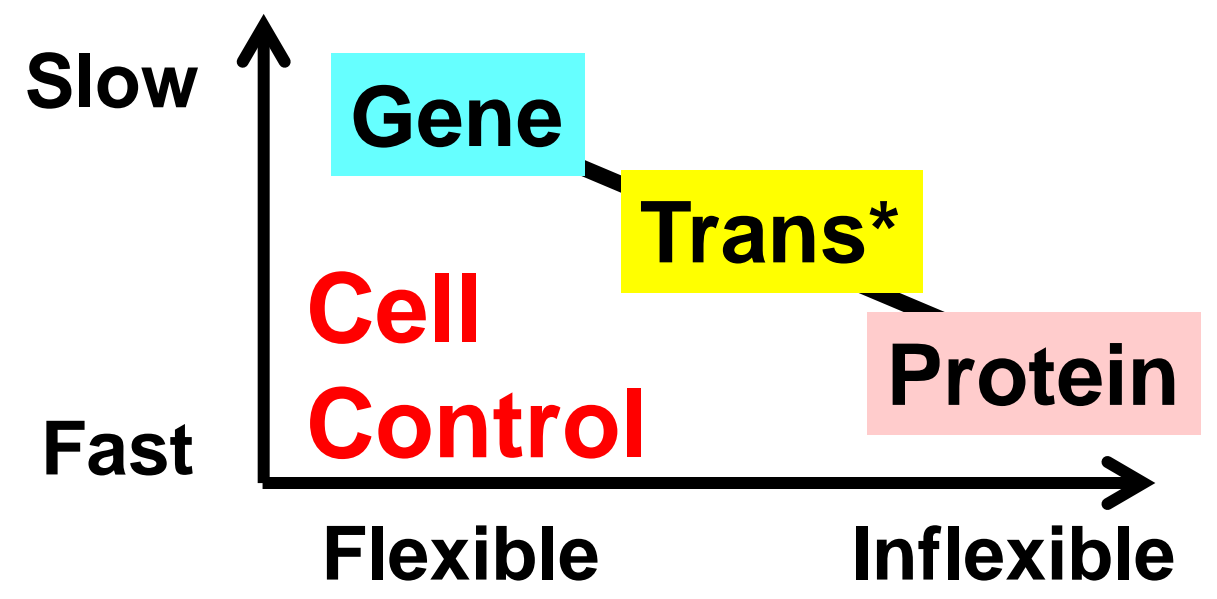
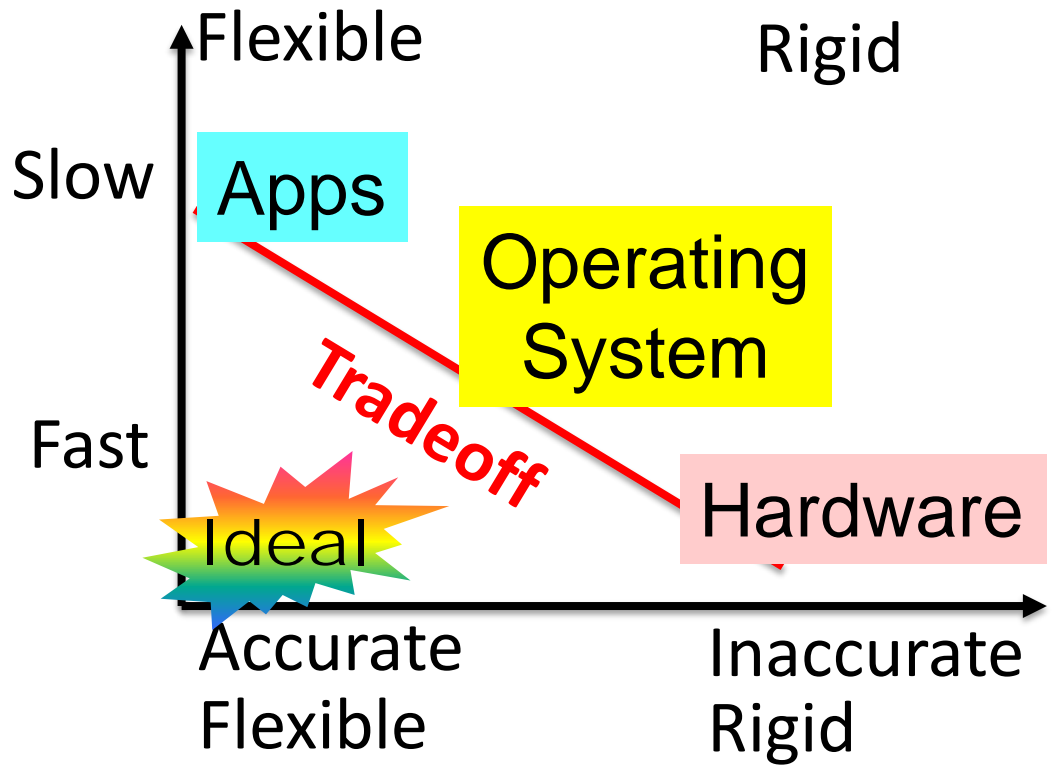
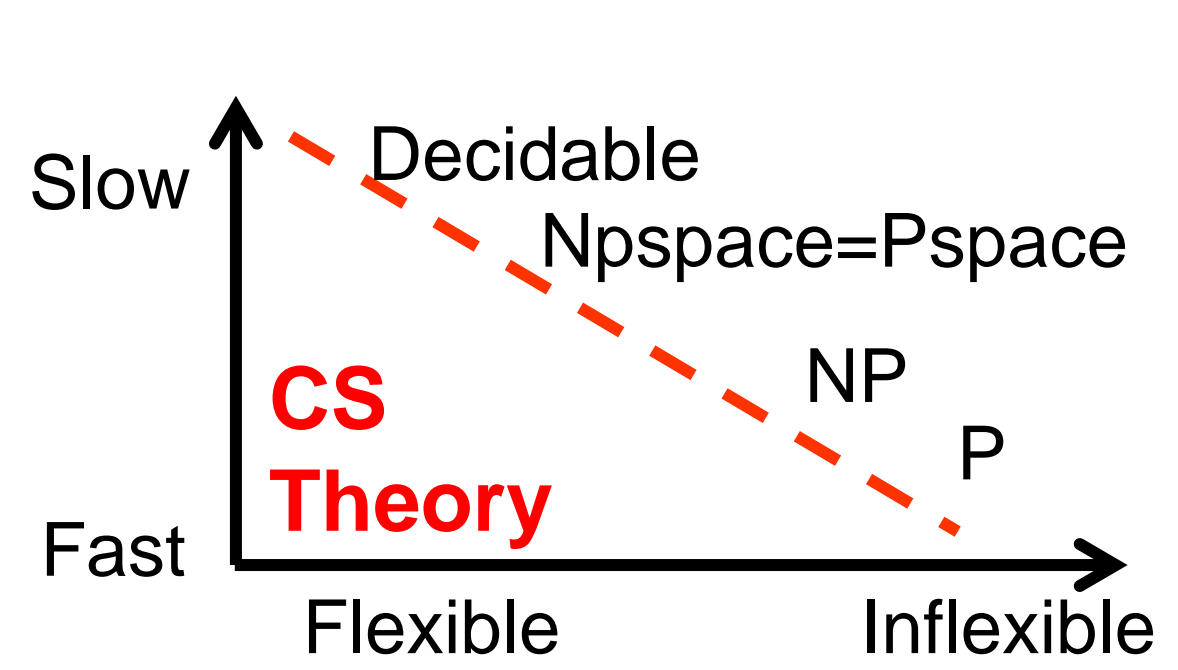
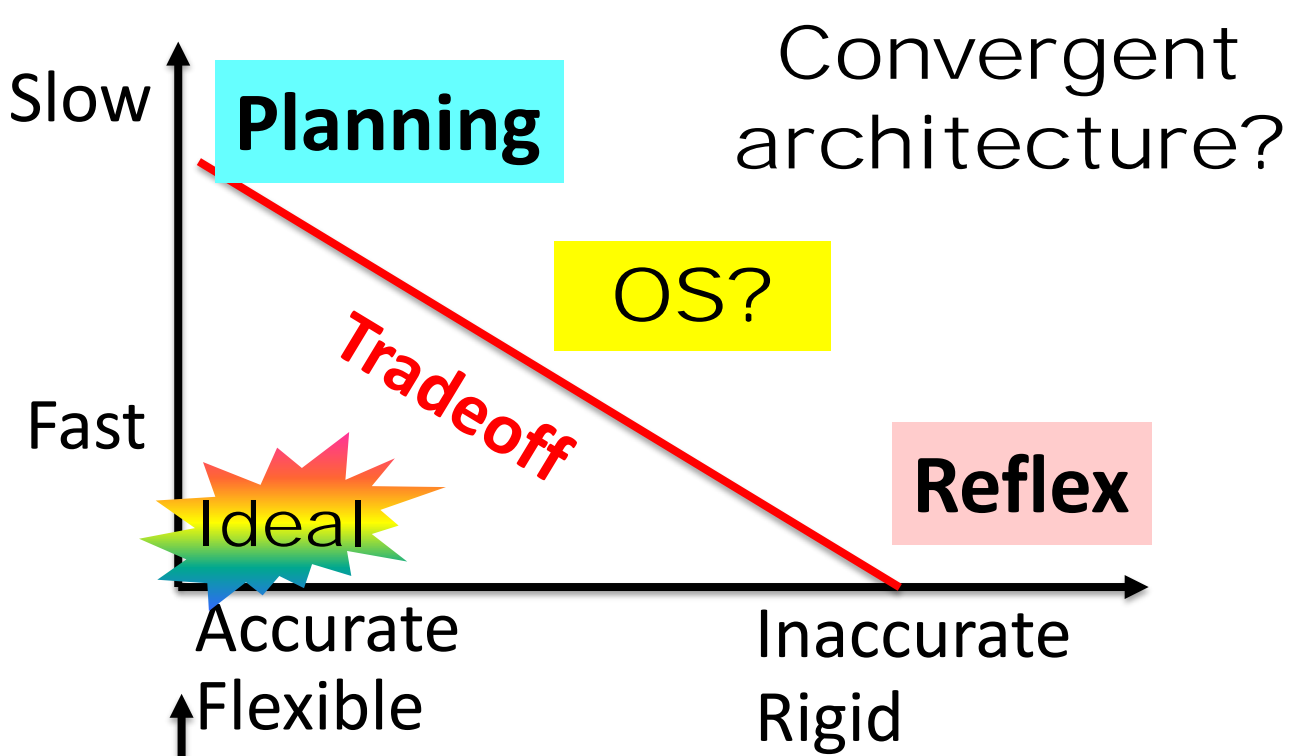
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta_x \\ \delta_y \end{bmatrix}$$

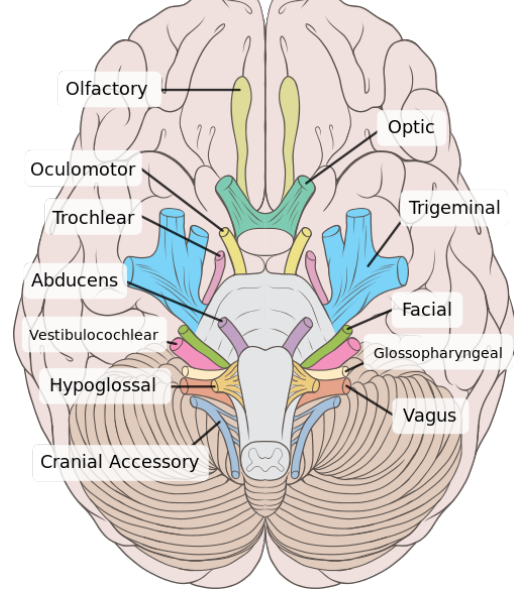
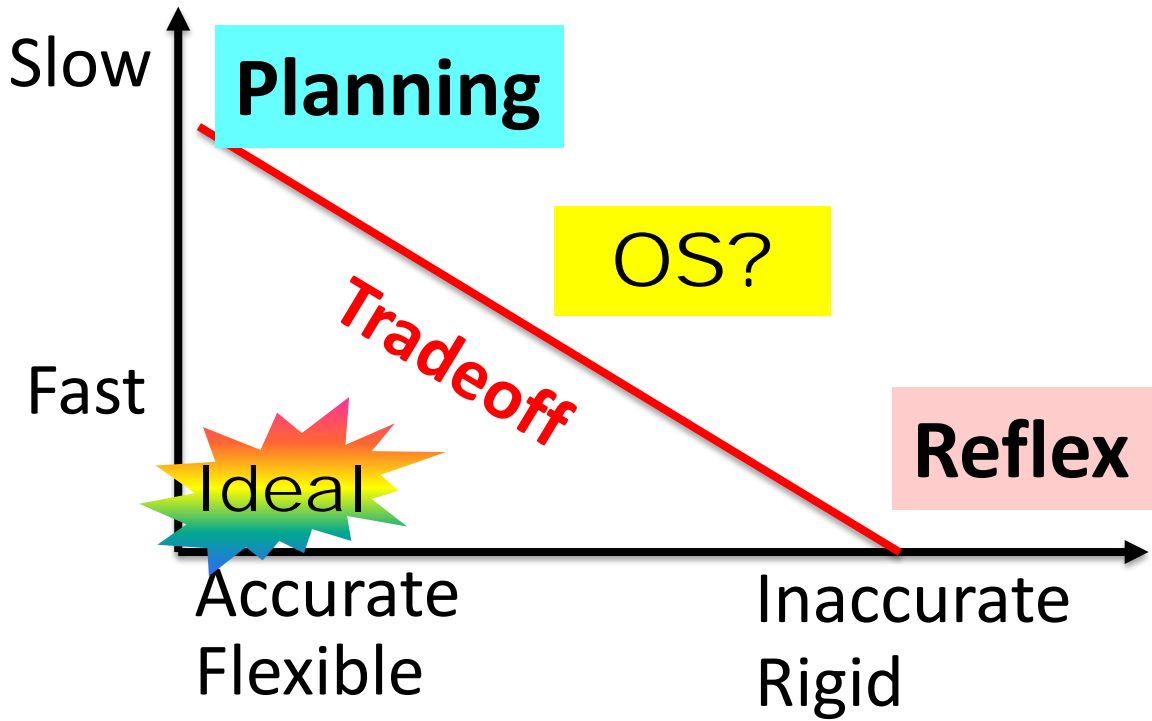
$$M = LC(zI - A)^{-1} \Rightarrow MB = LC(zI - A)^{-1}B = LP_{22}$$



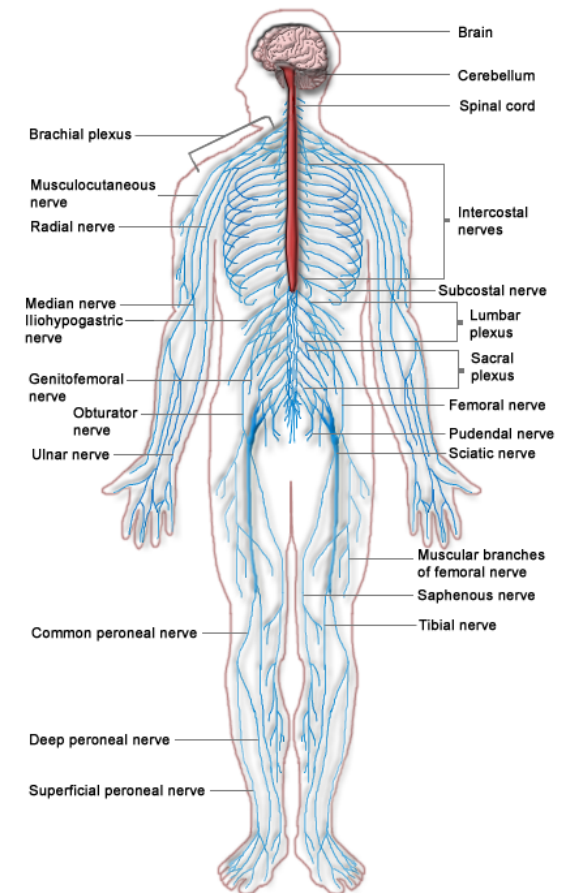
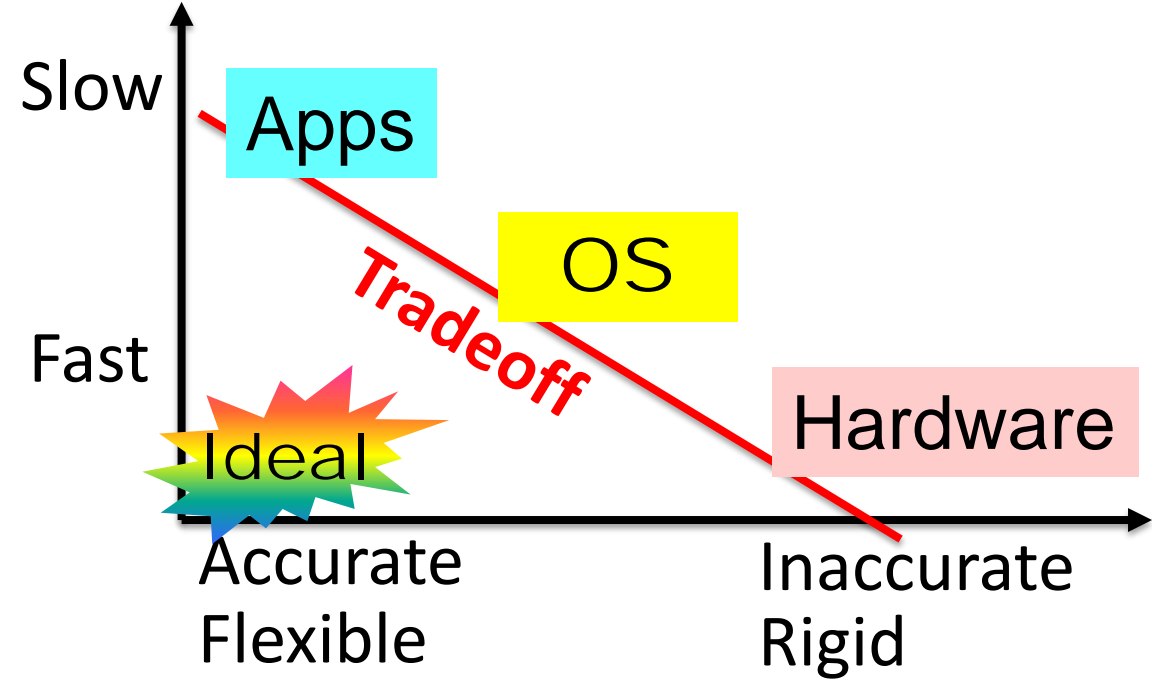
$$\begin{bmatrix} \mathbf{x} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{N} \\ \mathbf{M} & \mathbf{L} \end{bmatrix} \begin{bmatrix} \delta \mathbf{x} \\ \delta \mathbf{y} \end{bmatrix}$$



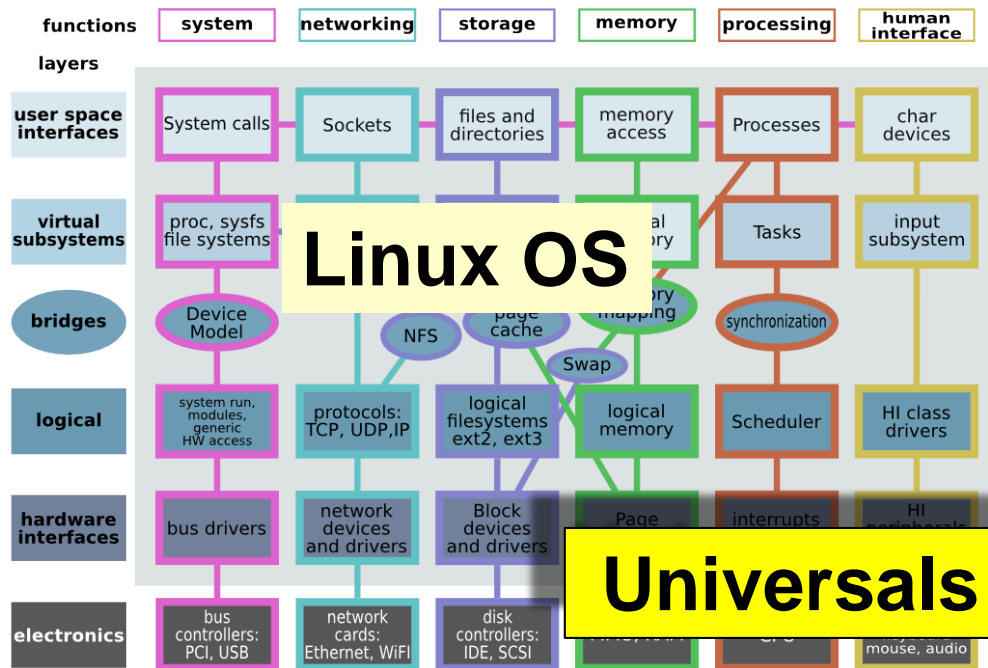




Convergent architecture?

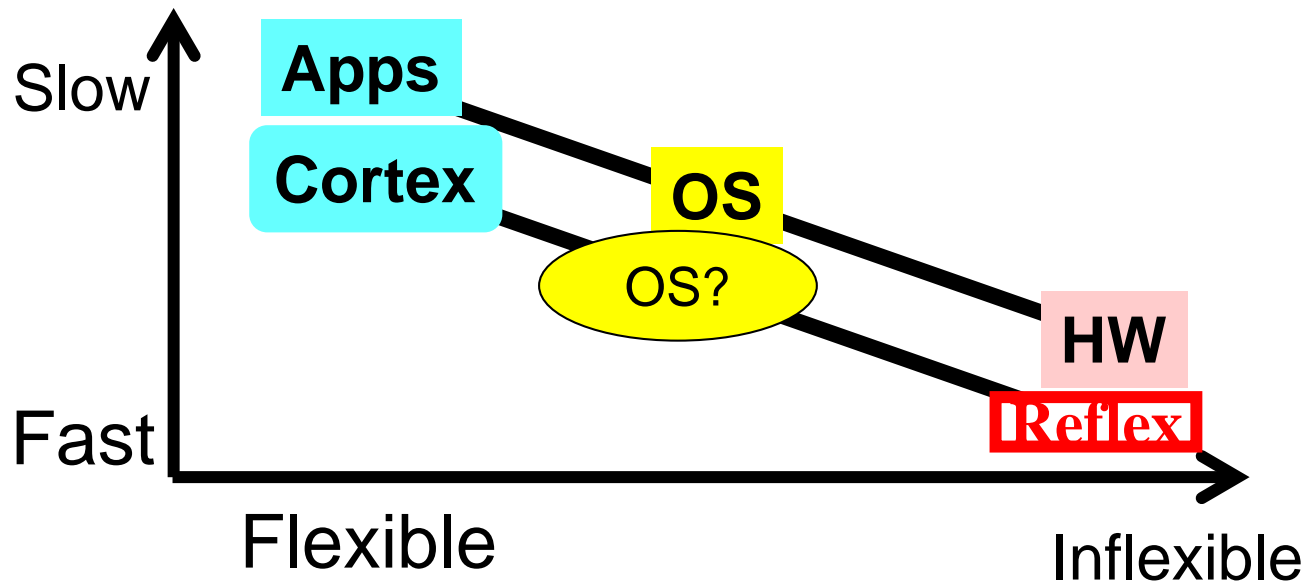
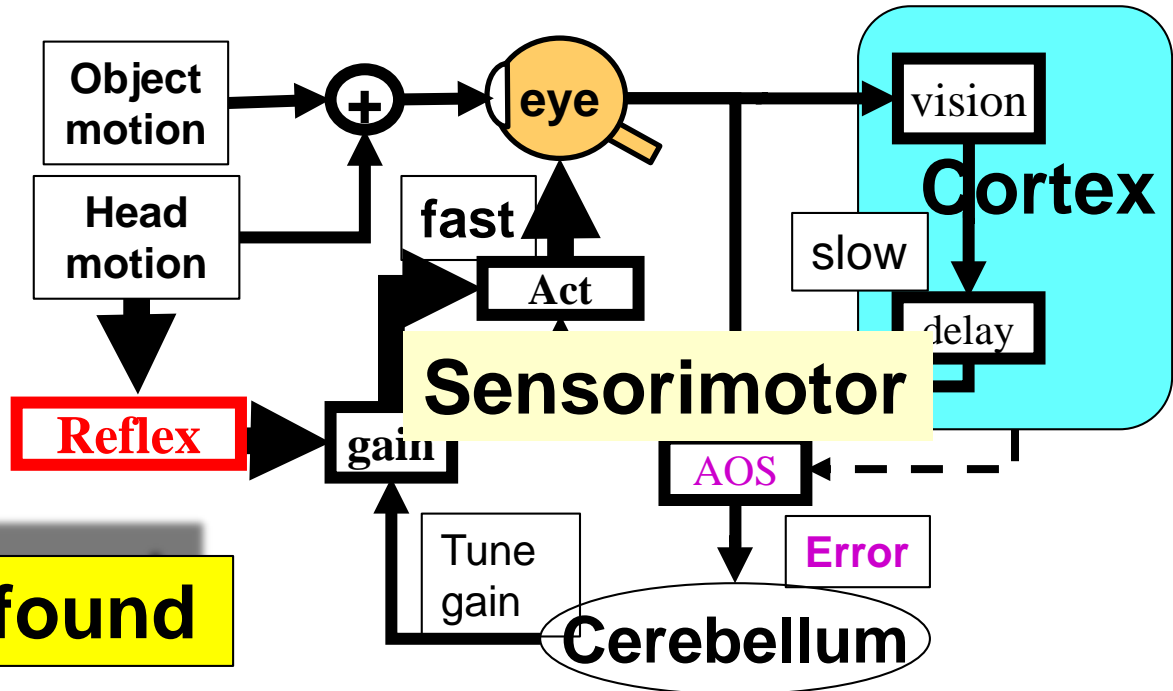


Linux kernel diagram

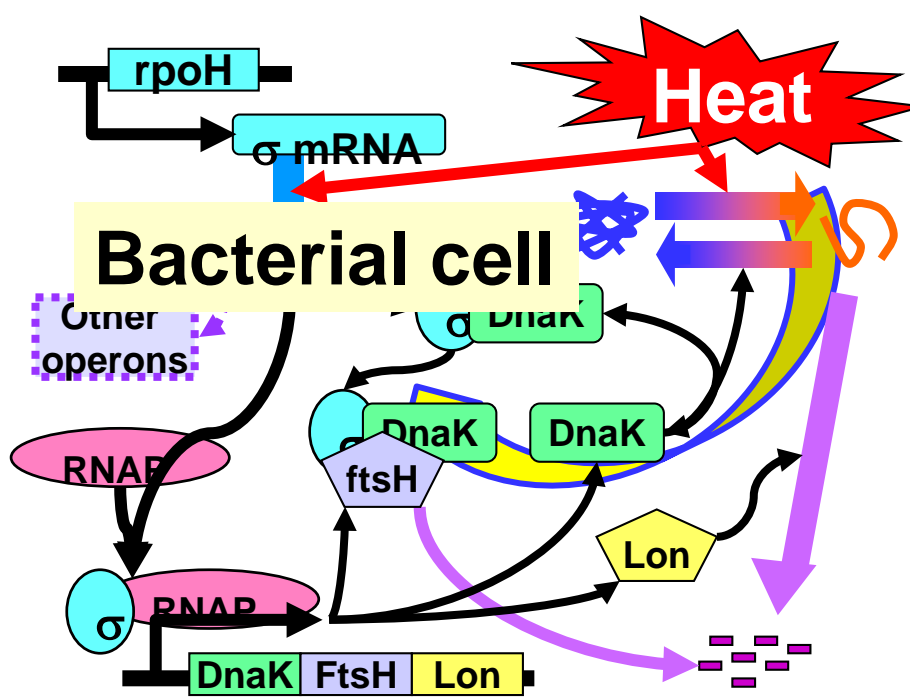
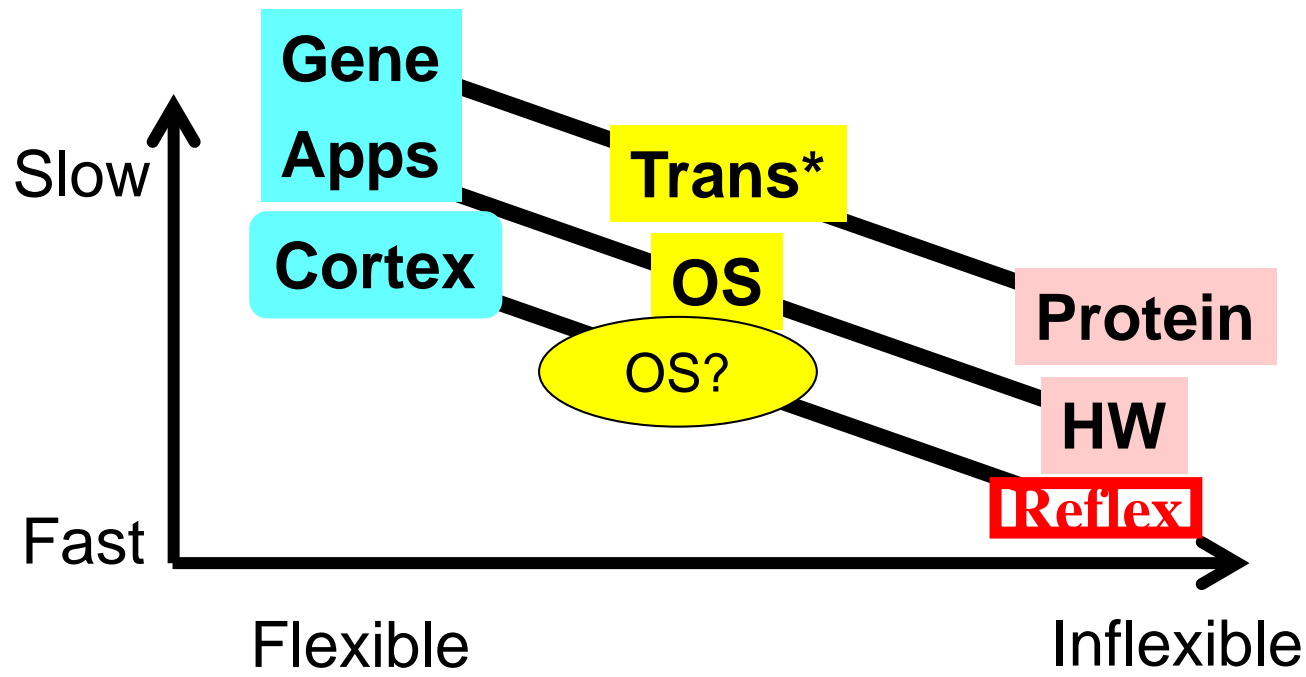
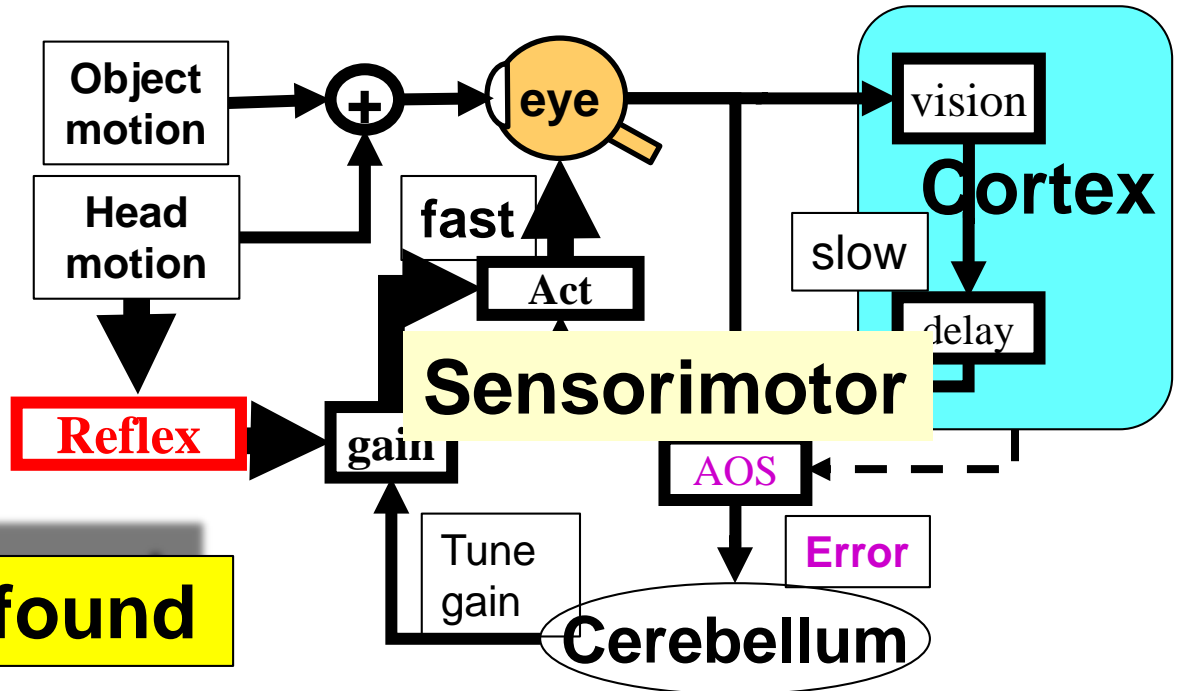
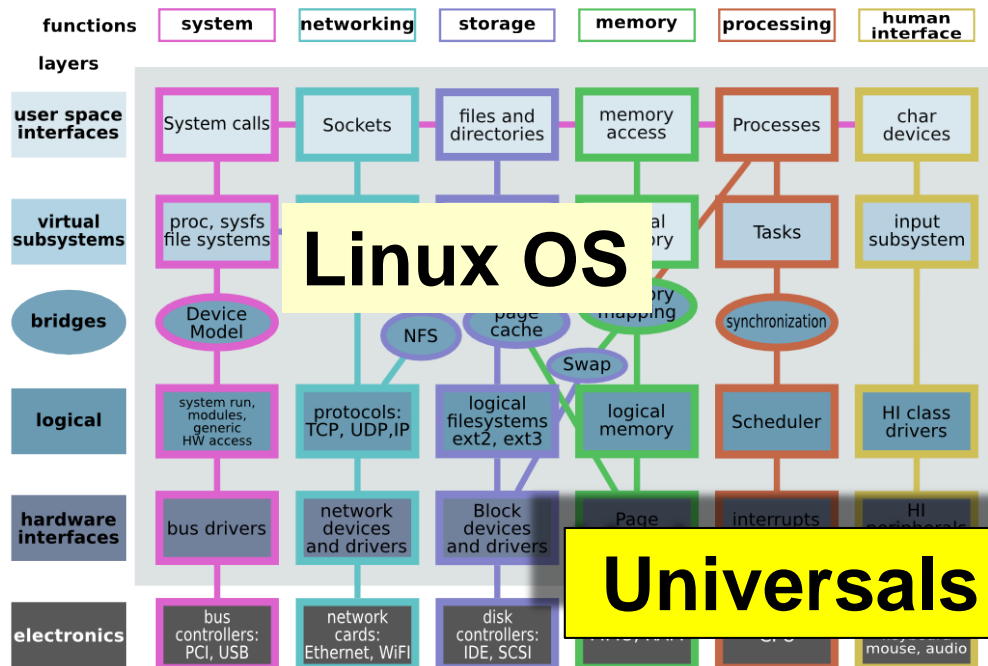


Universals are profound

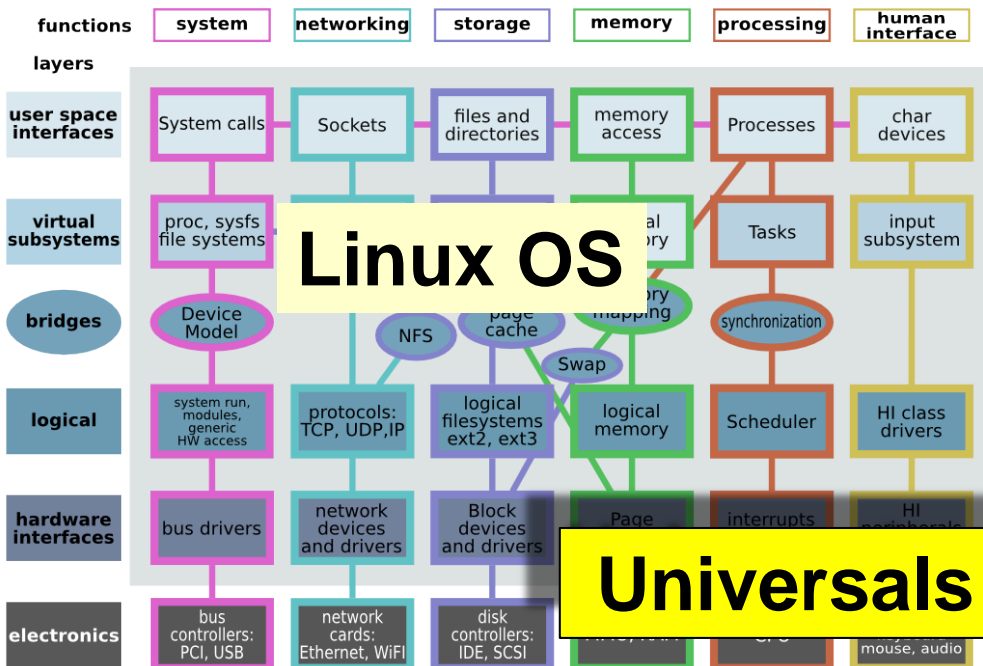
© 2007-2009 Constantine Shulyupin <http://www.MakeLinux.net/kernel/diagram>



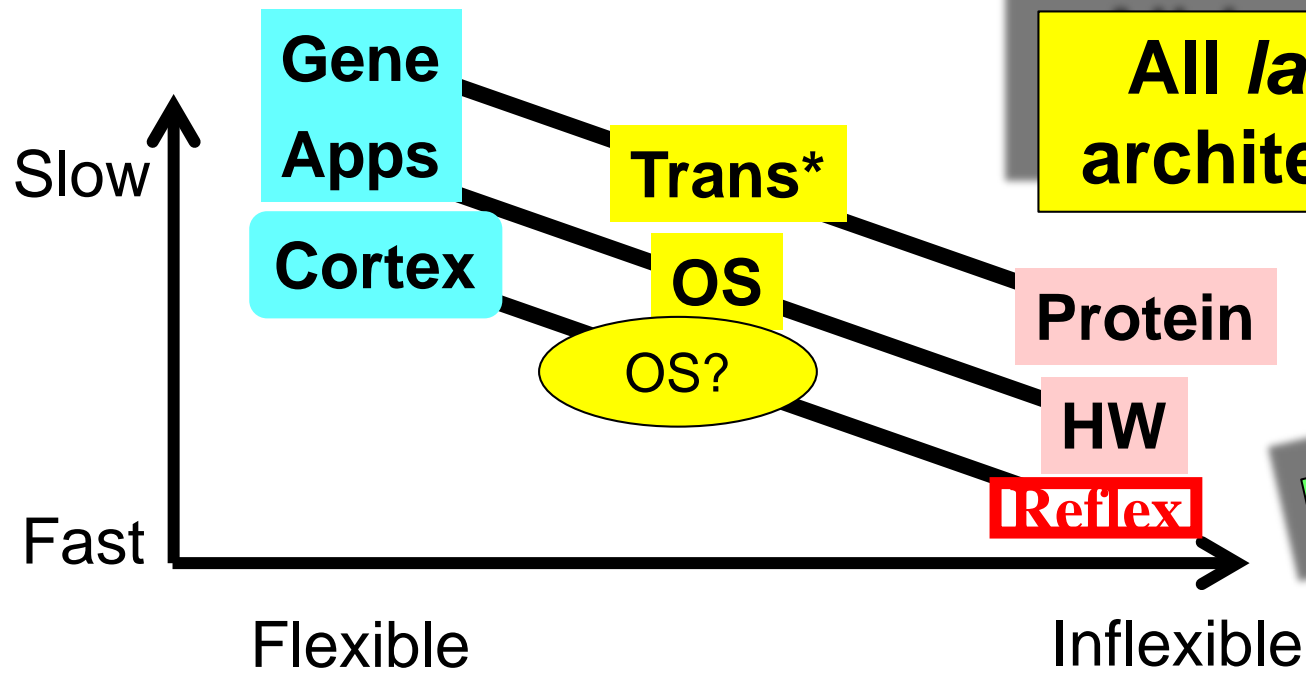
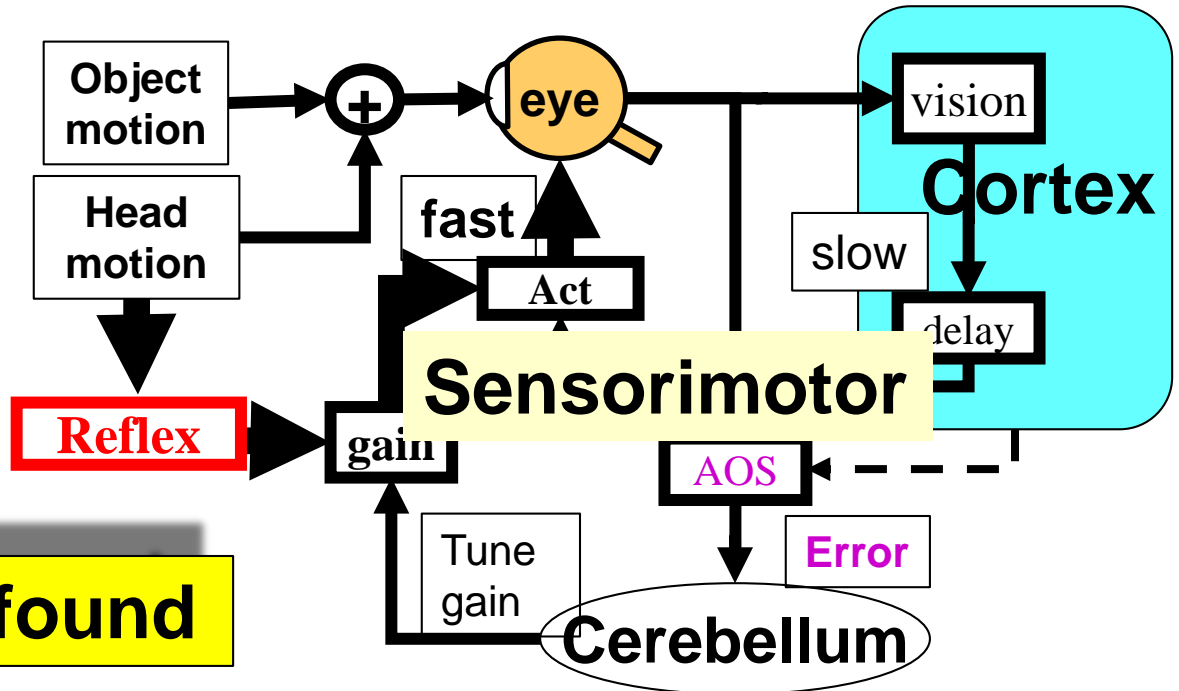
Linux kernel diagram



Linux kernel diagram

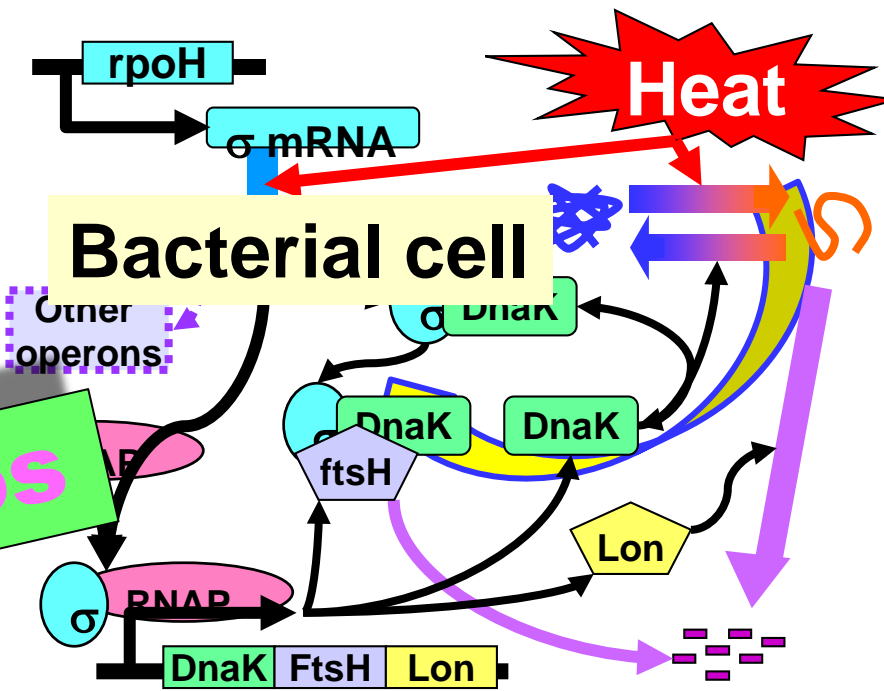


Universals are profound

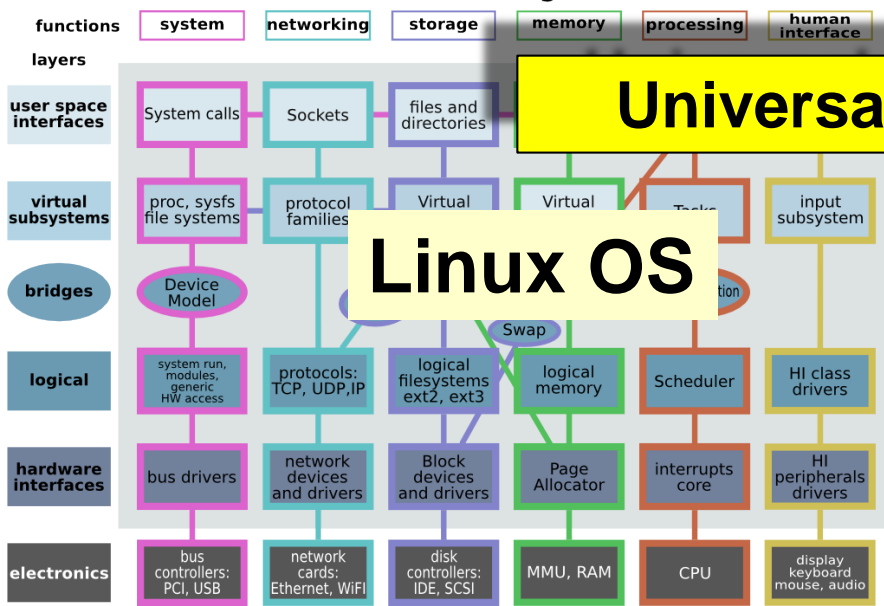


All layered architectures

Videos



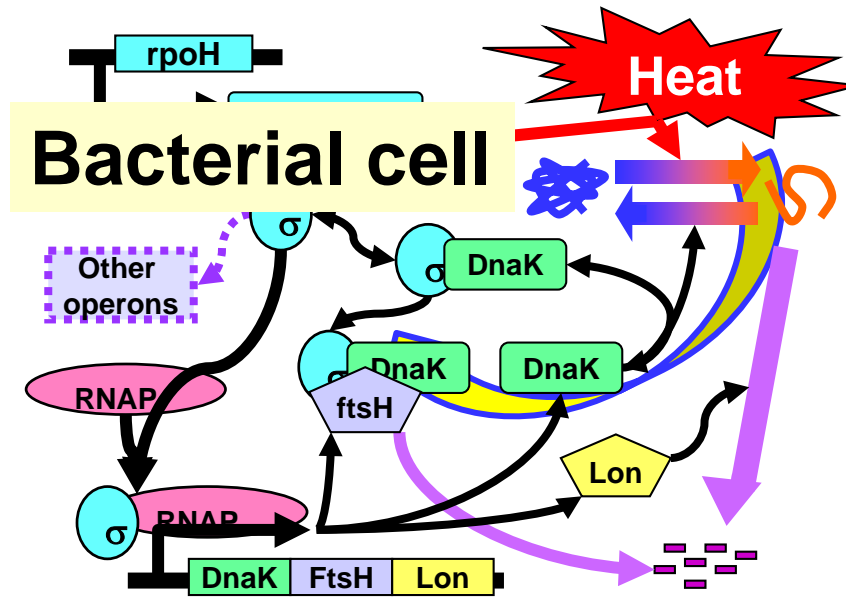
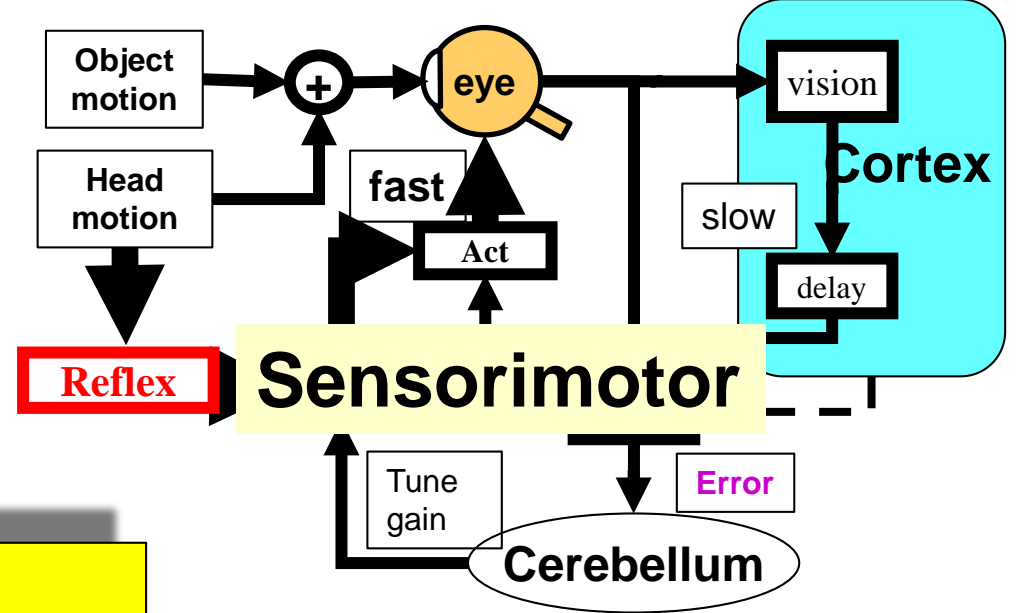
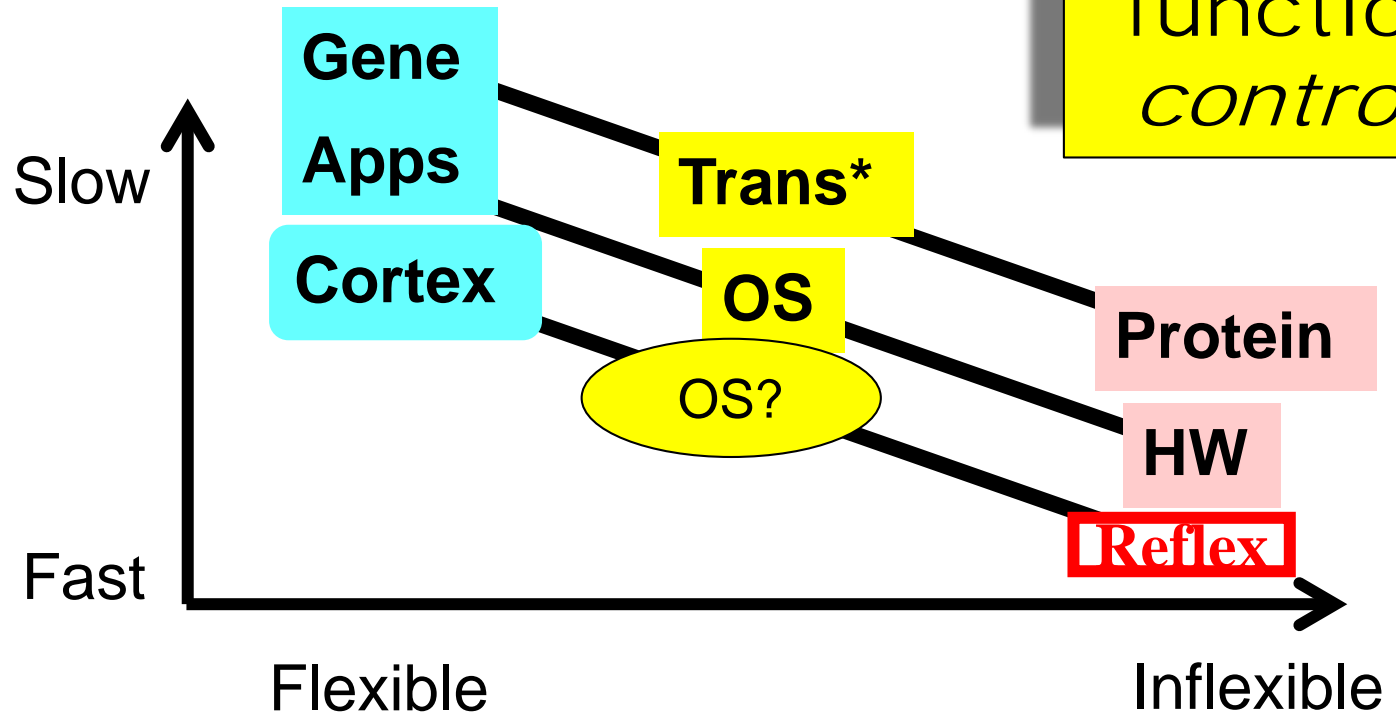
Linux kernel diagram

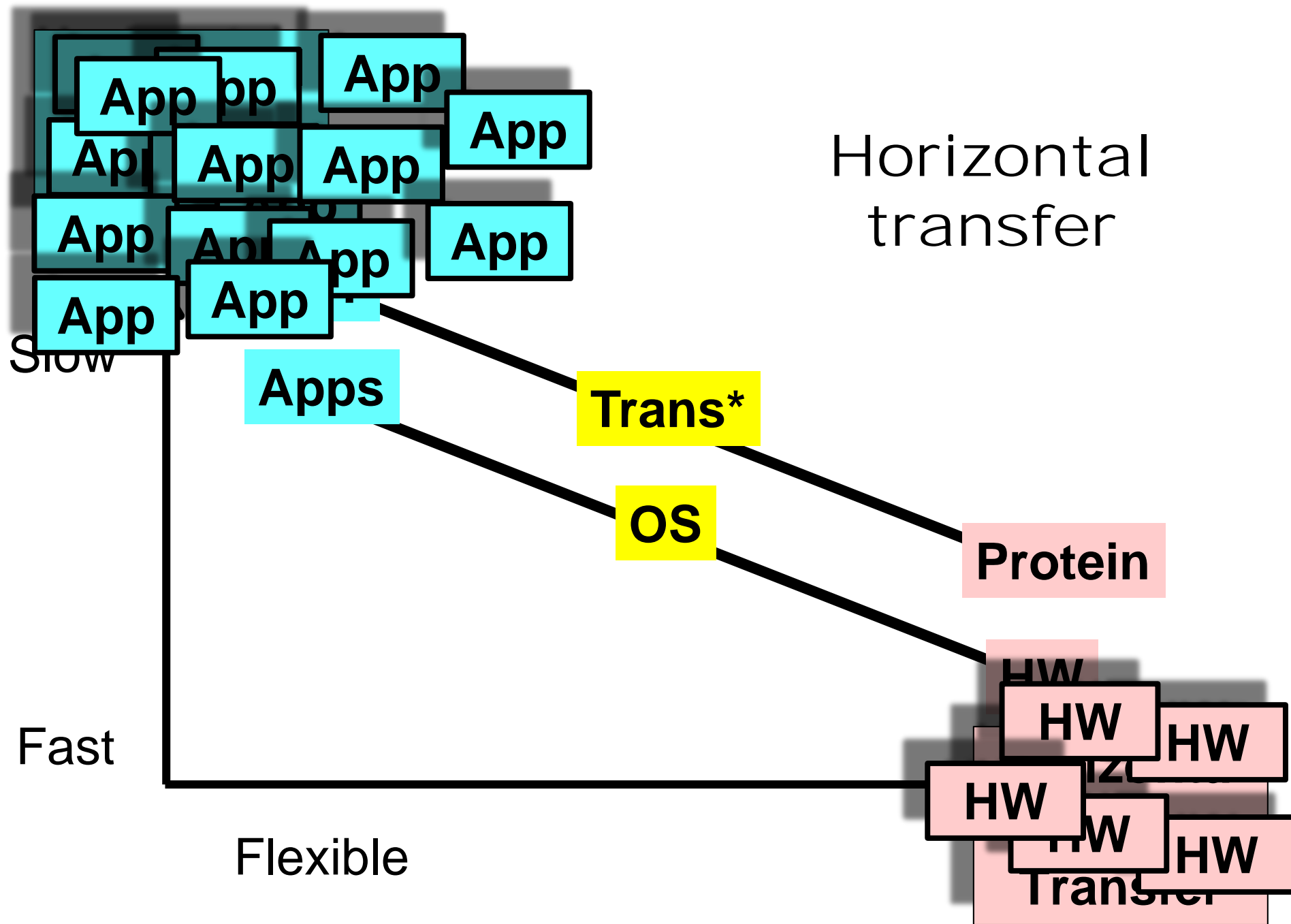


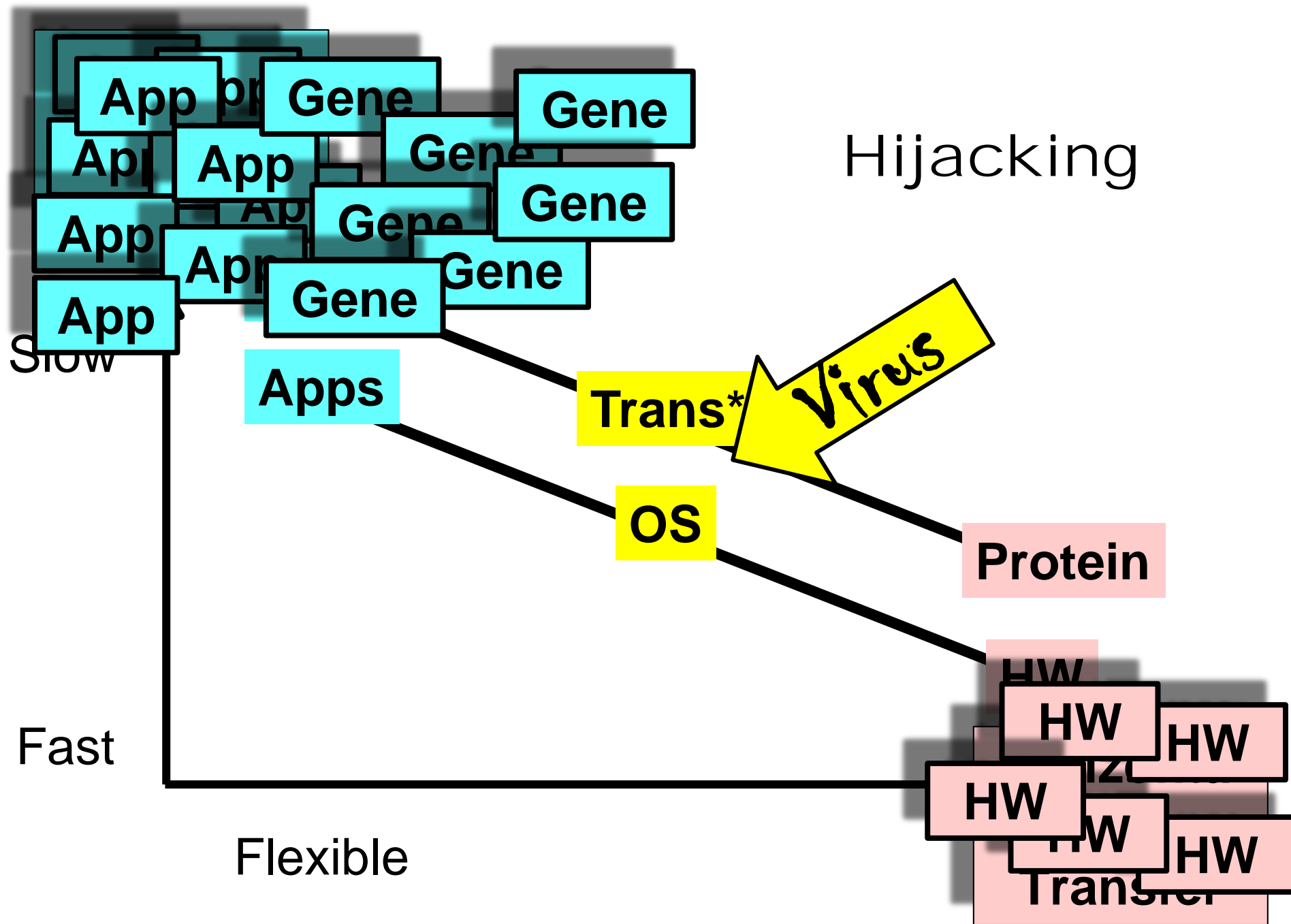
Universals are profound

Linux OS

Where function is controlled







Predators
don't care
about
architecture

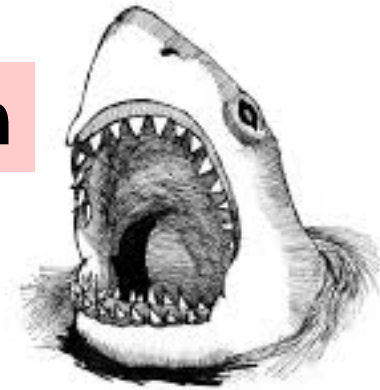


OK to
ignore/destroy
architecture

rotein

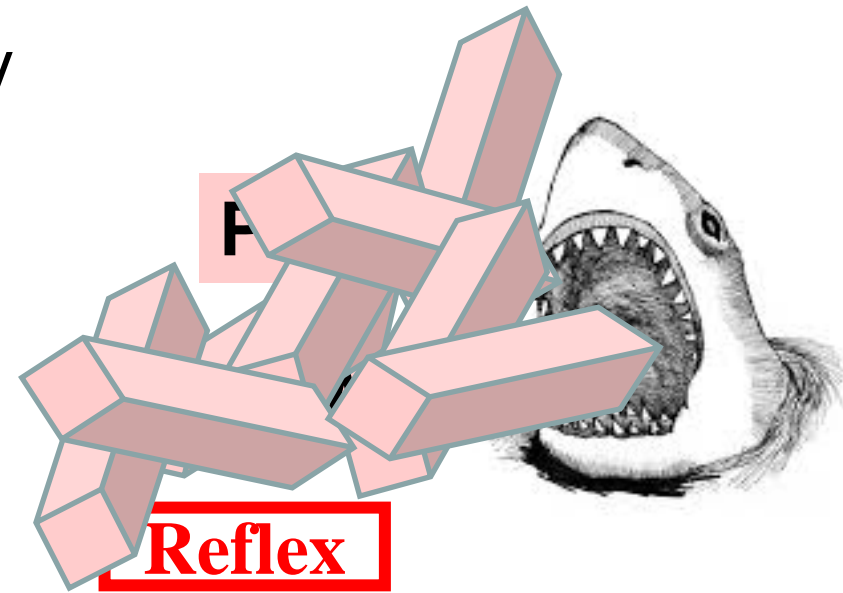
W

lex

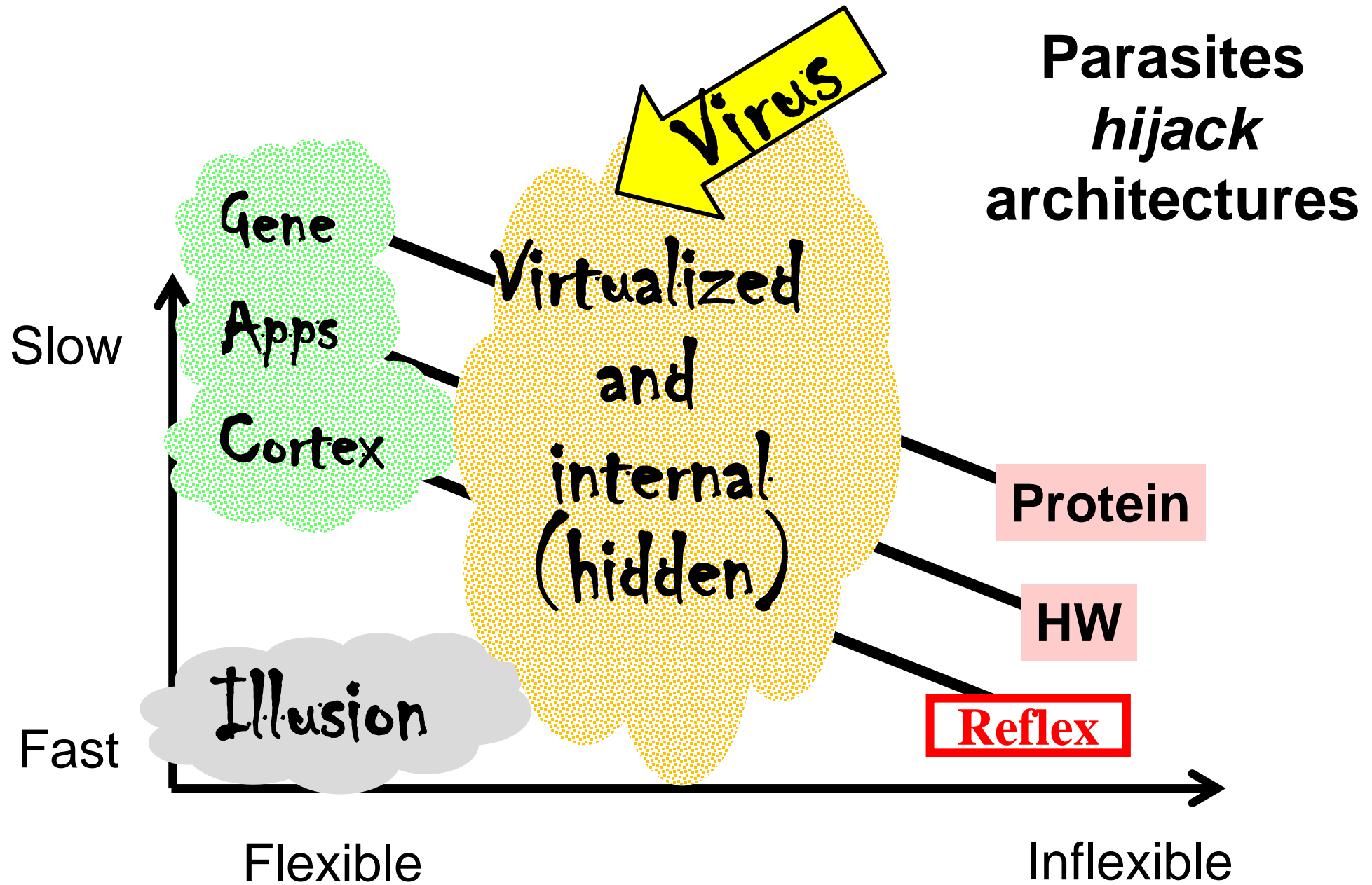


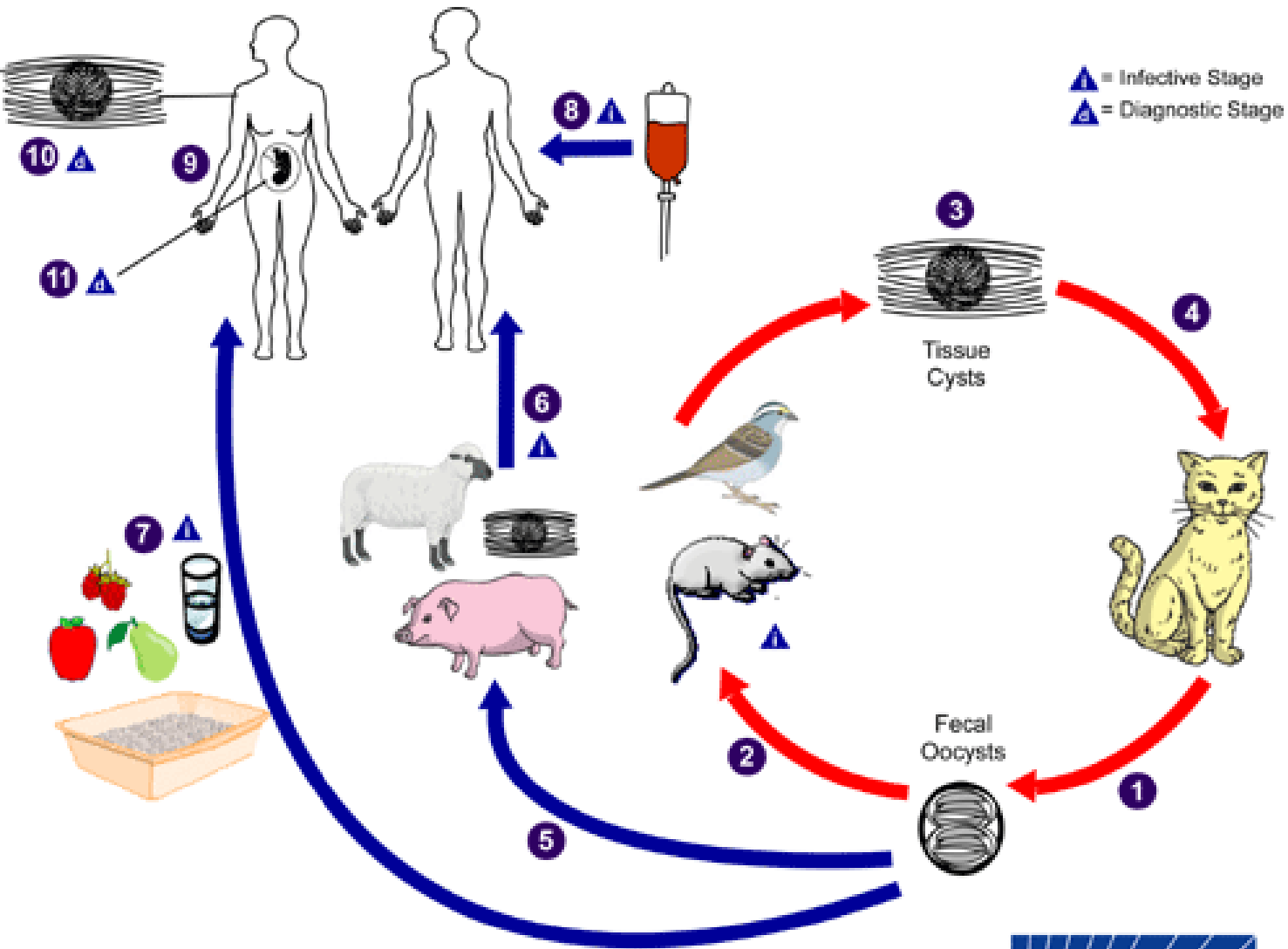
Predators
don't care
about
architecture

OK to
ignore/destroy
architecture



Consumes physical
building blocks





Zombie
parasites

Life Cycle of the Zombie Fly *Apocephalus borealis*

Female flies find a bee.



A Female Zombie Fly Laying Eggs inside a Honey Bee

Fly larvae (maggots) eat the insides of a bee, killing it.



A Maggot Emerges from a Honey Bee



Zombie parasites

A Female Zombie Fly



Cercariae become metacercariae after being eaten by an ant.

4



Maggots pupate

Cercariae are released from the snail via the respiratory pore in a slime ball.

3



Host becomes infected by ingestion of infected ants.

5



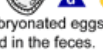
6

Adult in bile duct.



Embryonated eggs are shed in the feces.

1



▲ = Infective Stage
▲ = Diagnostic Stage

Eggs are ingested by a snail intermediate host.

2



Miracidia 2a → Sporocysts 2b → Cercariae 2c

▲ = Infective Stage
▲ = Diagnostic Stage



Zombie

Predator?



Zience
fiction

Zombieness

Parasite?



Zombie

Predator?



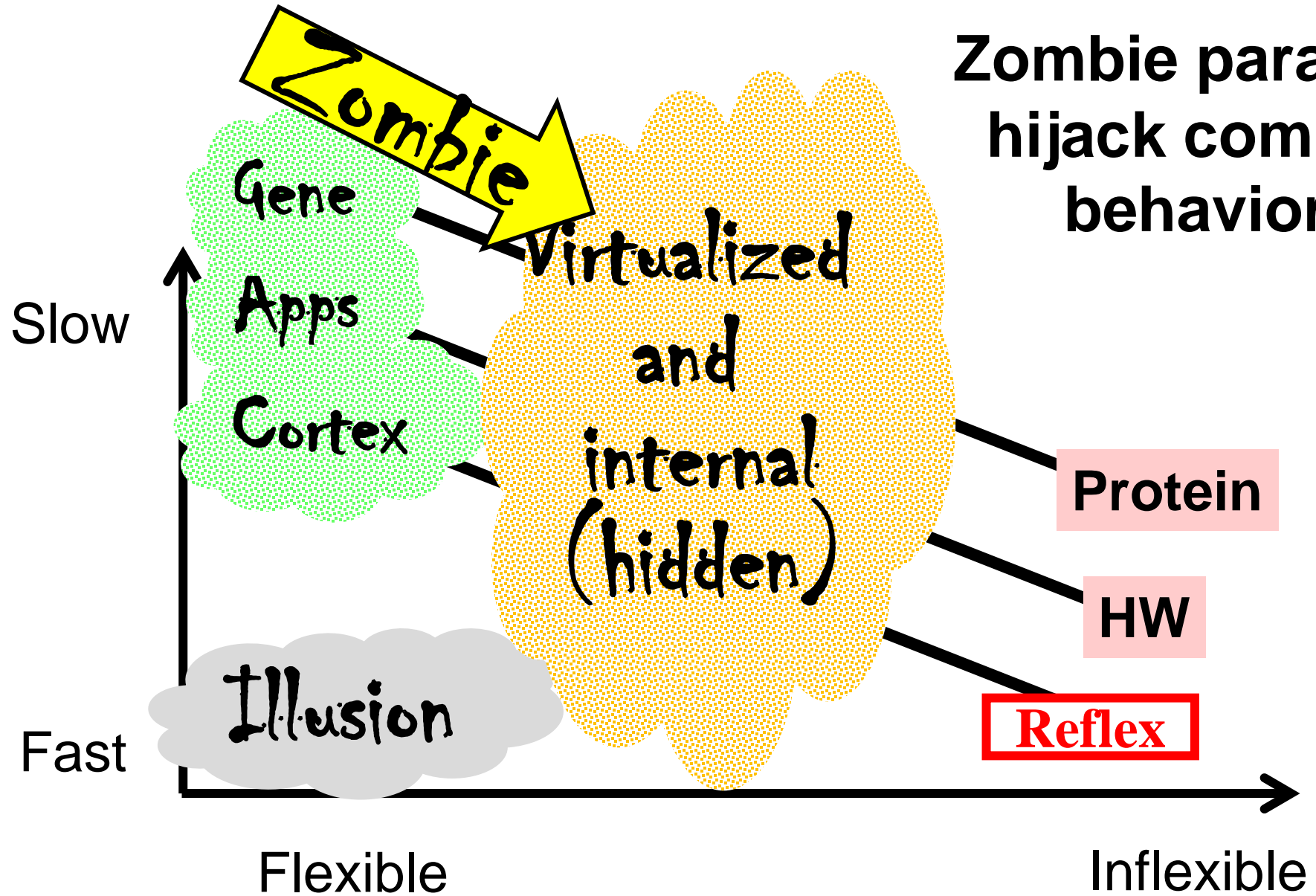
Rabies



Zombieness

Parasite?



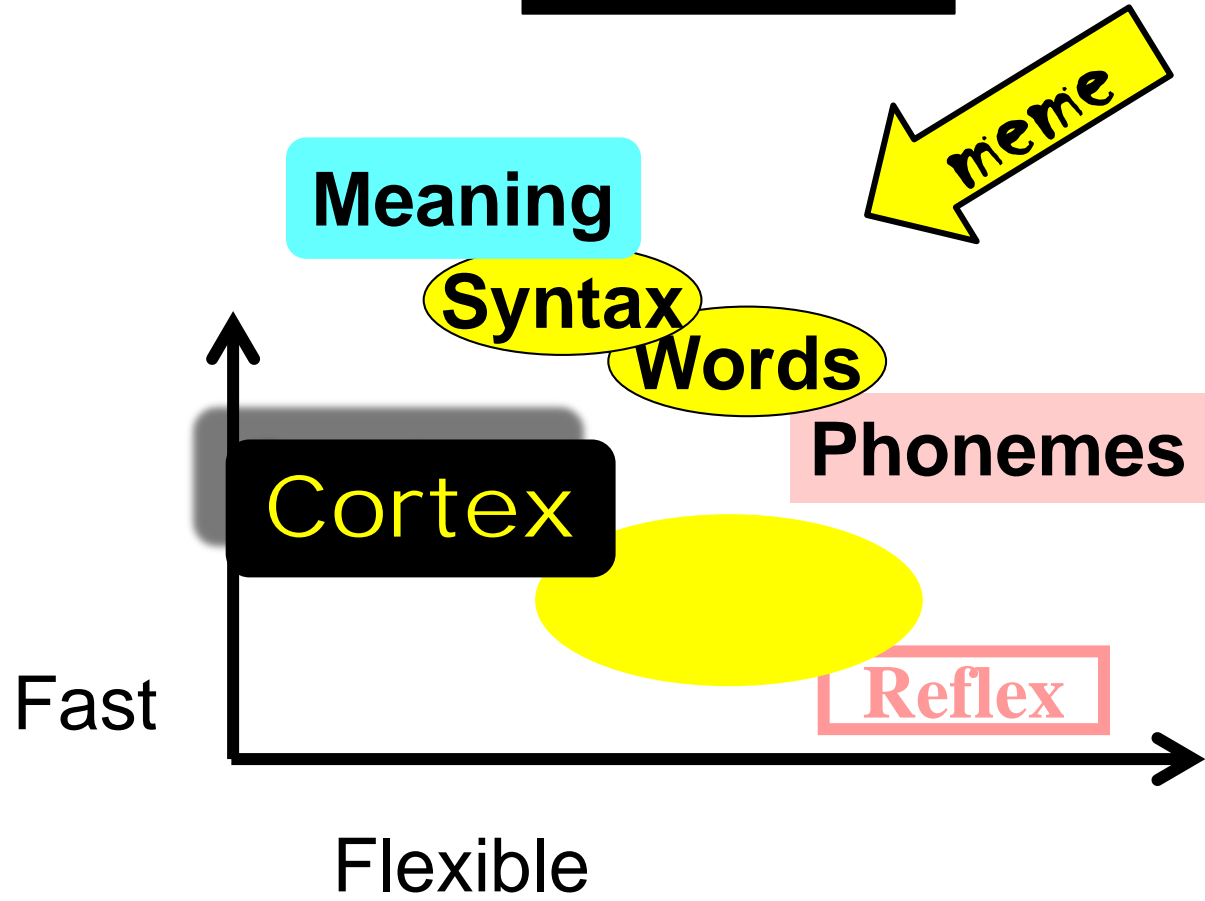


Zombie memes?

Bad Meme Transfer

Hijacking?

- Beliefs
- Viral
 - False
 - Unhealthy
 - Dangerous



Lifespan, violence, cancer, wound healing, and sociality

A control architecture perspective

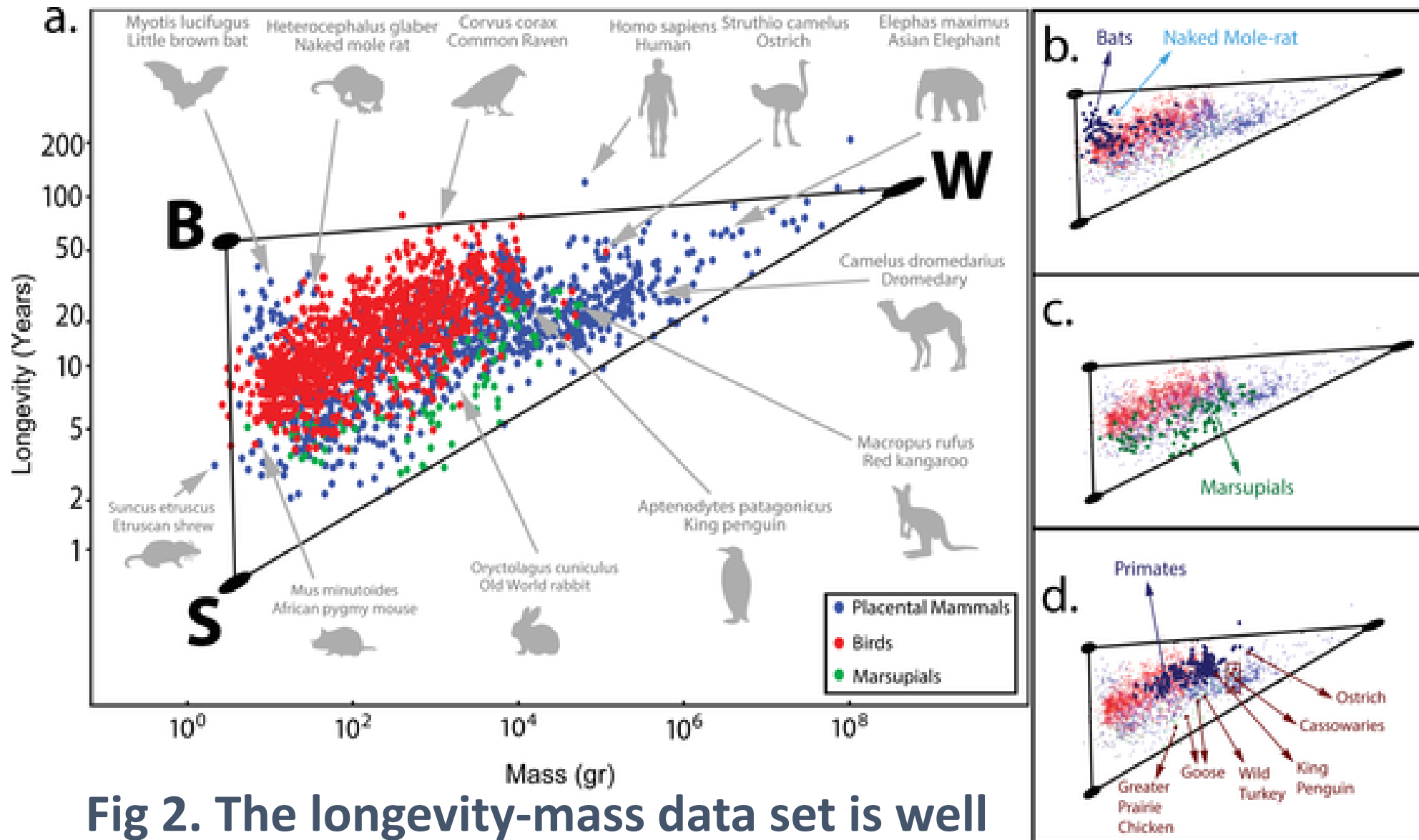


Fig 2. The longevity-mass data set is well described by a triangle in log space.

Szekely P, Korem Y, Moran U, Mayo A, Alon U (2015) The Mass-Longevity Triangle: Pareto Optimality and the Geometry of Life-History Trait Space. PLOS Computational Biology 11(10): e1004524. <https://doi.org/10.1371/journal.pcbi.1004524>
<http://journals.plos.org/ploscompbiol/article?id=10.1371/journal.pcbi.1004524>

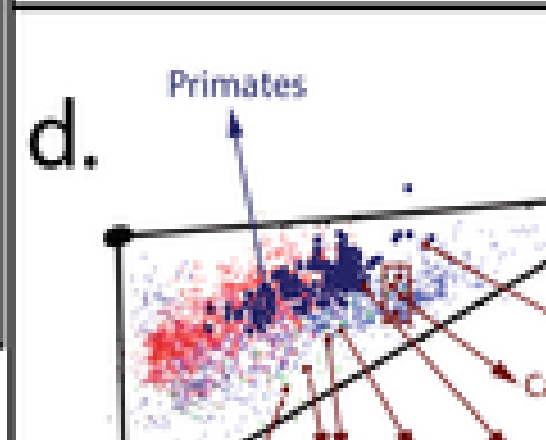
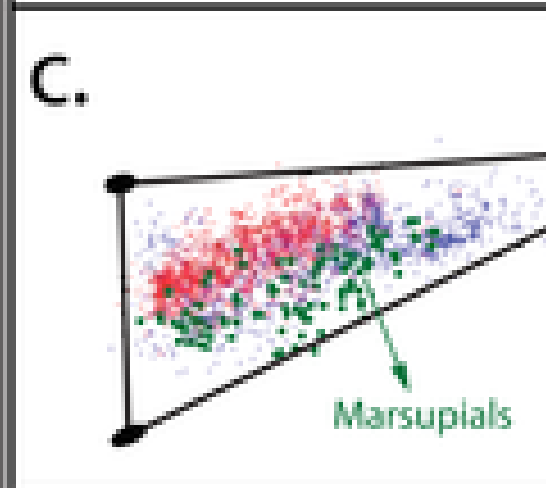
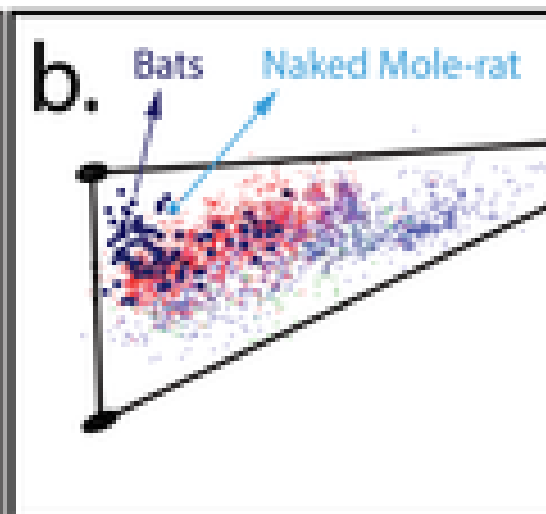
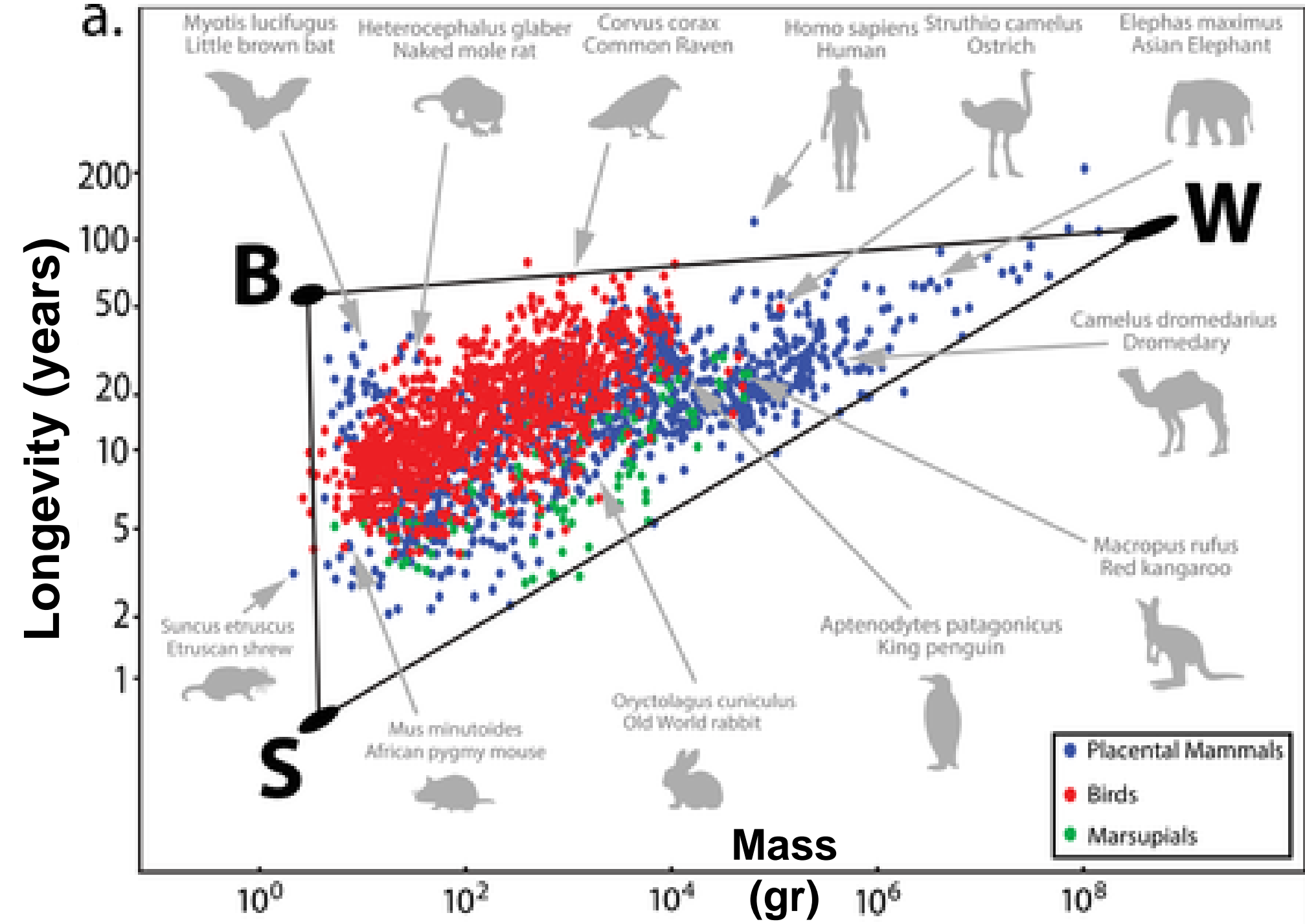
Szekely P, Korem Y, Moran U, Mayo A, Alon U (2015)

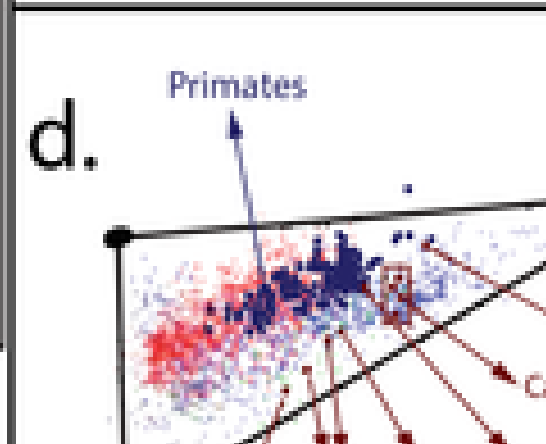
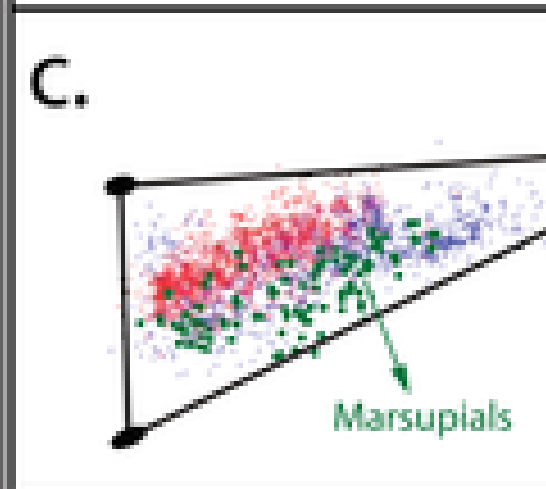
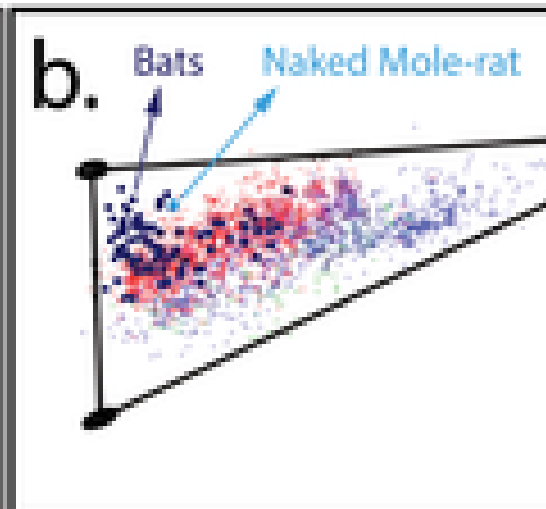
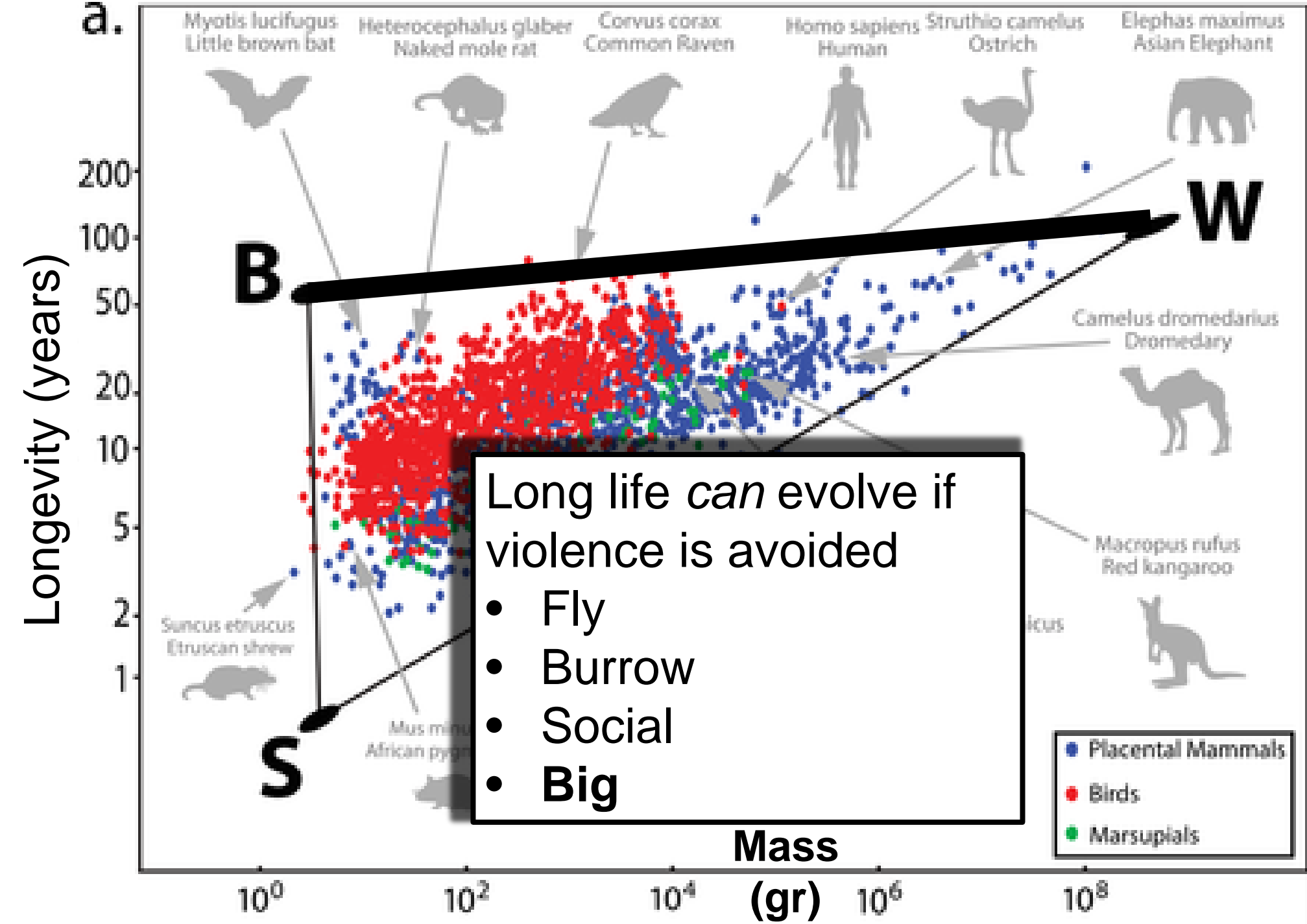
The Mass-Longevity Triangle: Pareto Optimality and the Geometry of Life-History Trait Space.

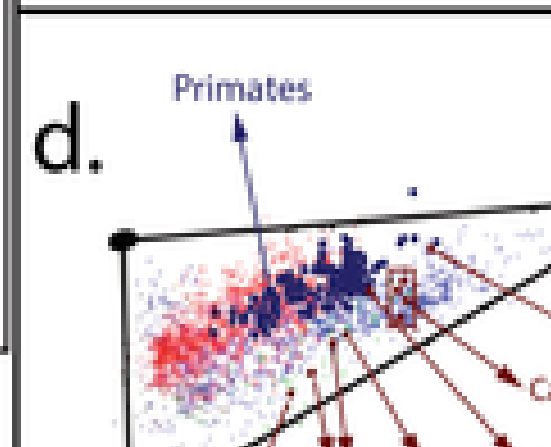
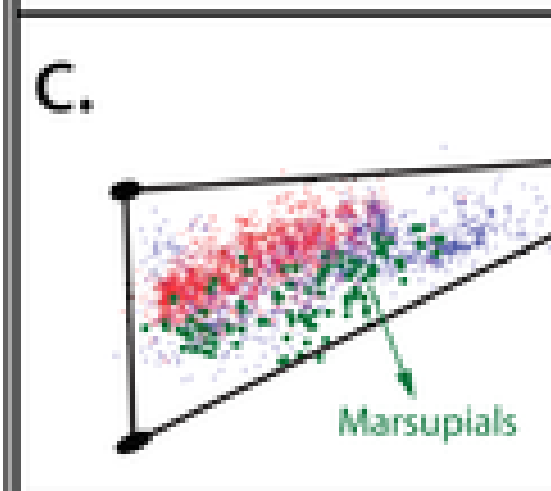
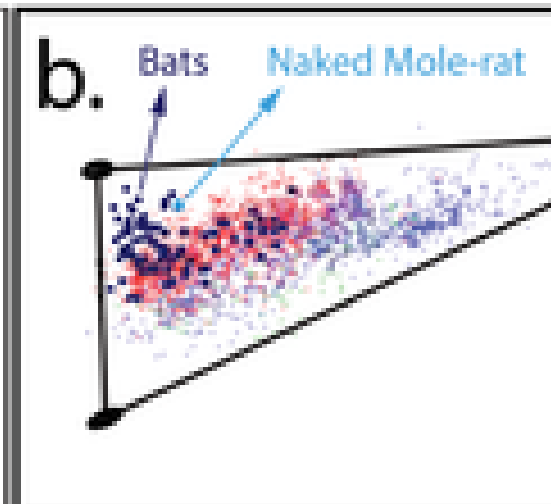
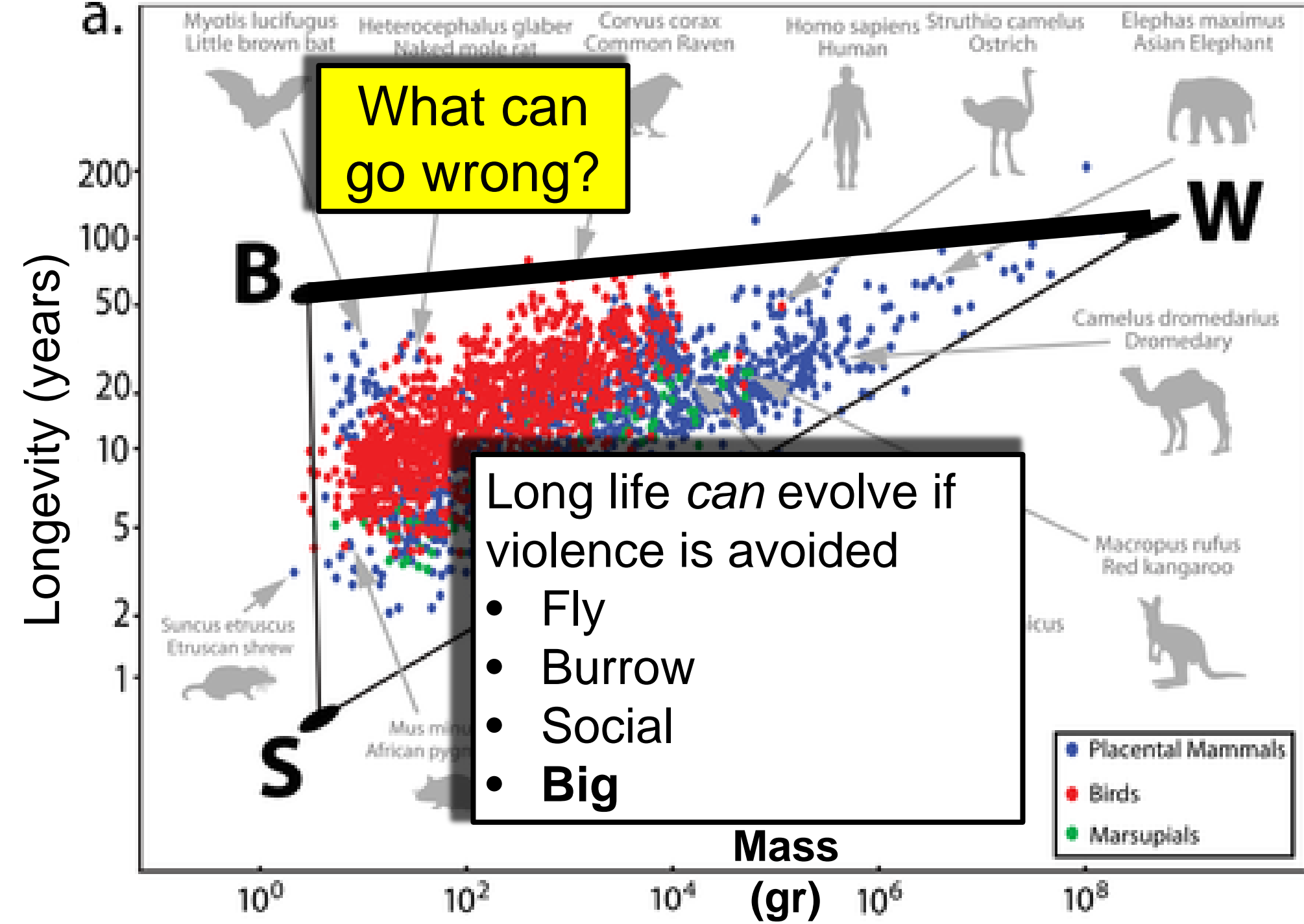
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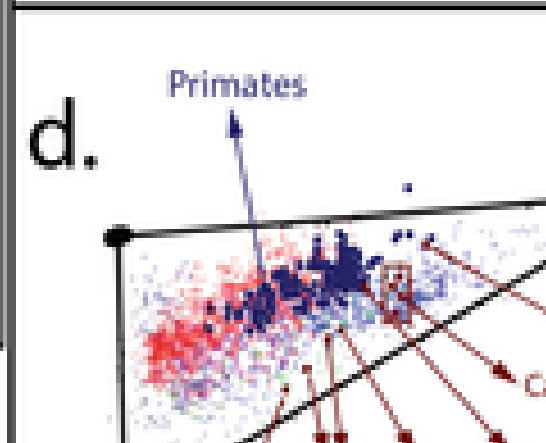
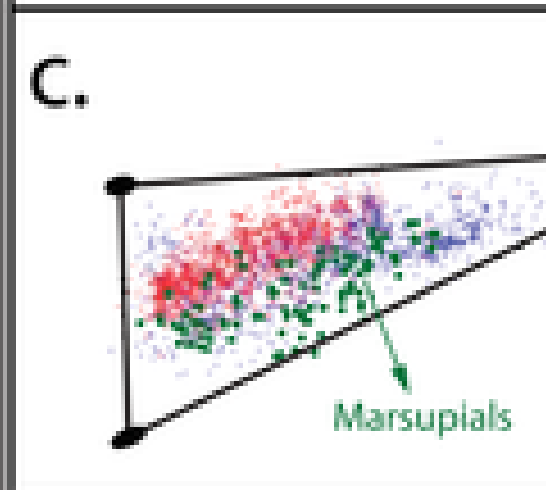
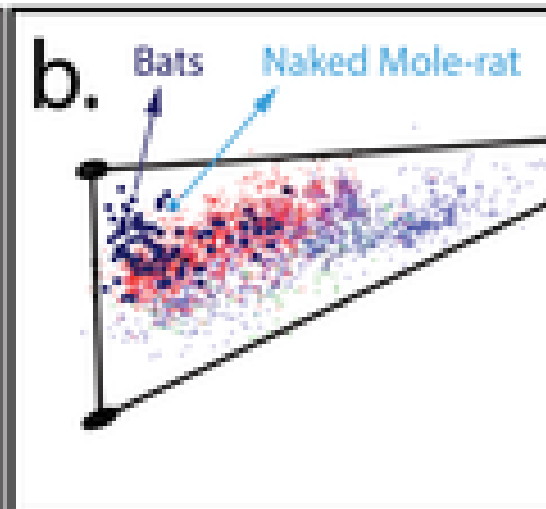
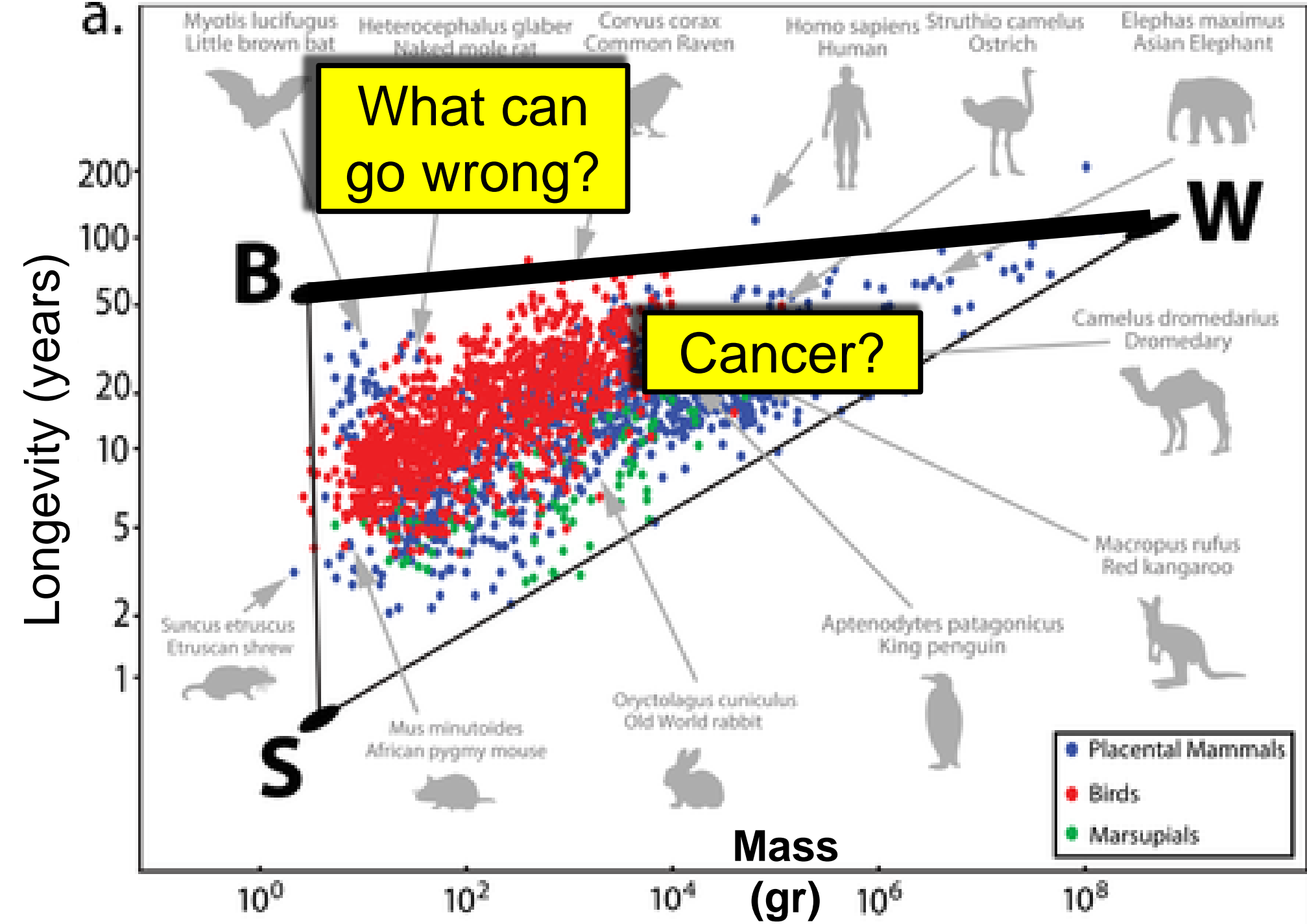
e1004524. <https://doi.org/10.1371/journal.pcbi.1004524>

<http://journals.plos.org/ploscompbiol/article?id=10.1371/journal.pcbi.1004524>

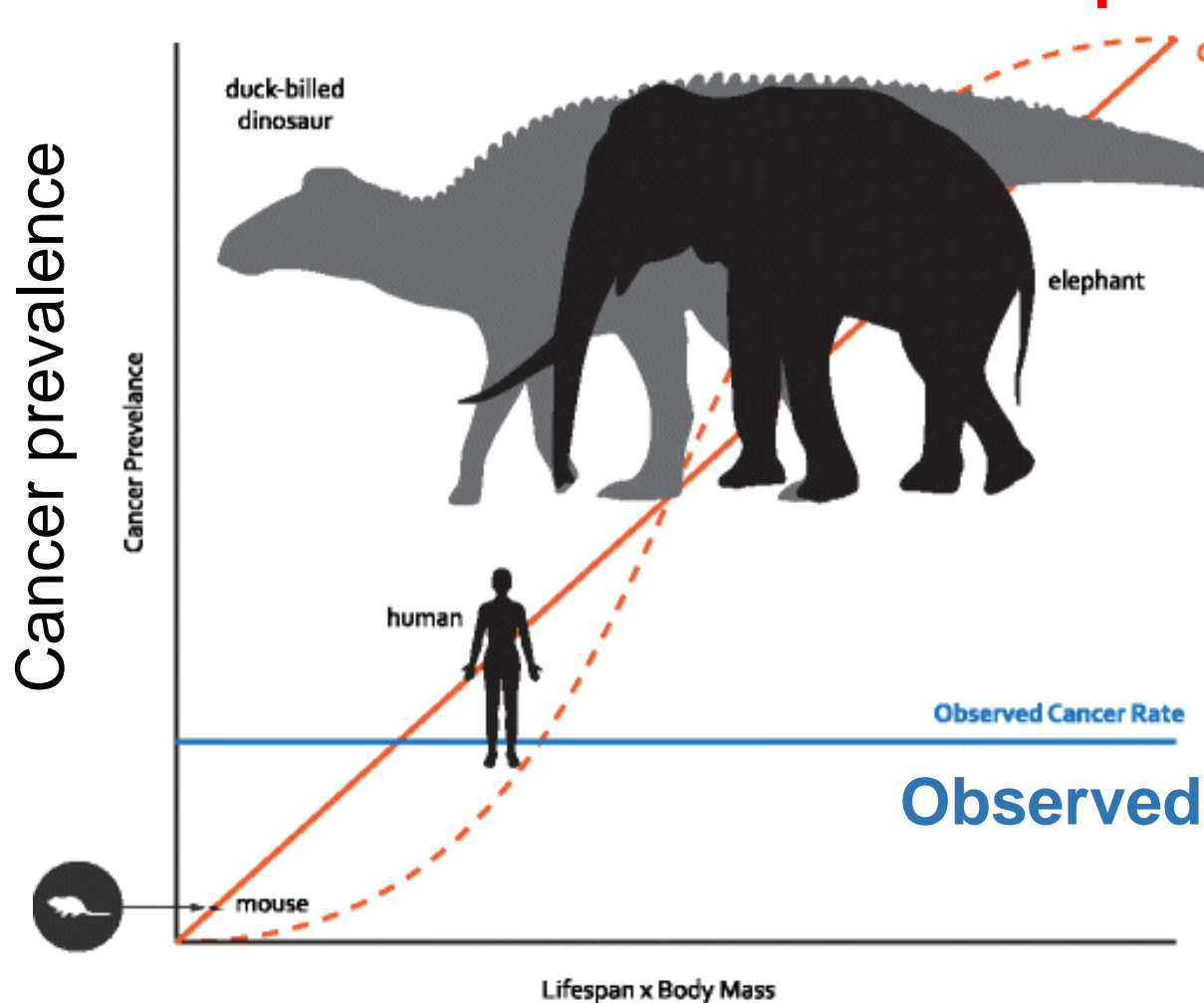








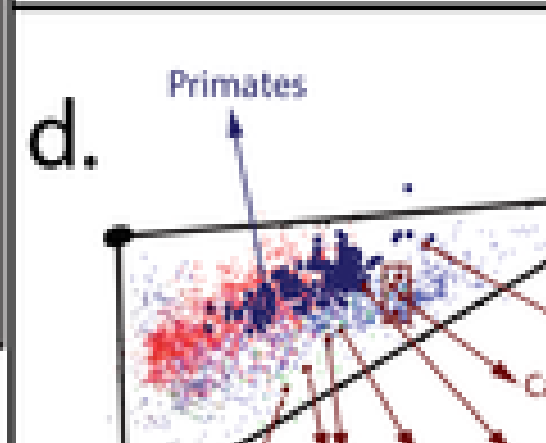
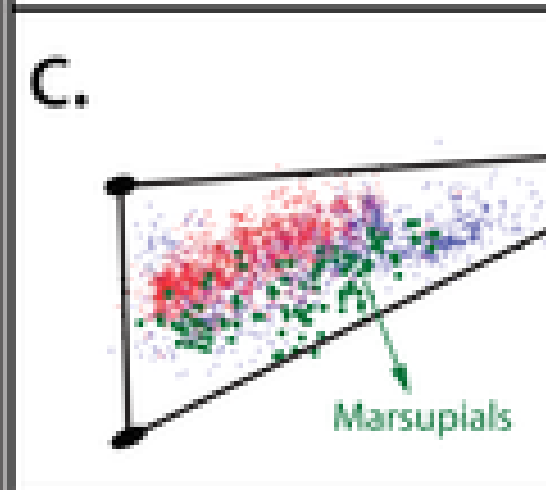
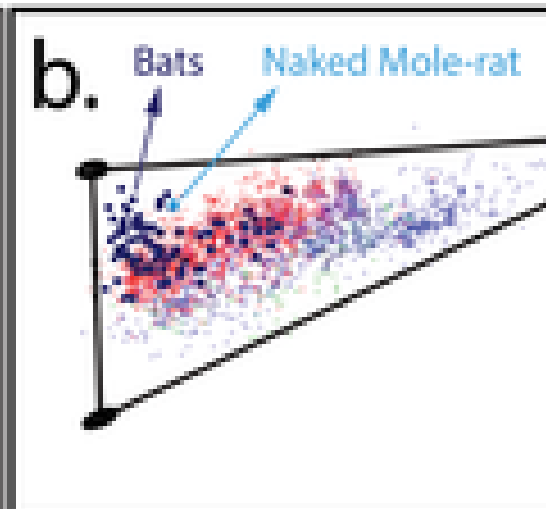
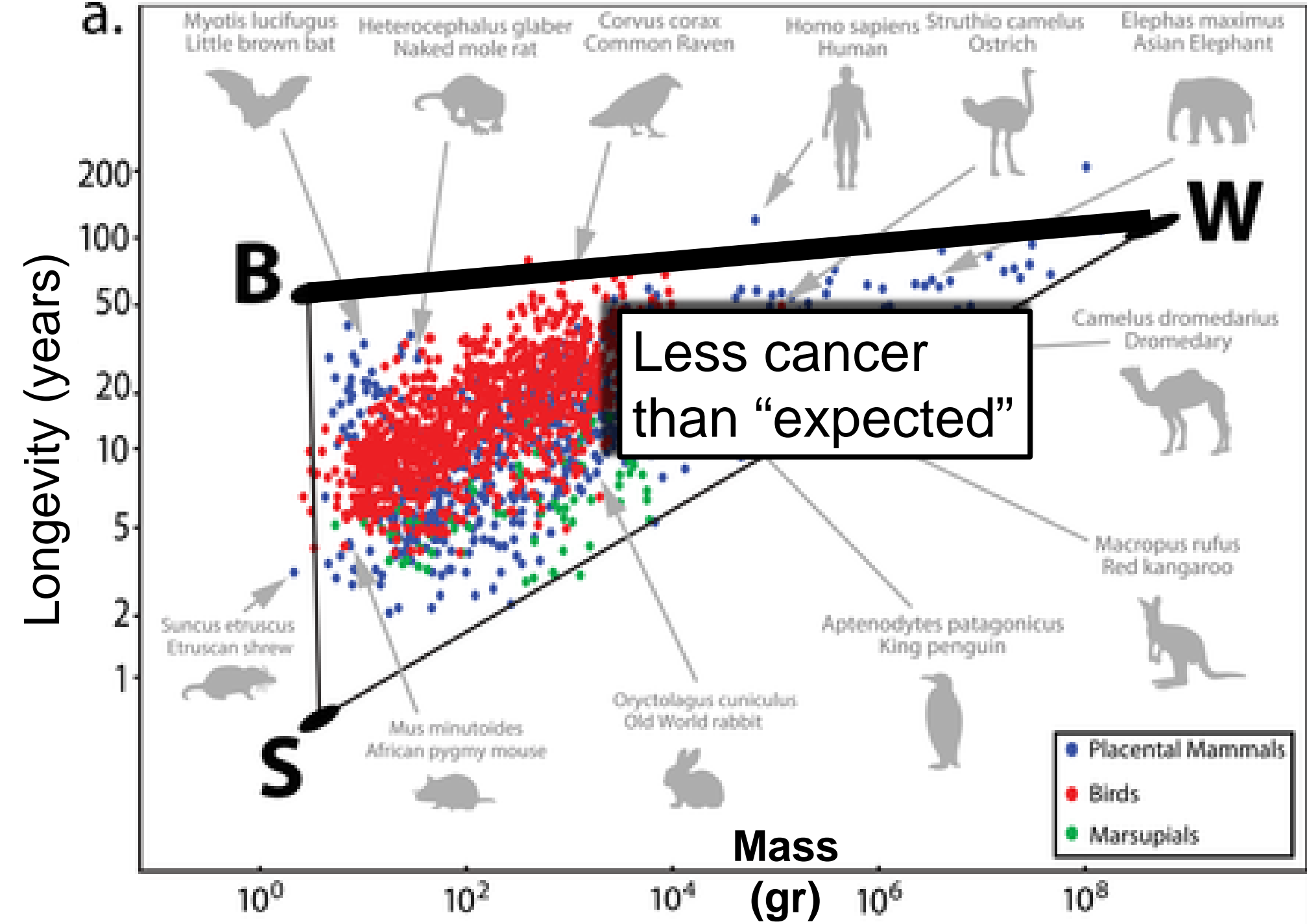
Peto's Paradox

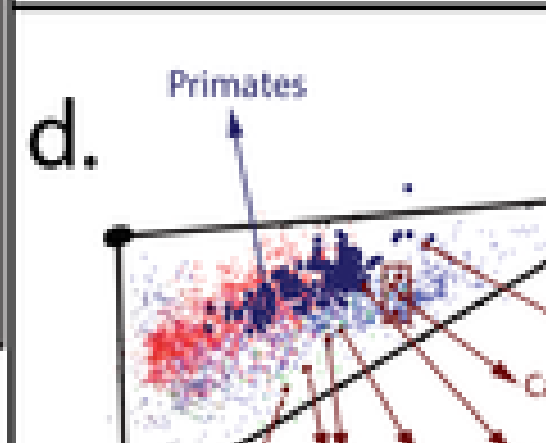
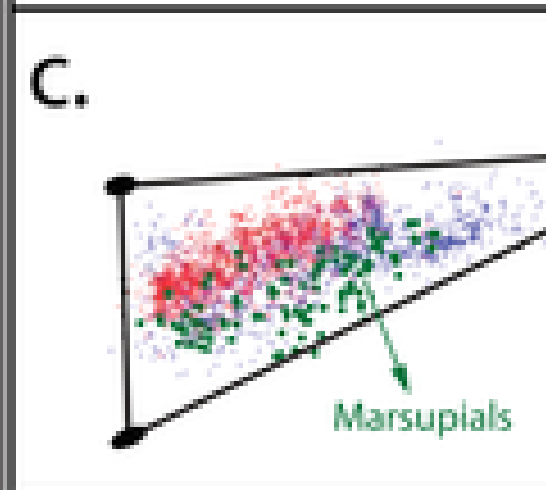
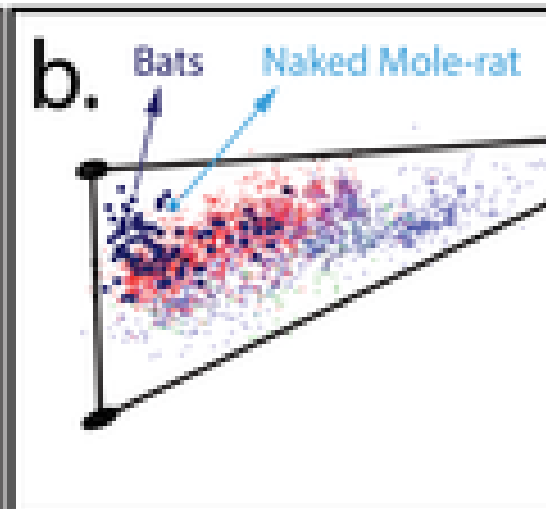
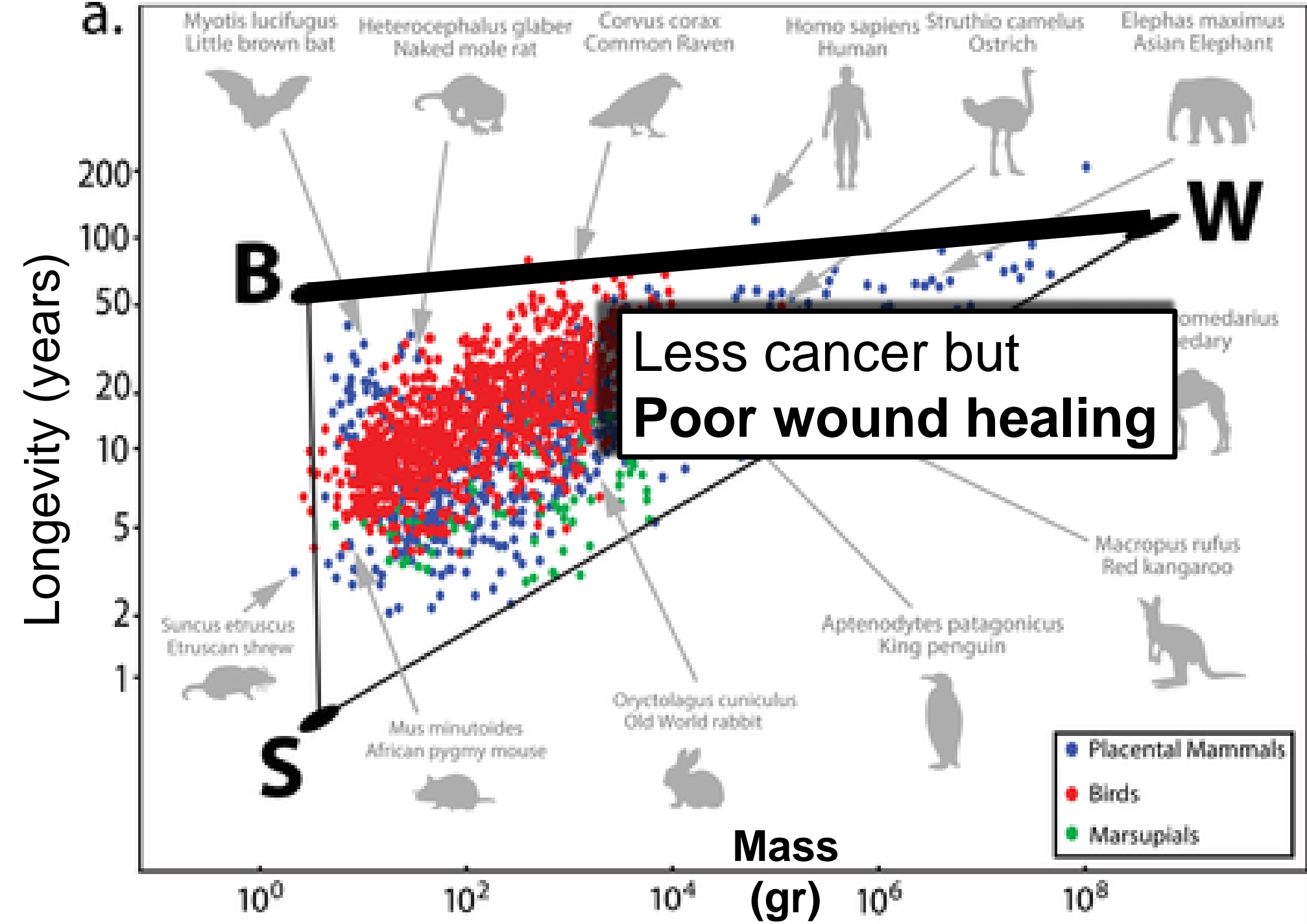


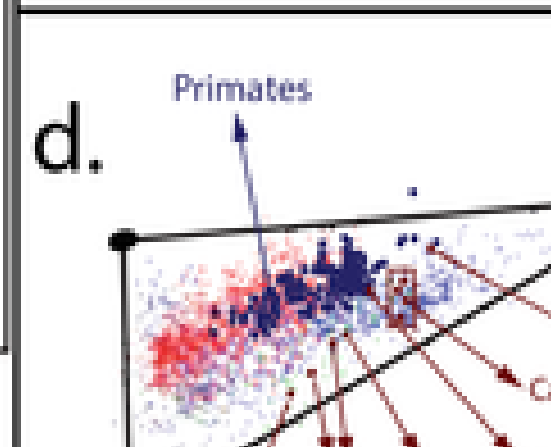
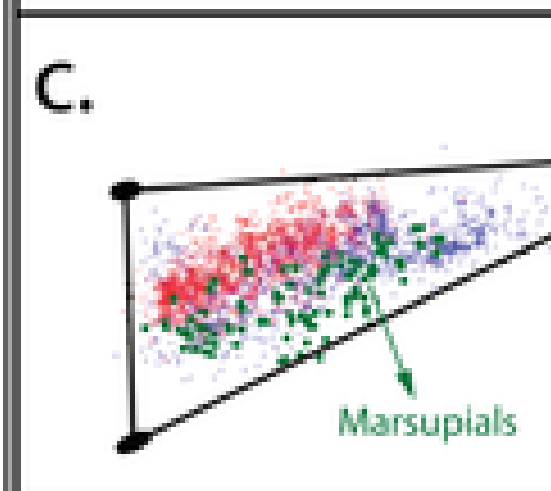
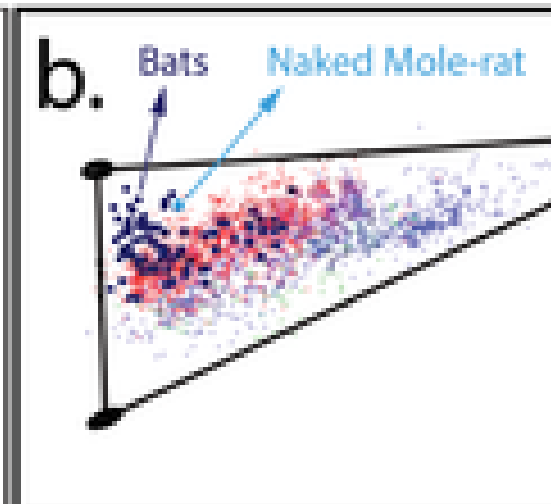
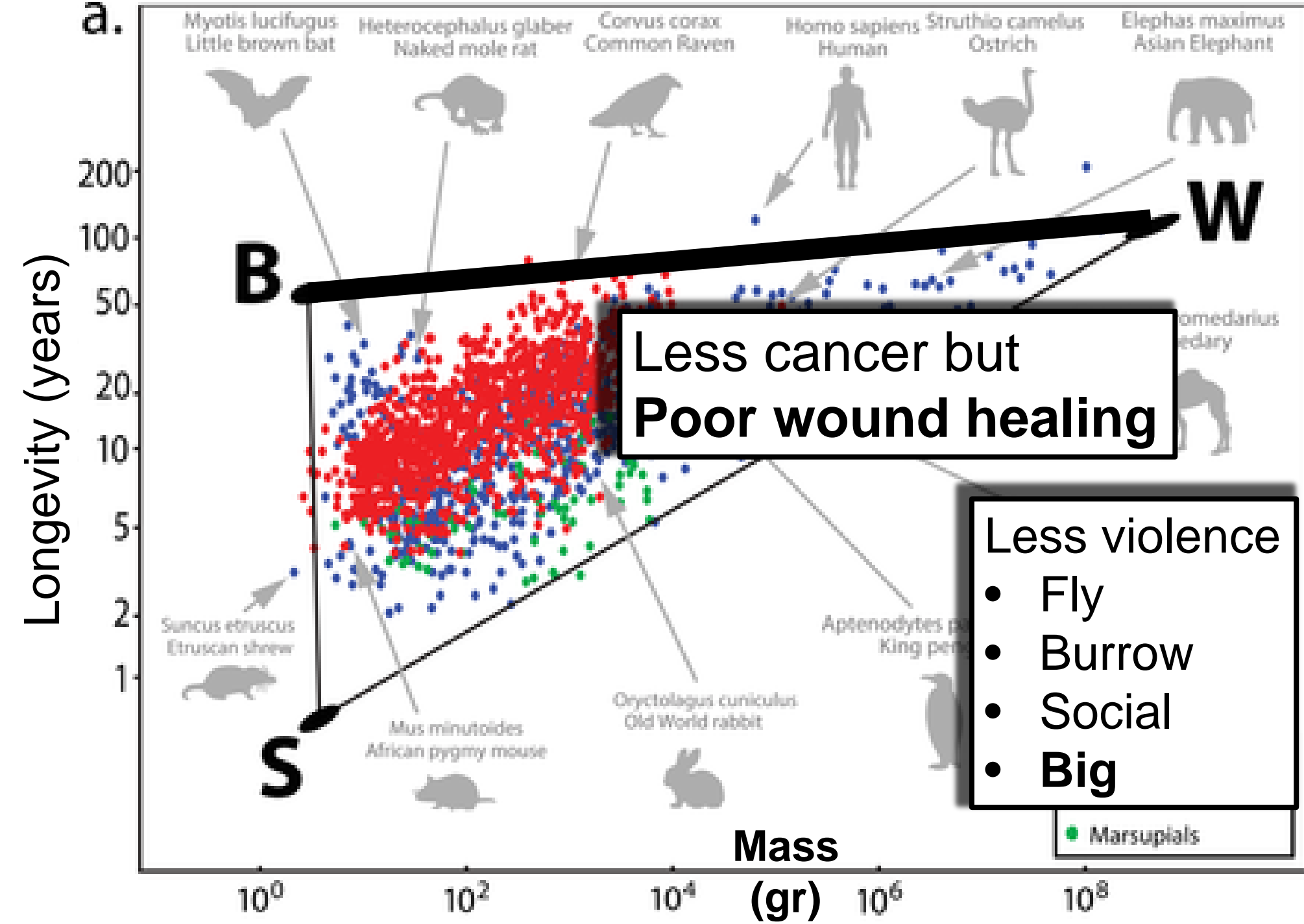
Lifespan x Body Mass

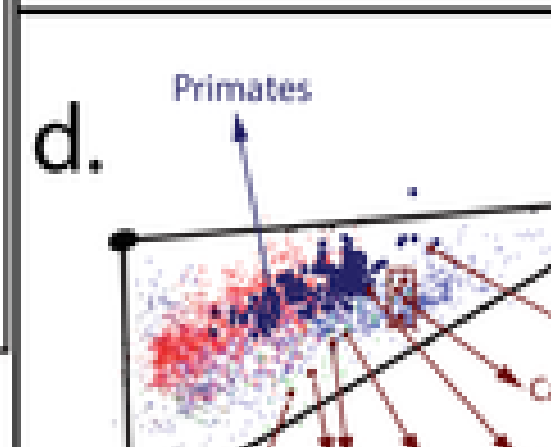
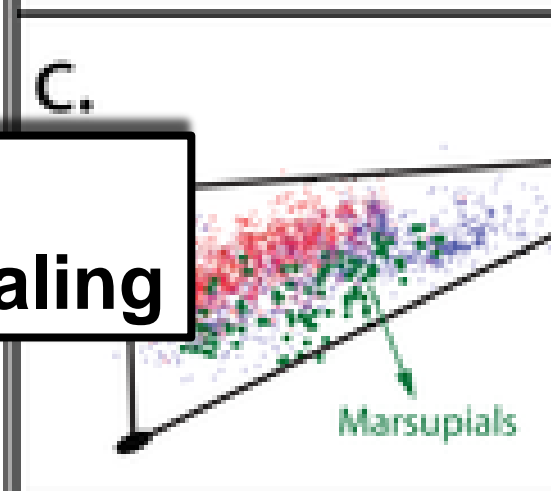
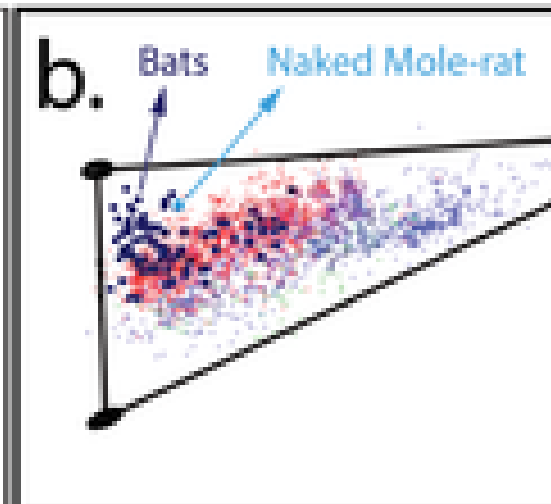
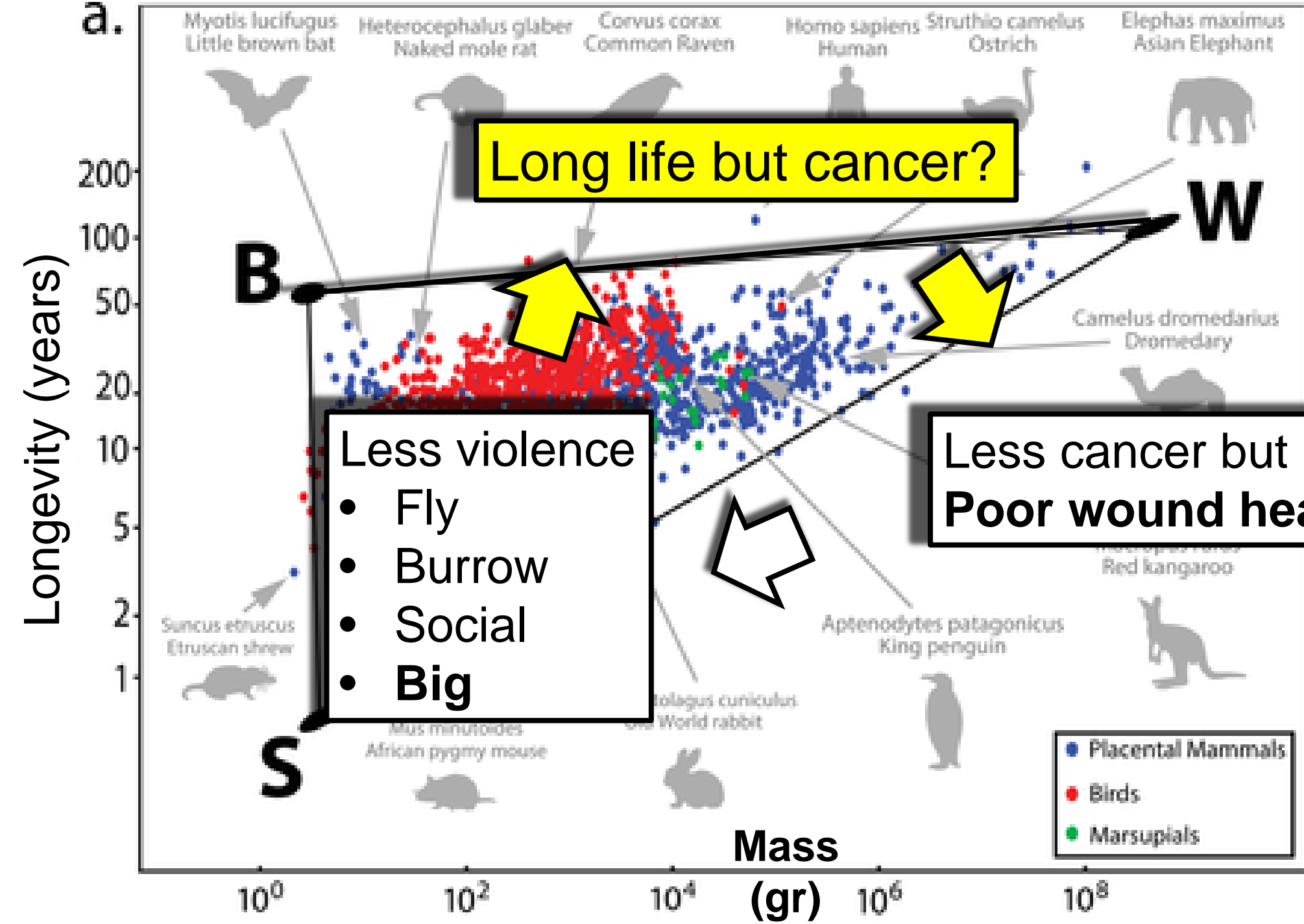
An illustration of **Peto's Paradox**. **Cancer** is a disease of uncontrolled cell growth and division, and the risk of developing cancer increases with the number of cell divisions during the lifetime of an organism. Thus, the expected **cancer rate for large and/or long-lived species is higher** than for smaller short-lived ones.

The *solid red line* indicates a linear relationship between cancer rate and $(\text{body mass}) \times (\text{lifespan})$ and the *dashed red line* represents an approximation of the expected cancer rate assuming a model describing the probability of an individual developing colorectal cancer after a given number of cell divisions [4]. The *solid blue line* represents the observation that there is no relationship between cancer risk and (body

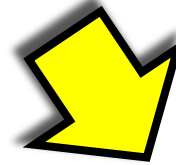
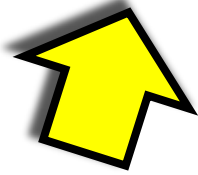








Long life but cancer?

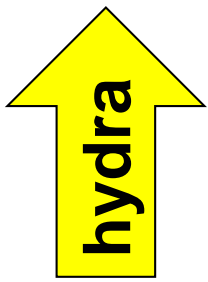


Less violence

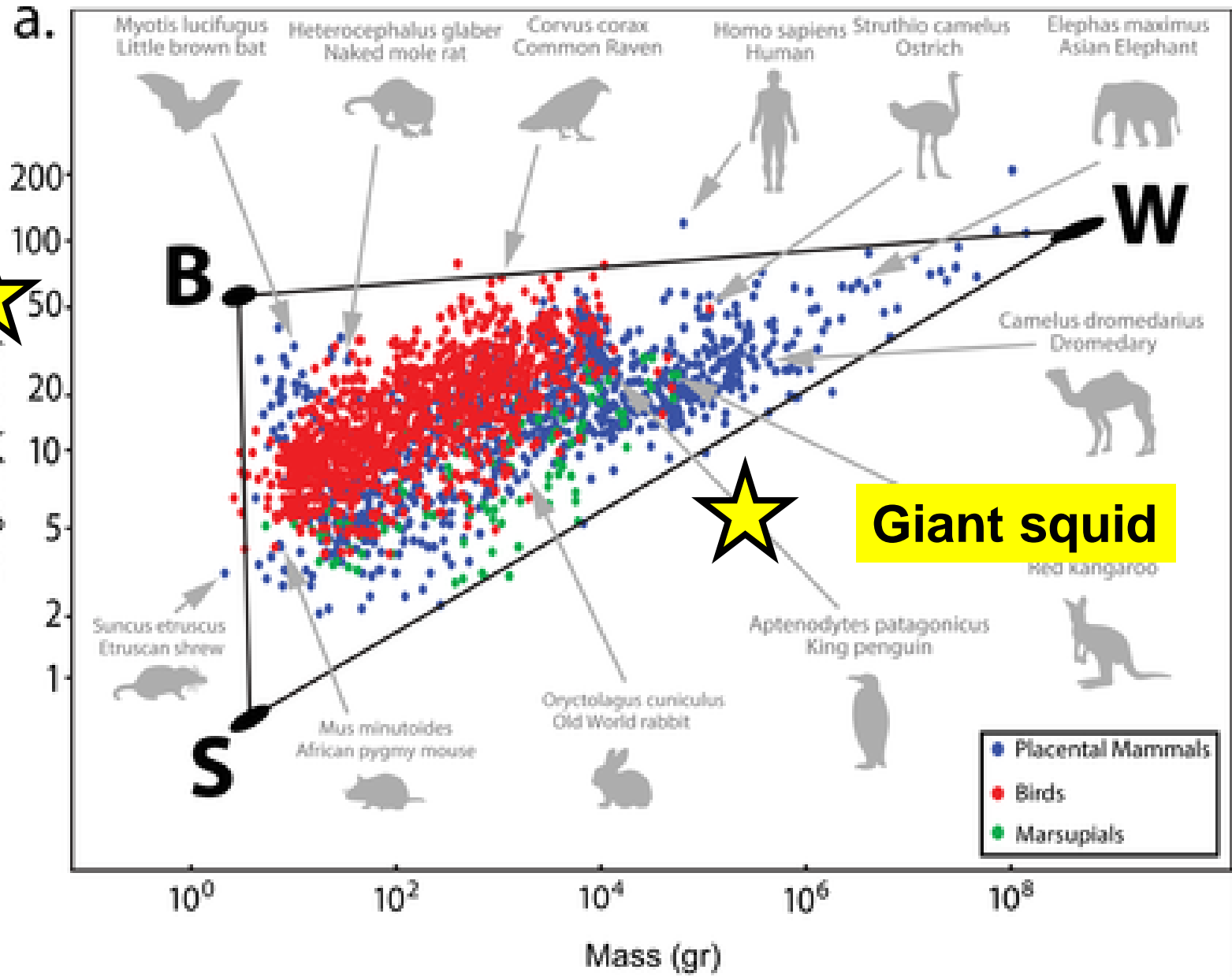
- Fly
- Burrow
- Social
- **Big**

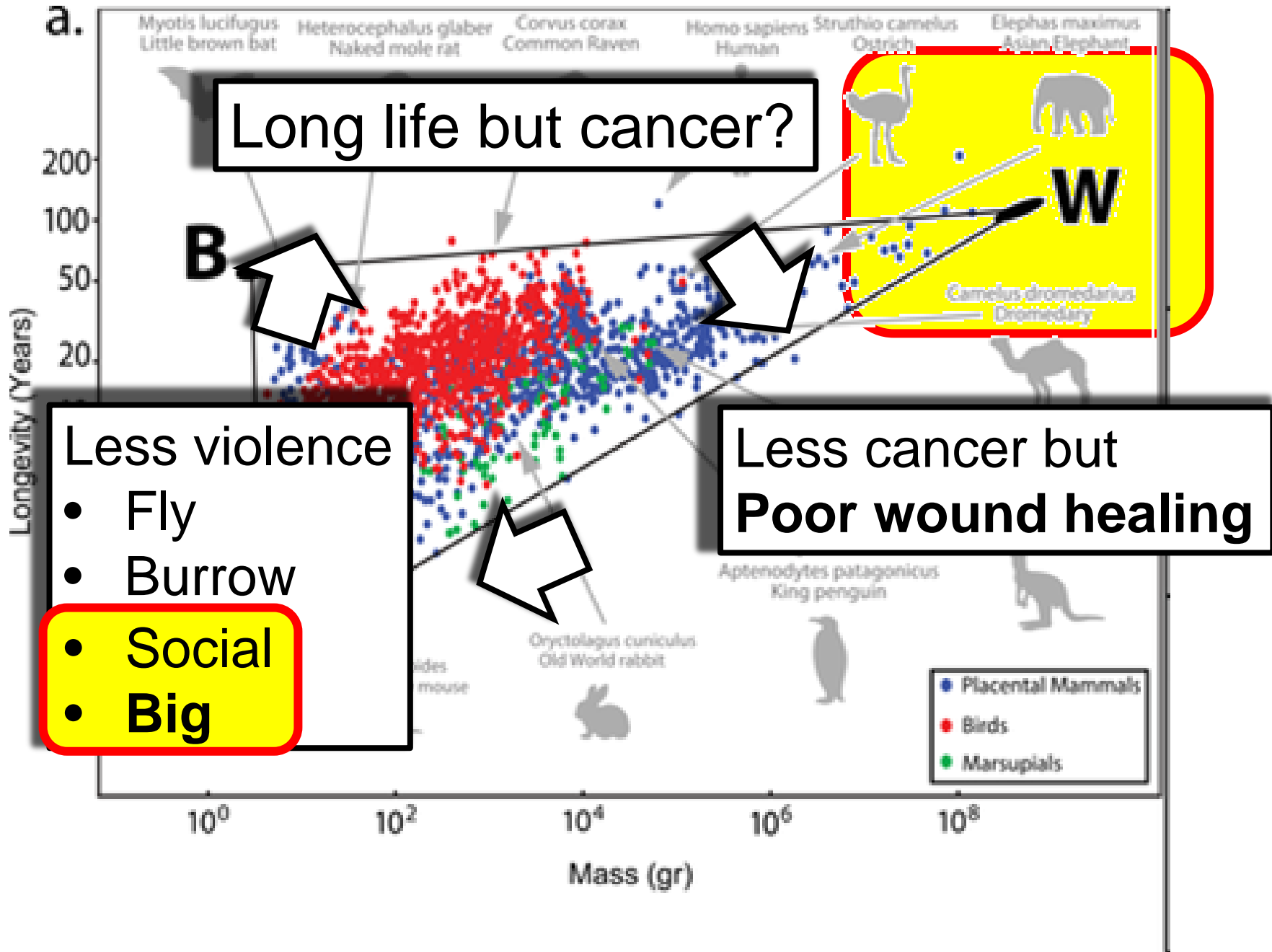


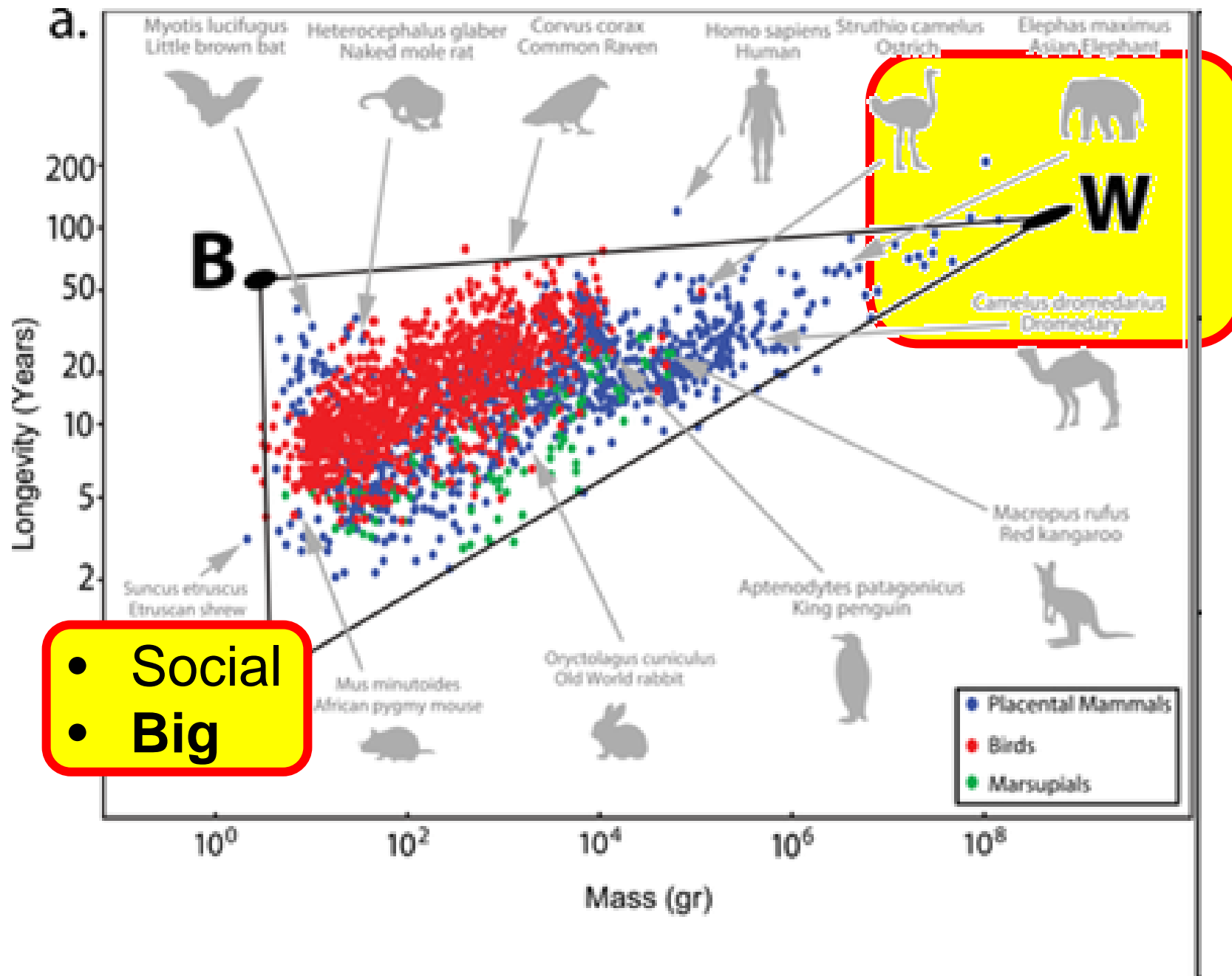
Less cancer but
Poor wound healing



Termite queen?







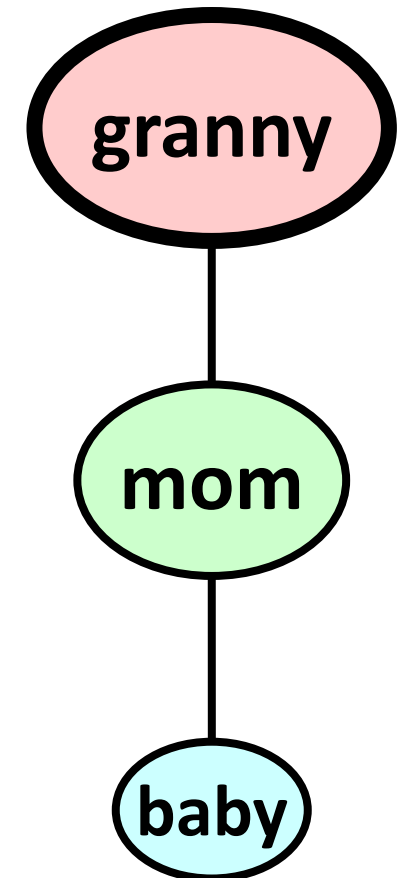
Elephants
Orcas

- Social
- Big

Social Architectures

- Atomic network elements
- Human examples?
- Stability and robustness?
- Scalability?

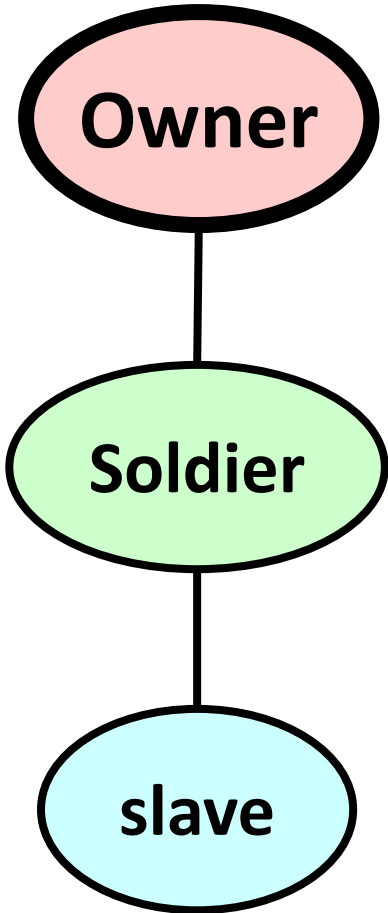
Bonobos
Elephants
Orcas
Baboons?



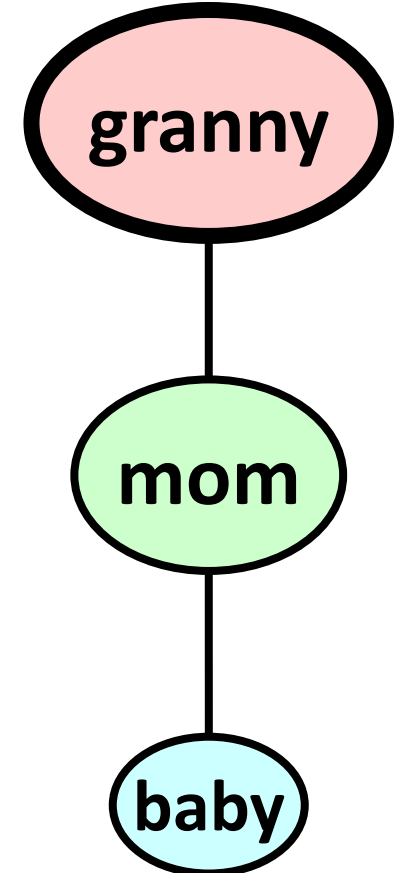
Chimps
Humans
Baboons?

Social Architectures

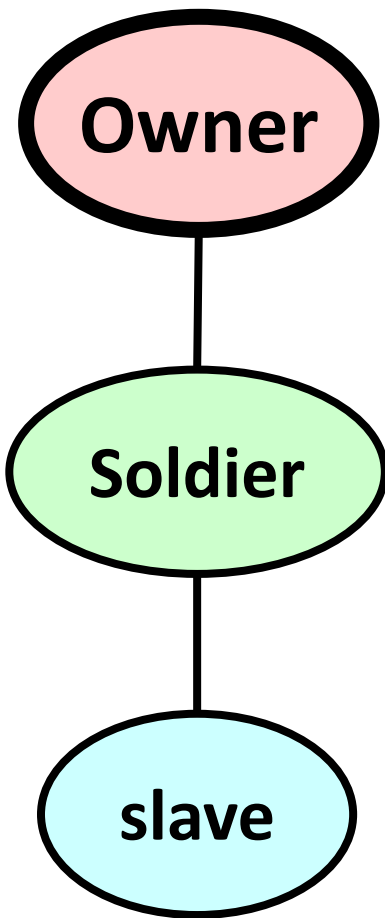
Bonobos
Elephants
Orcas
Baboons?



- Atomic network elements
- Human examples
- Stability and robustness
- Scalability



Warning: may be offensive to everyone, but especially humans



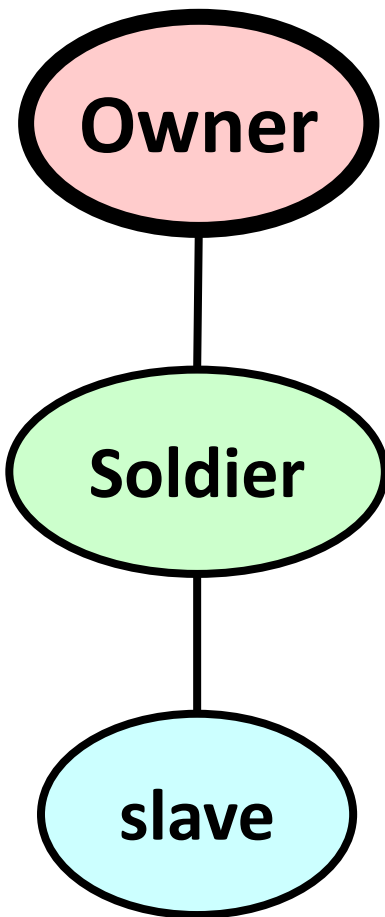
Dominance

**Near
term**

**Fear
Anger
Hatred
Violence**

**Chimps
Humans
Baboons?**

Atomic network elements

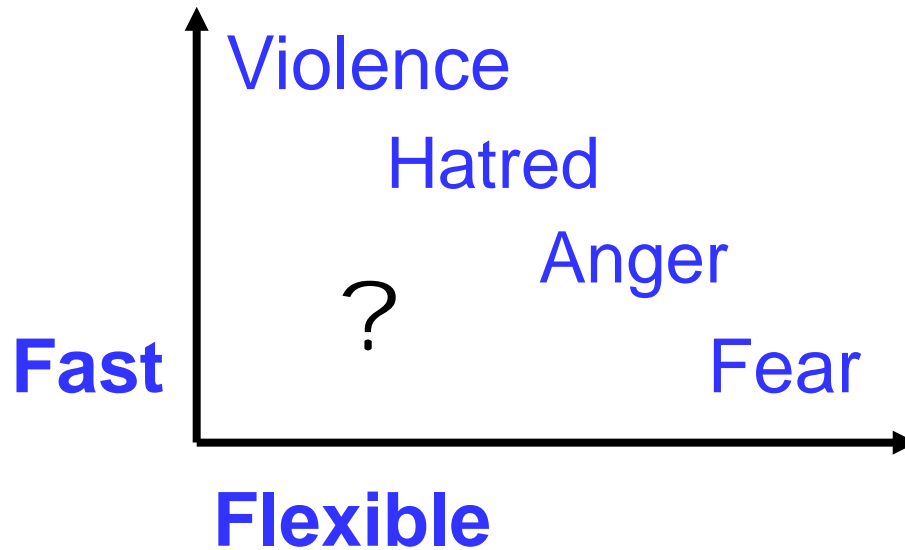


Dominance

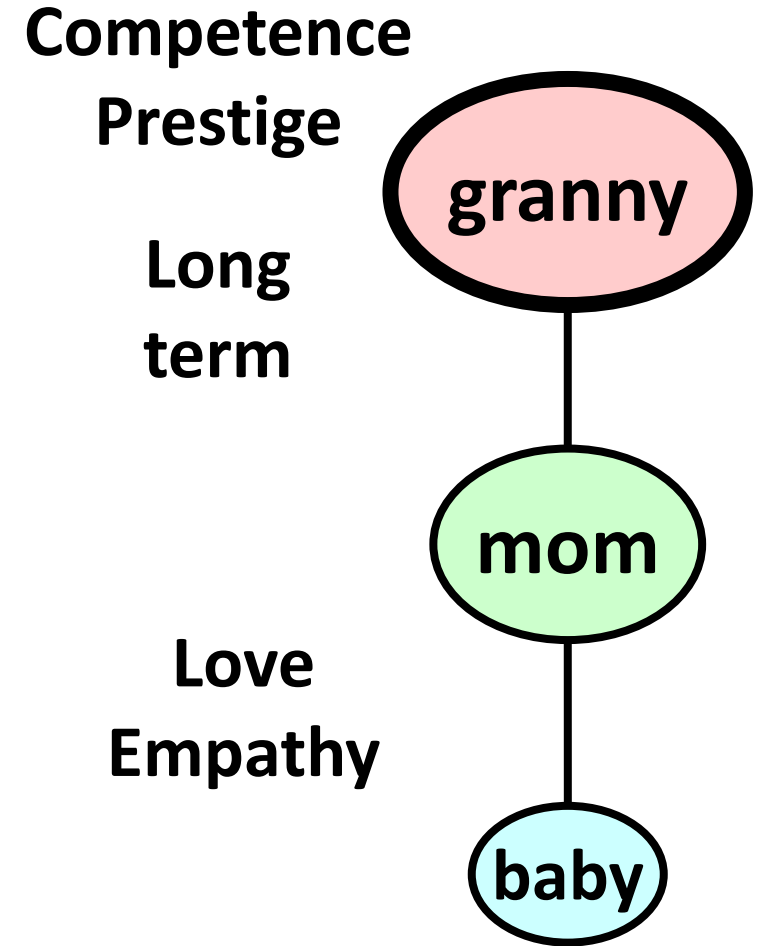
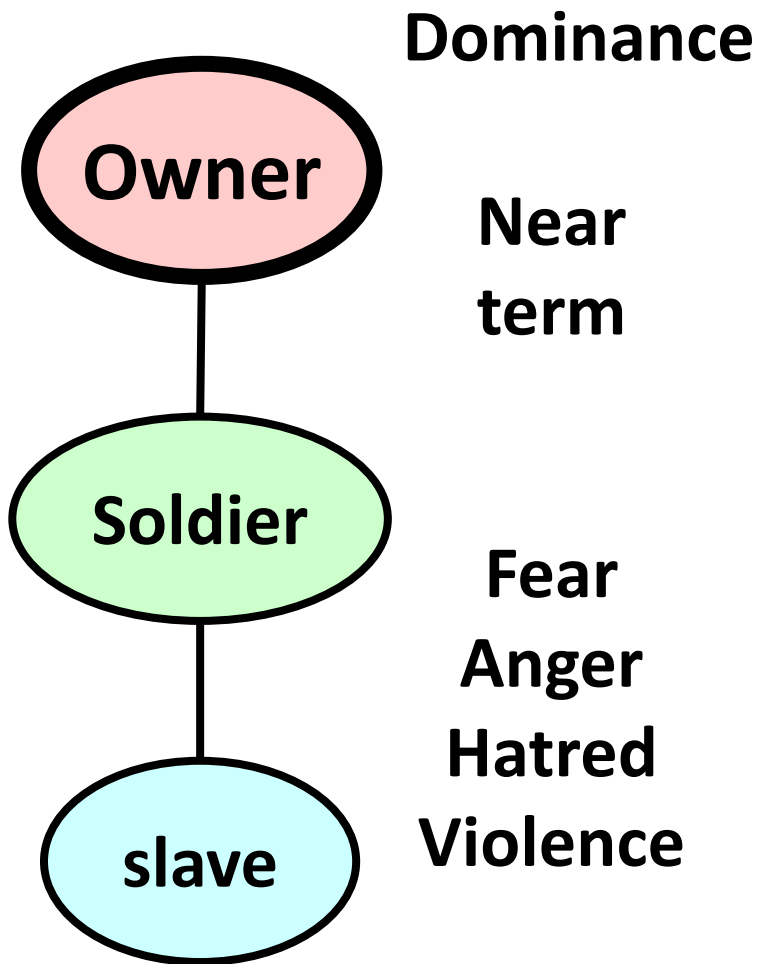
**Near
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**Fear
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**Chimps
Humans
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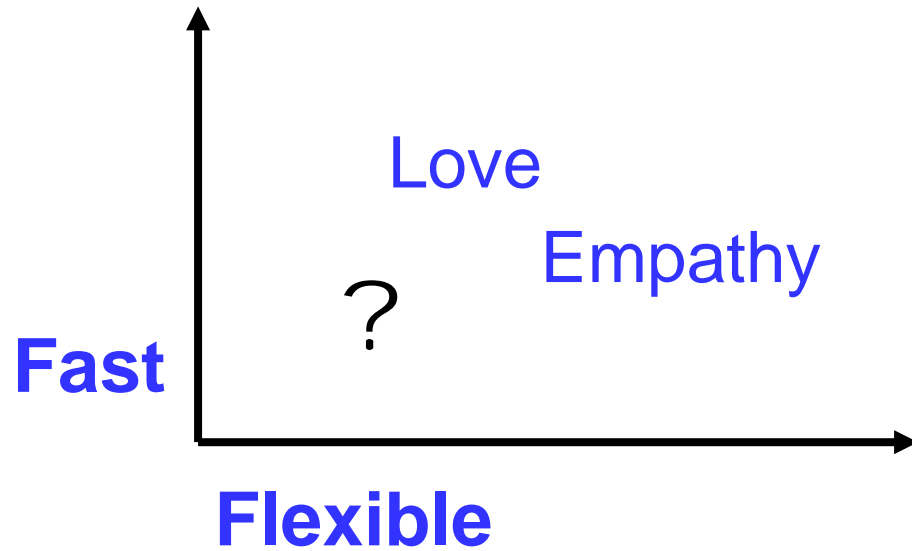


Atomic network elements



Atomic network elements

Bonobos
Elephants
Orcas
Baboons?

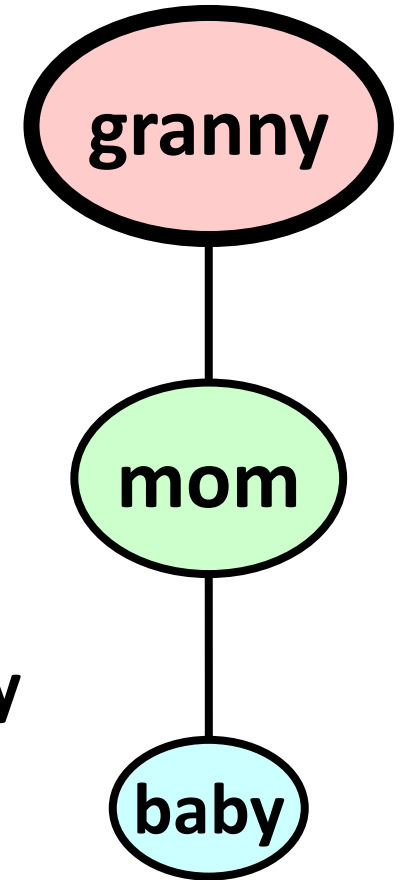


Competence

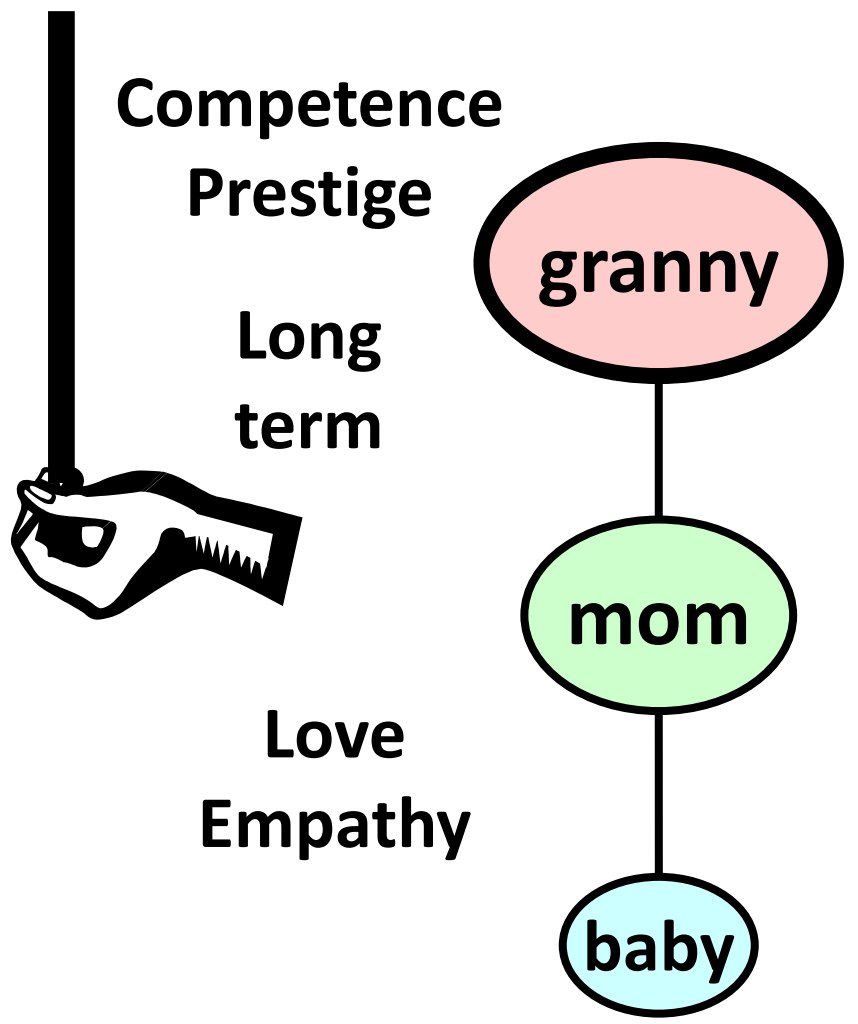
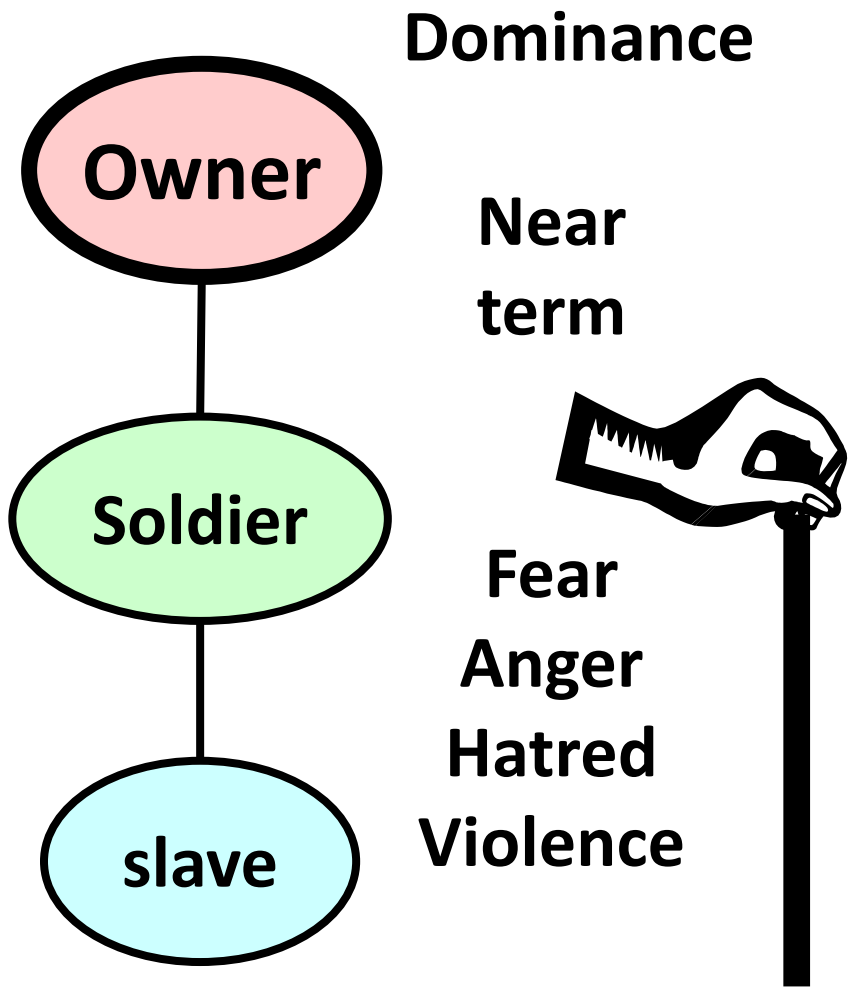
Prestige

Long
term

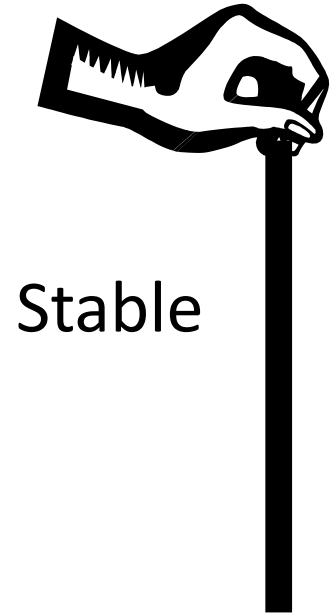
Love
Empathy



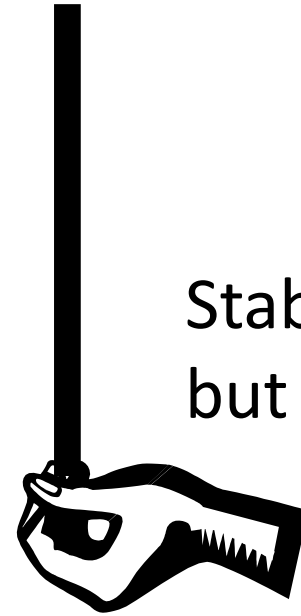
Atomic network elements



Atomic network elements

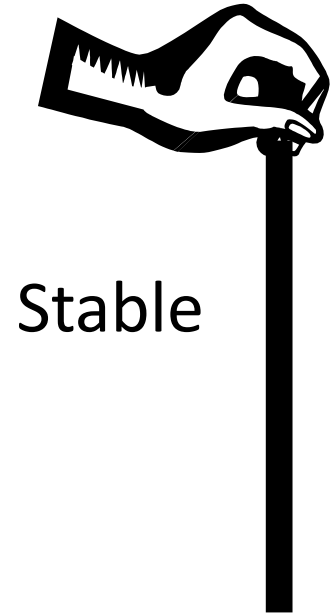


Stable



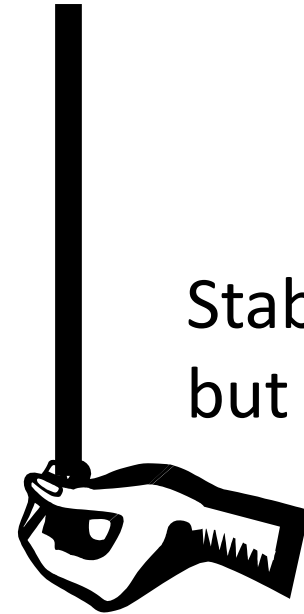
Stabilizable
but fragile

Other examples

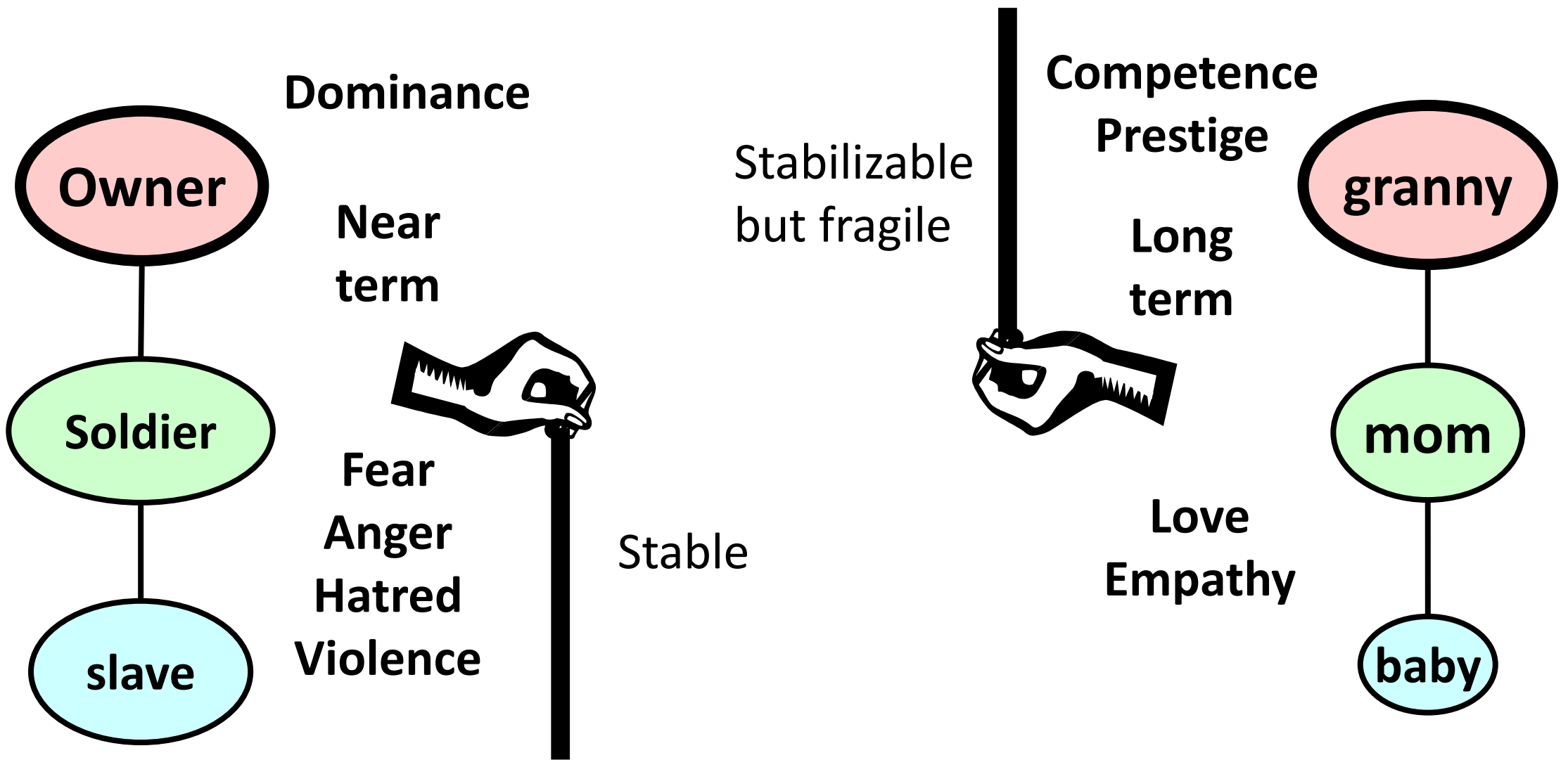


Death

Life

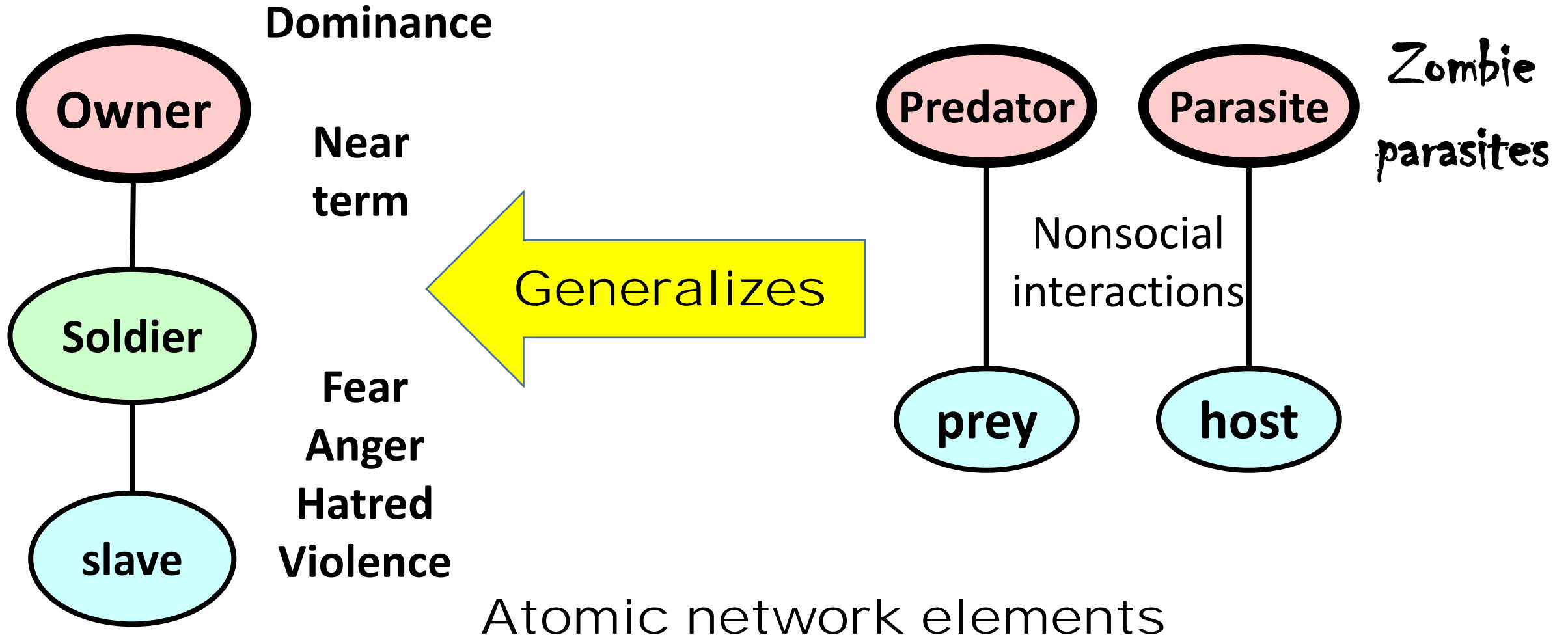


Stabilizable
but fragile

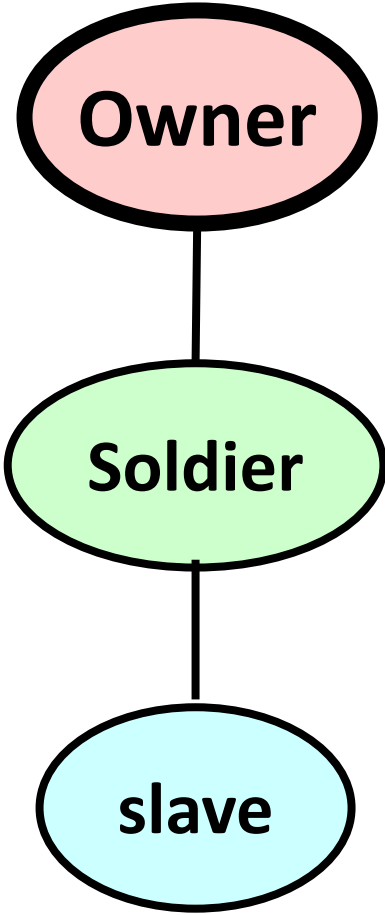


Atomic network elements

Owner = predator + parasite

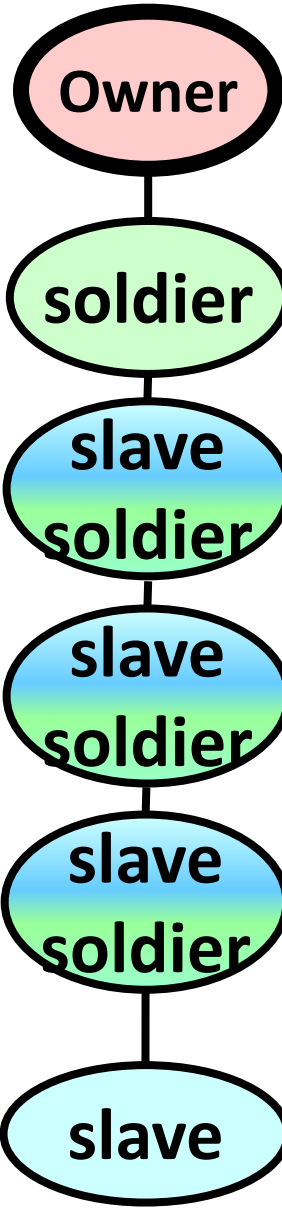


Scale?

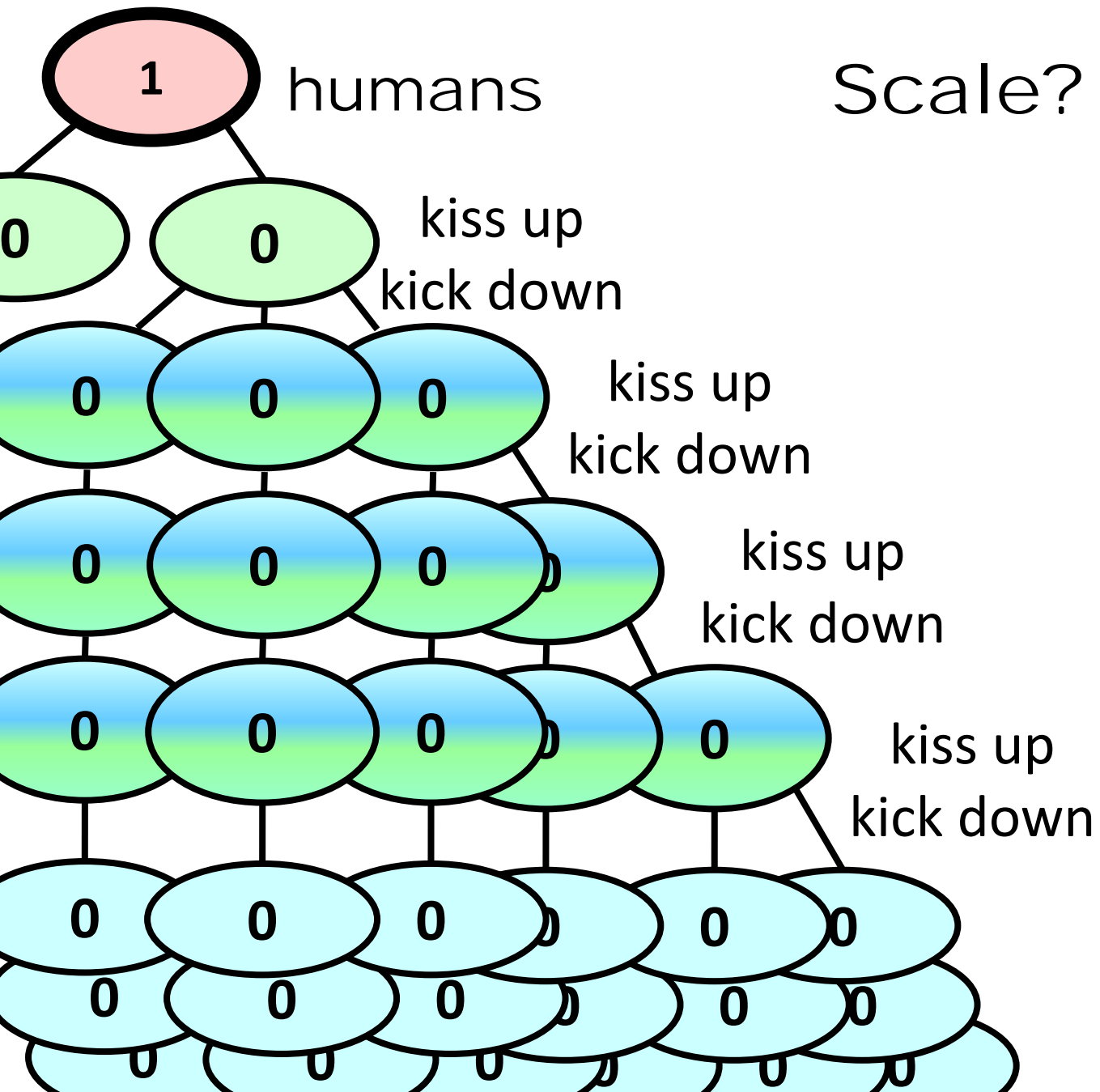


kiss up
kick down

Example:
chimps



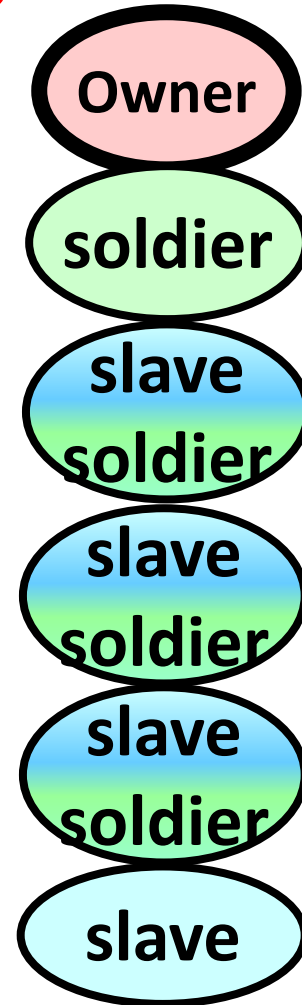
kiss up
kick down
kiss up
kick down
kiss up
kick down

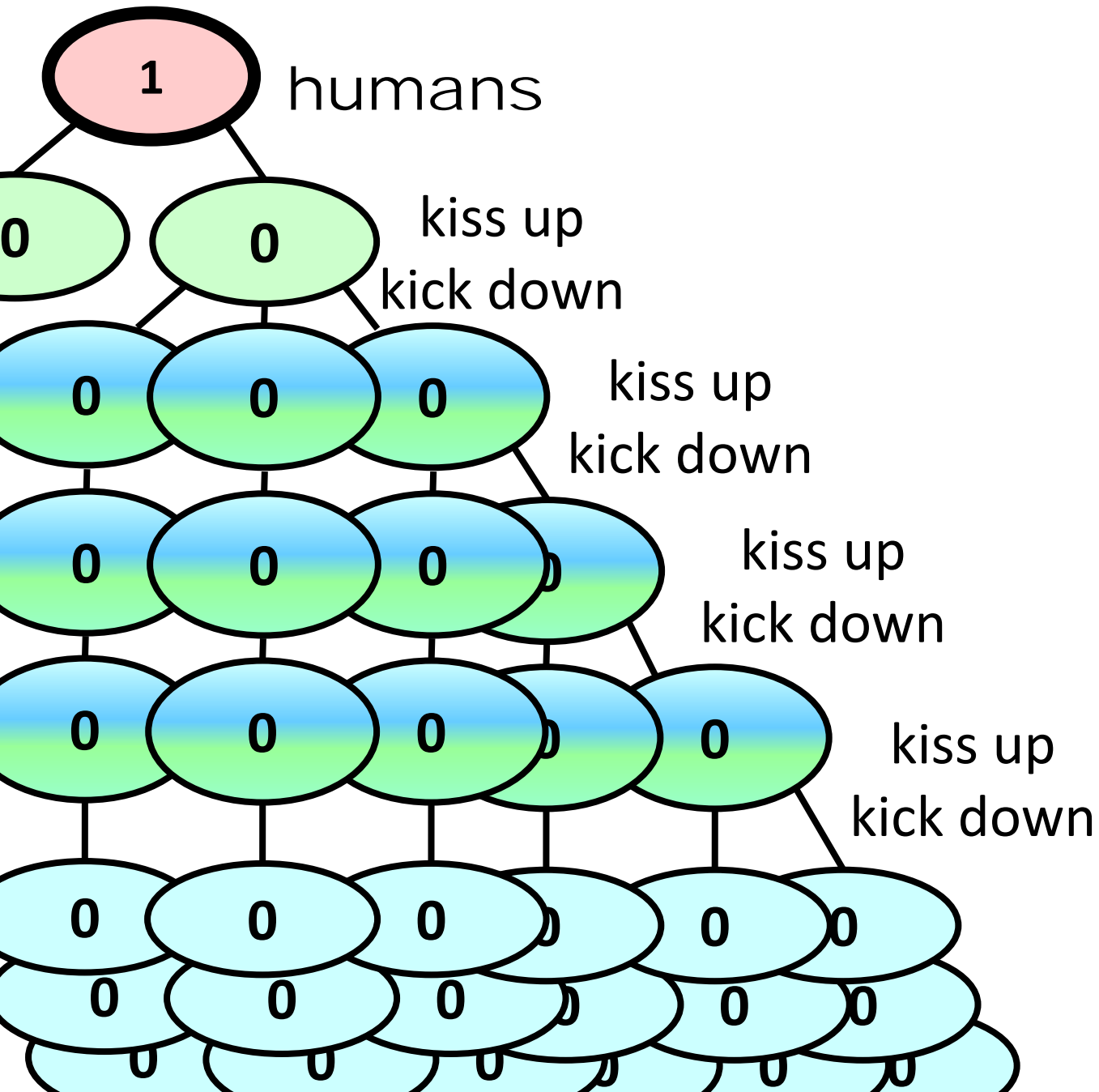


Stable and scalable

Goods

Control



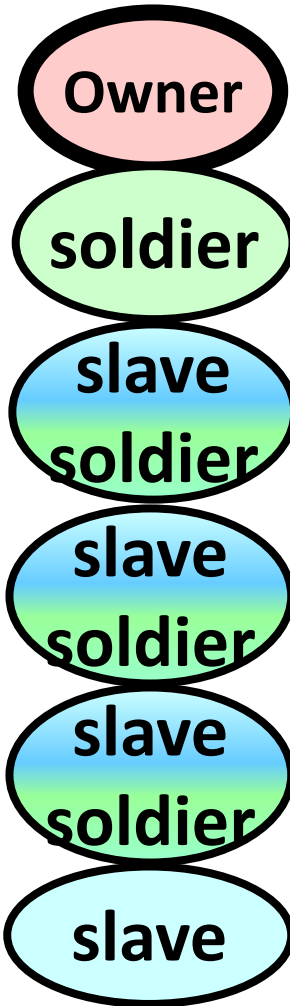
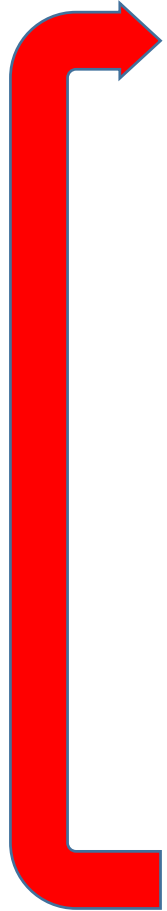


The biggest con

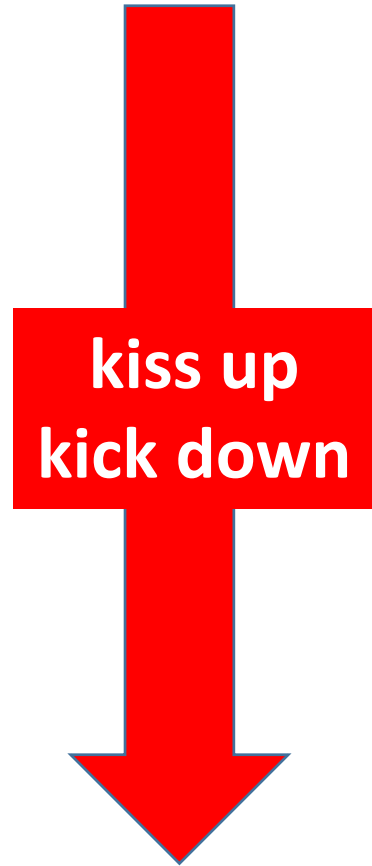
Empires

Stable and
scalable

Goods



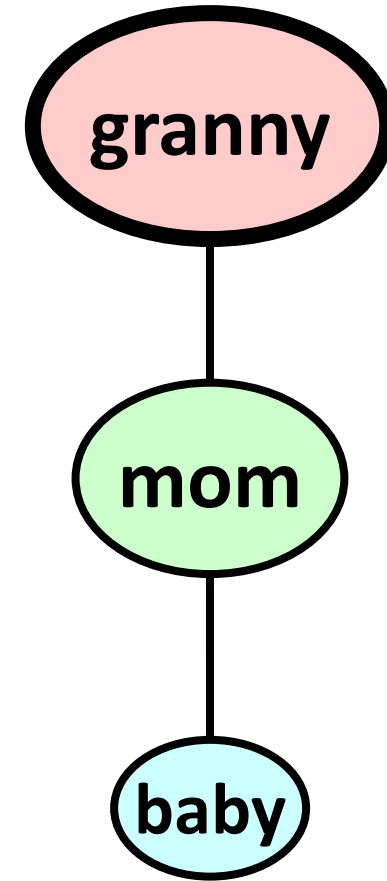
Control



So is Death

Stable but
not scalable?

Control



Goods

